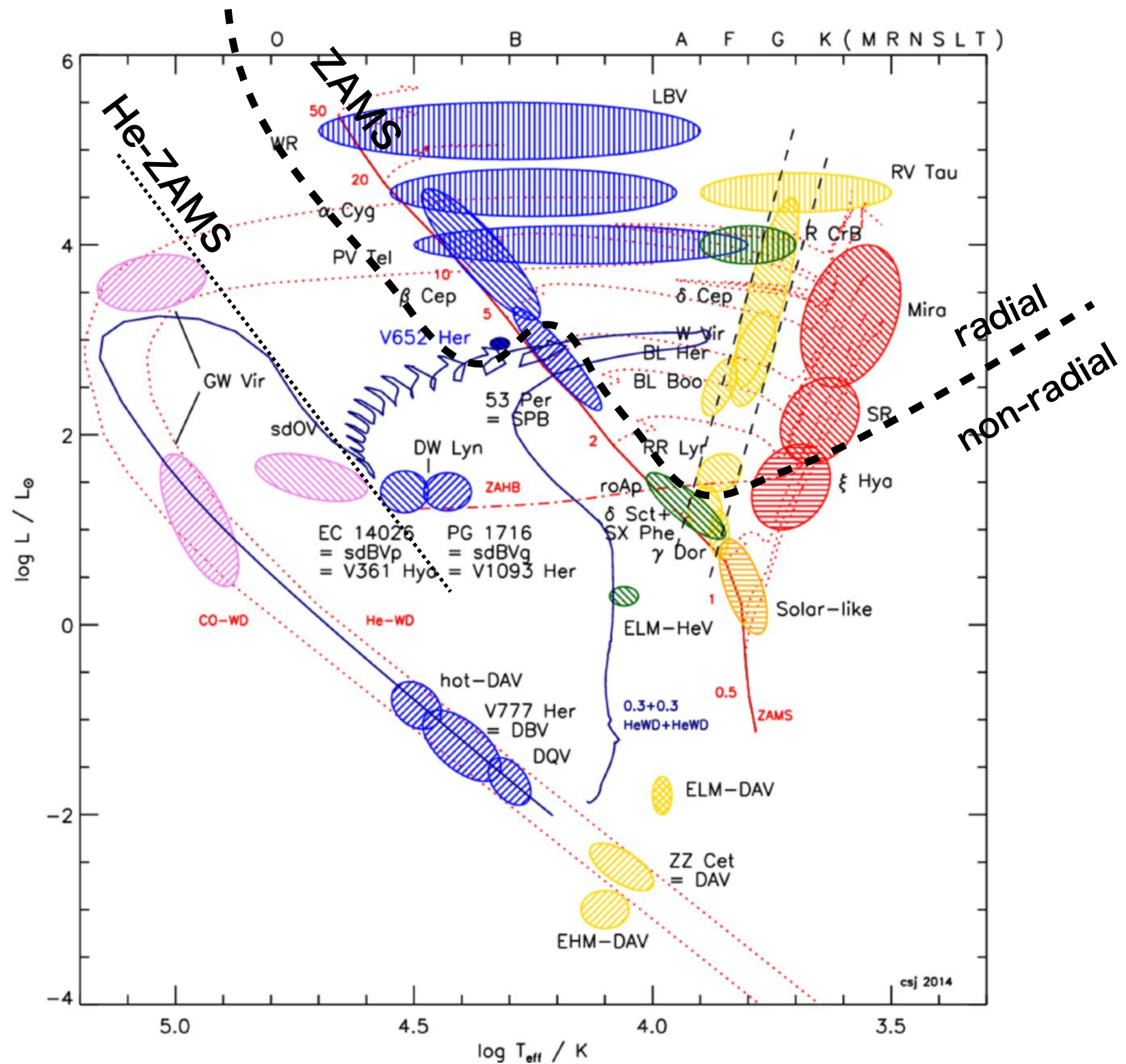


# 星震学による恒星進化モデルの検証

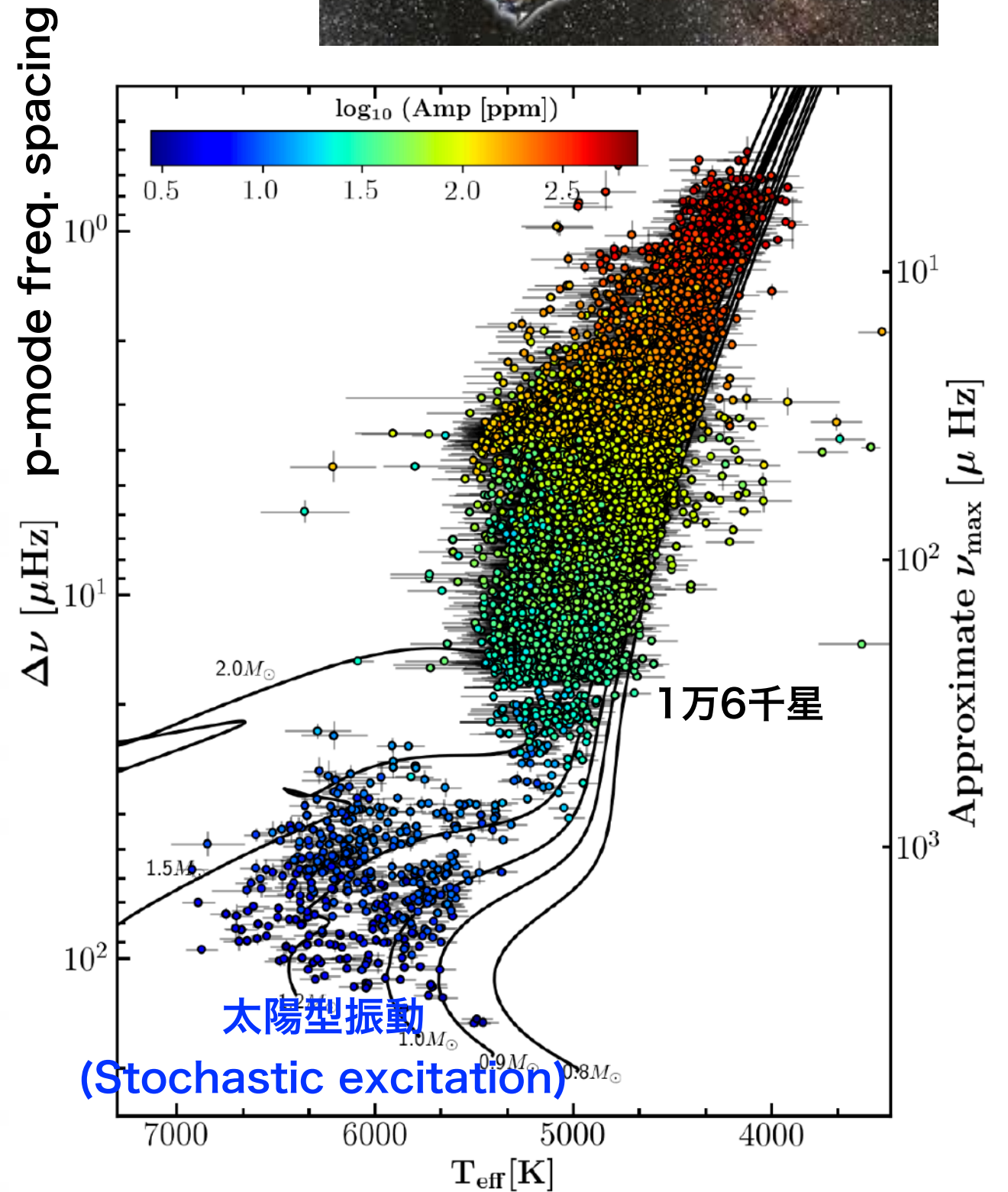
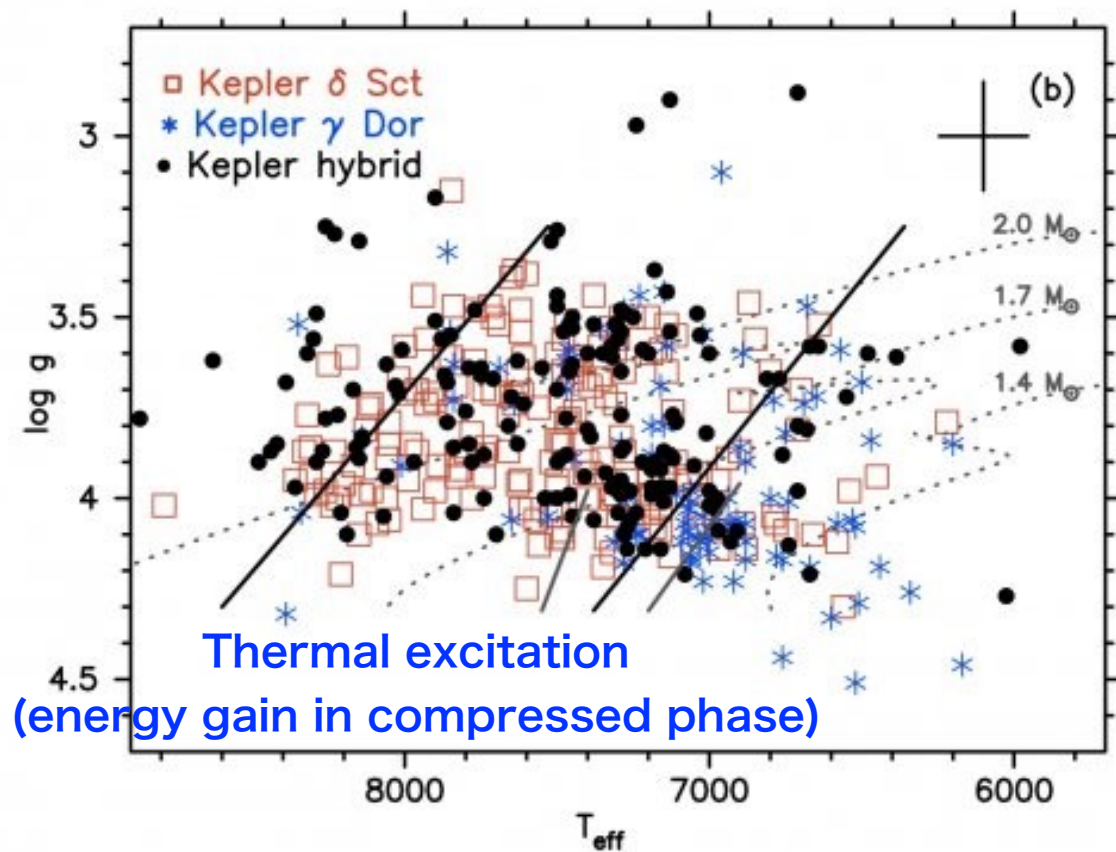
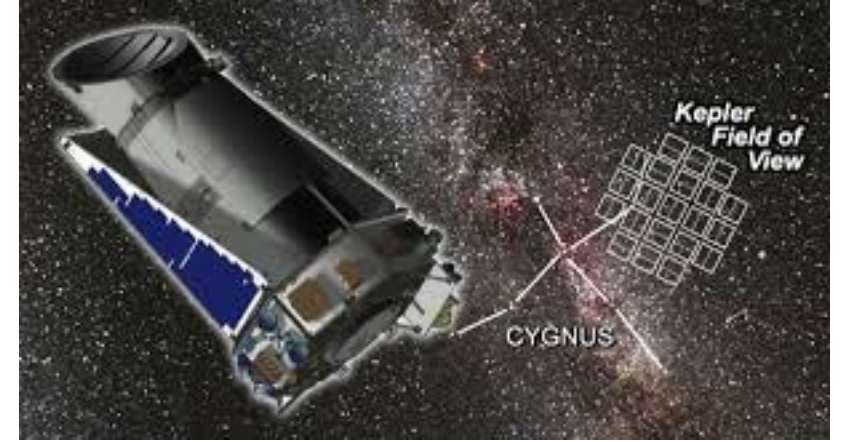
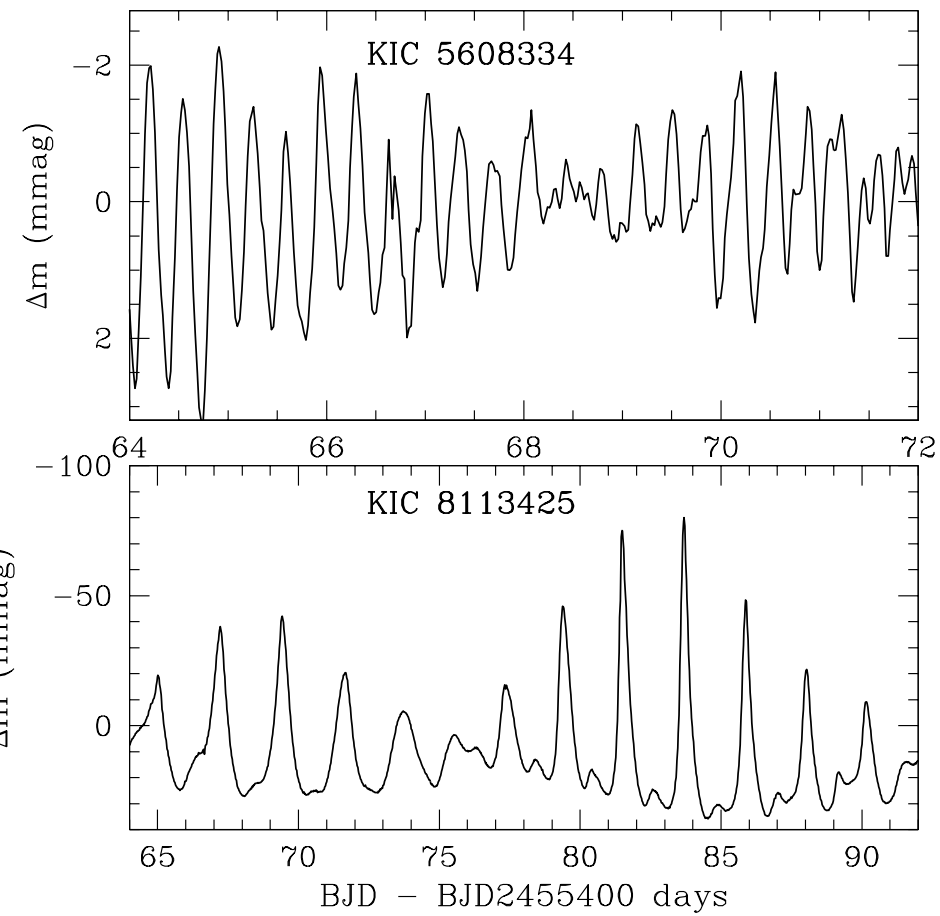
齊尾英行（東北大学）

1. 恒星振動(脈動) についての introduction
2. 恒星振動から知る、主系列星・赤色巨星の進化段階と内部自転速度
3. 恒星の振動が示す対流領域の広がり・混合・質量放出など
4. 恒星の振動が示す恒星合体の起こった証拠
5. r modes (Rossby waves in stars)

# Pulsational variables in the HRD



Jeffery et al. (2015)



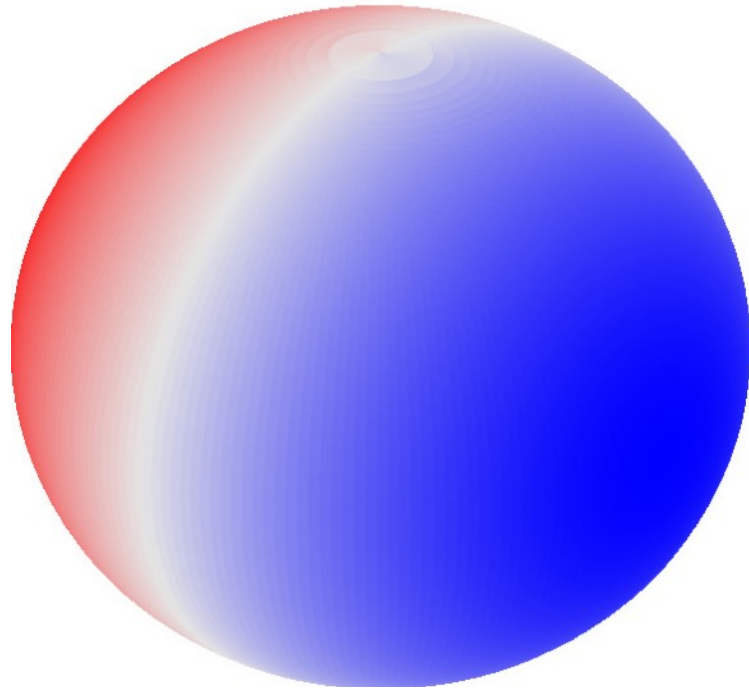
Yu et al. (2018)



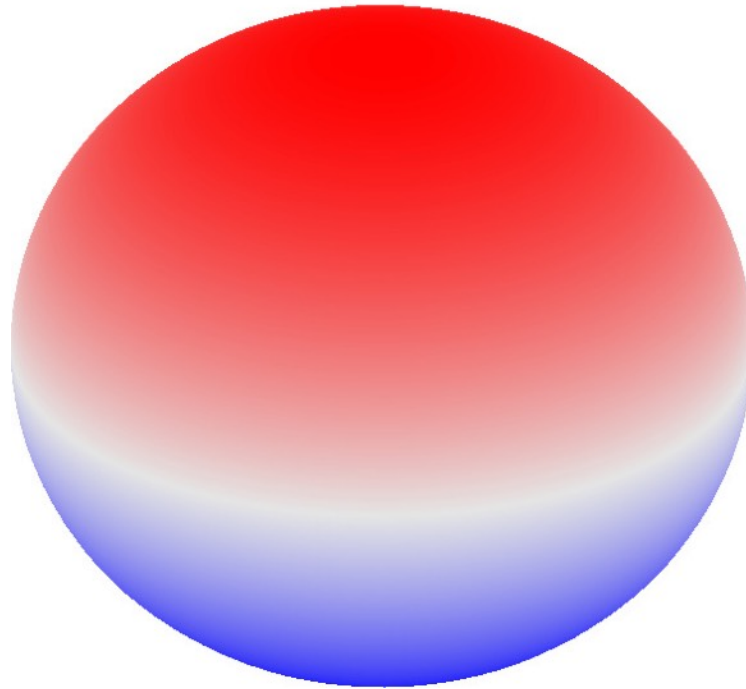
# Temp. variation of Non-radial pulsations

$$Y_{\ell}^m(\theta, \phi)$$

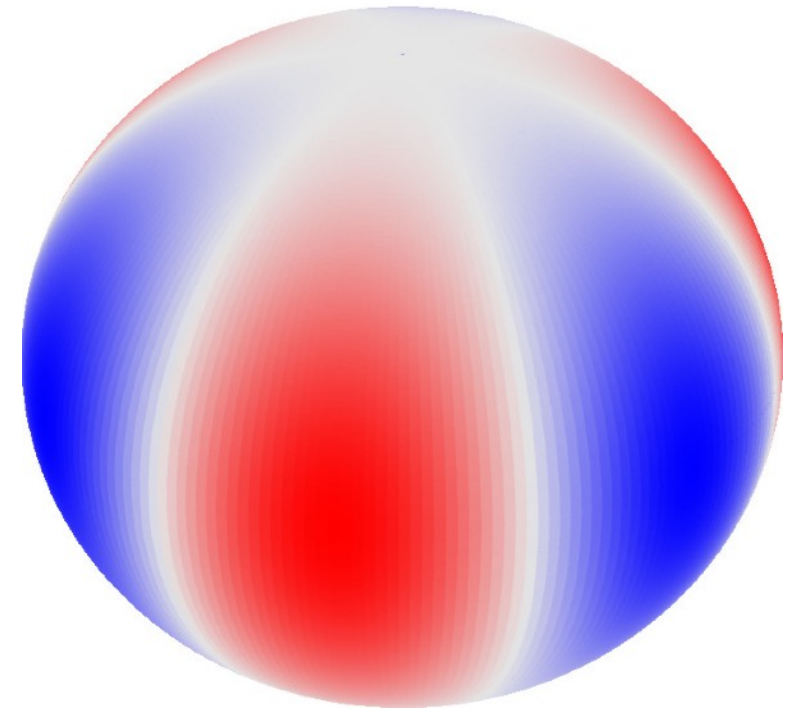
$$\ell = 1, m = \pm 1$$



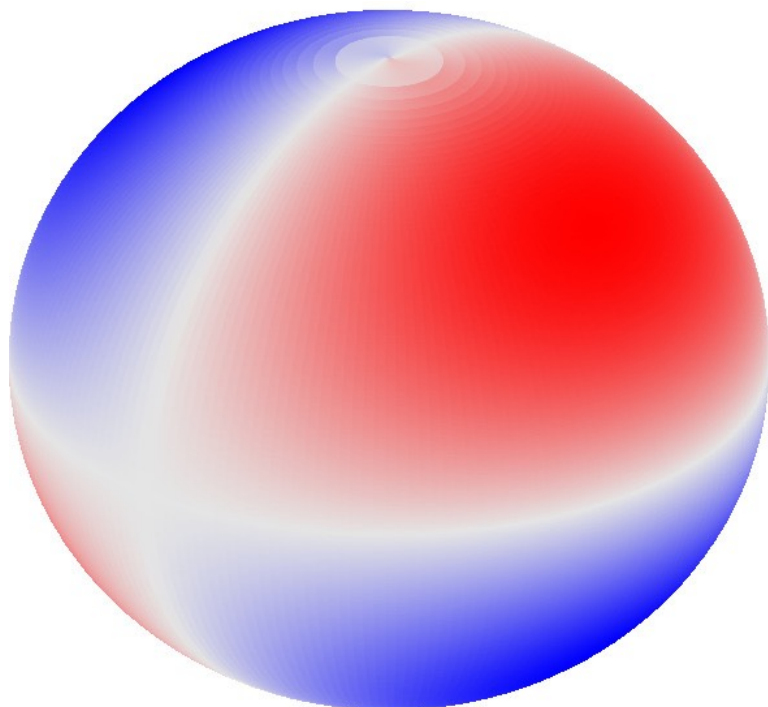
$$\ell = 1, m = 0$$



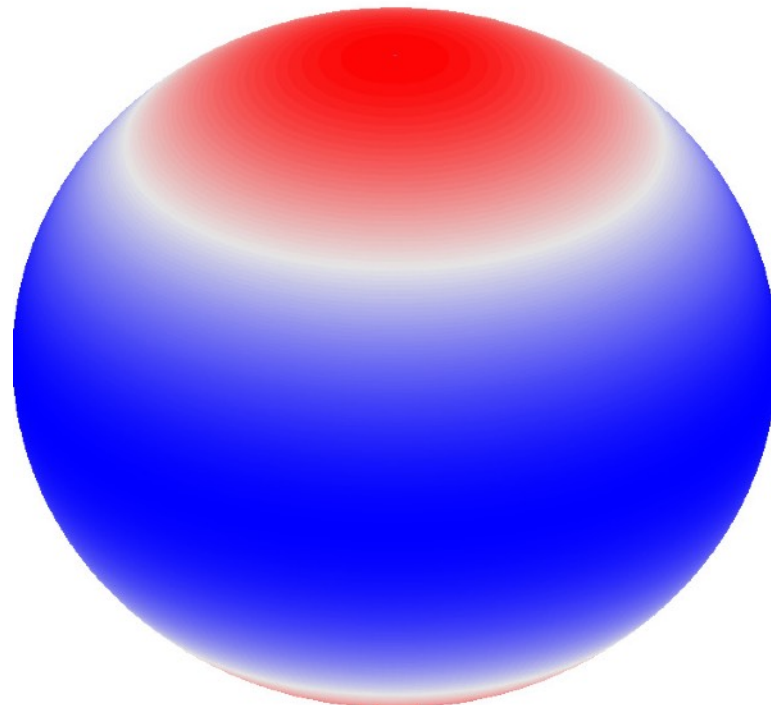
$$\ell = 3, m = \pm 3$$



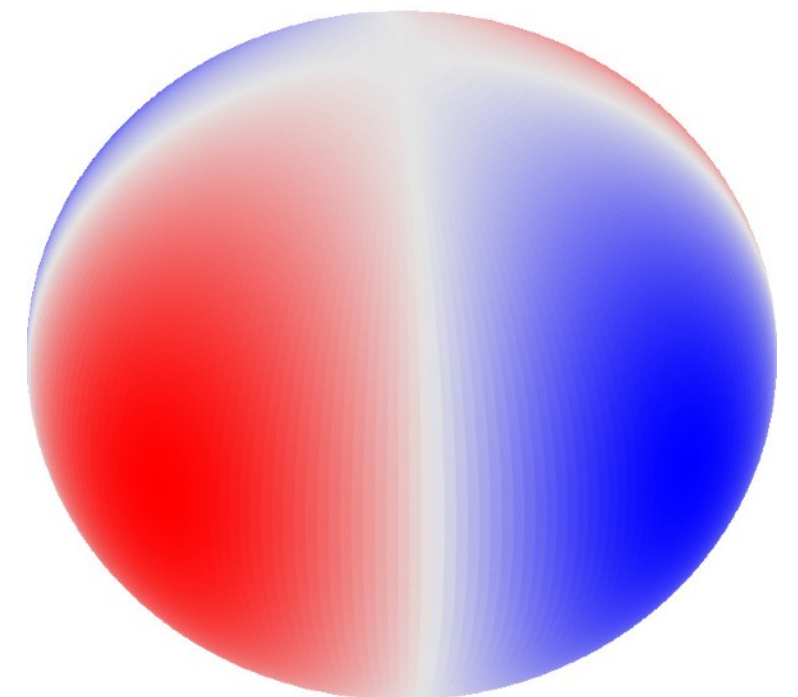
$$\ell = 2, m = \pm 1$$



$$\ell = 2, m = 0$$



$$\ell = 2, m = \pm 2$$





# p modes (radial & non-radial)

と

# g modes (non-radial)

$n \gg 1$

$\nu(\text{p mode}) \approx n\Delta\nu$

振動数間隔一定

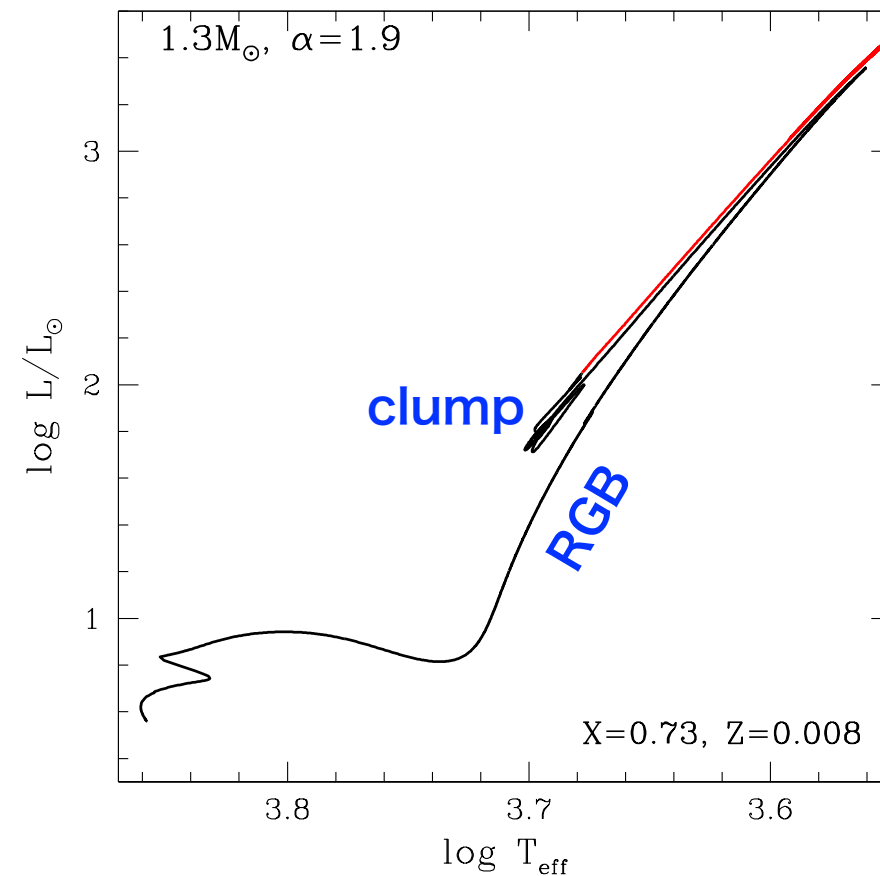
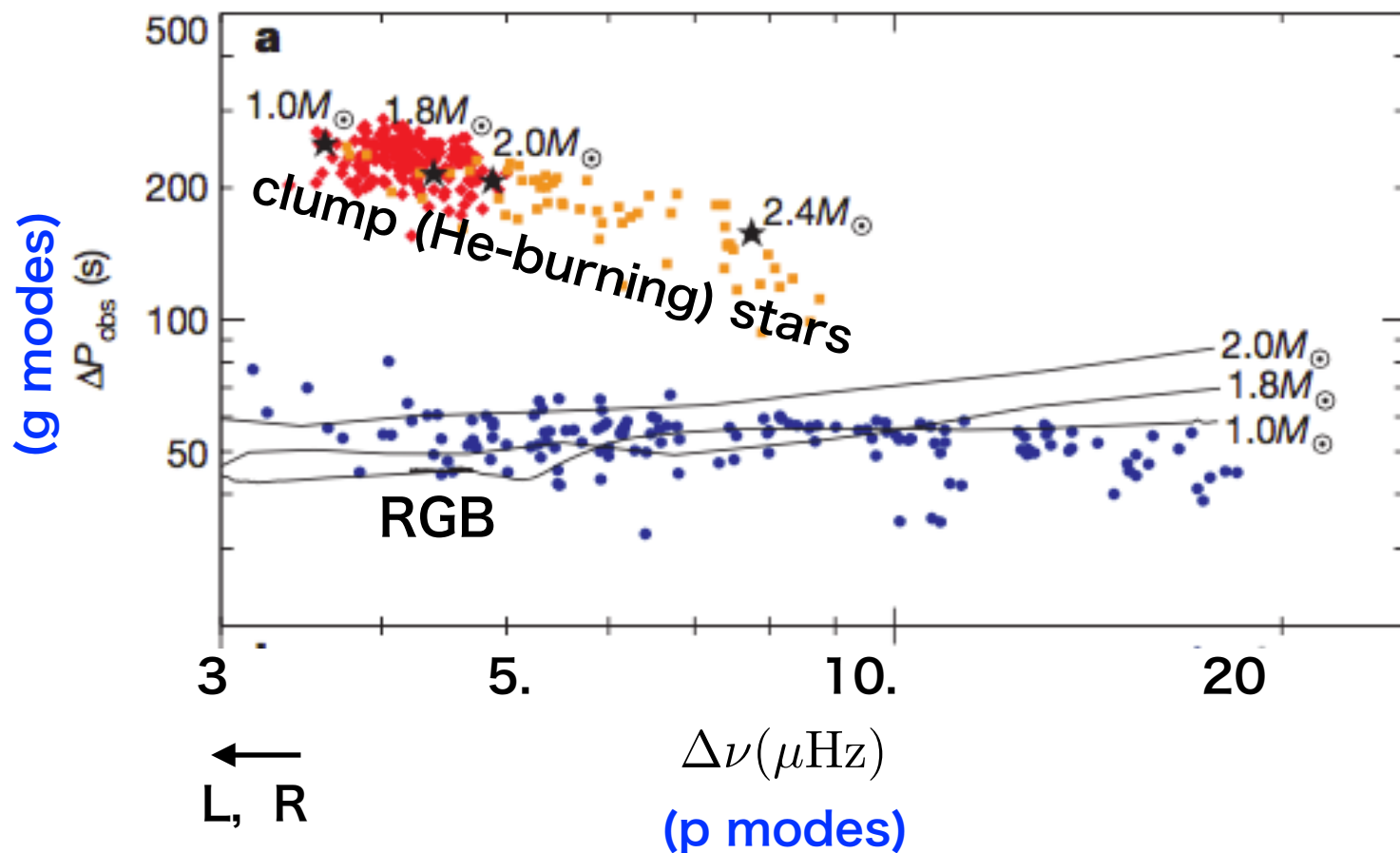
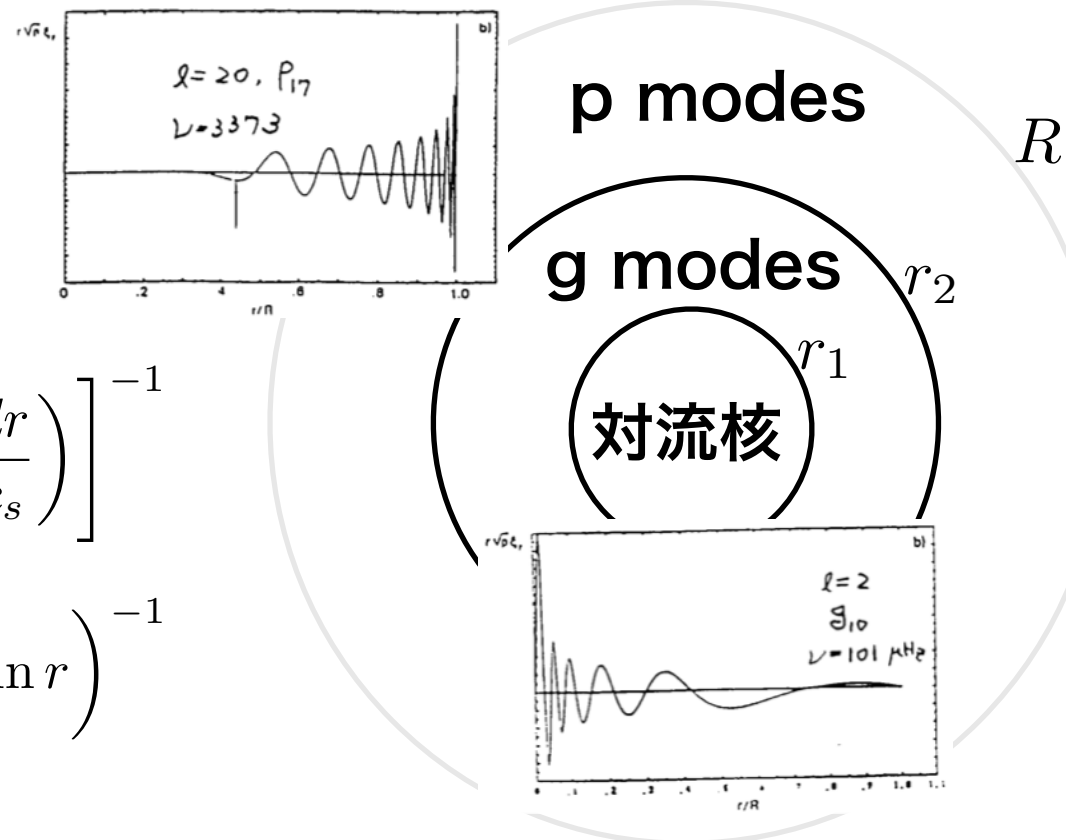
$$\Delta\nu = \left[ 2 \int_0^R \left( \frac{dr}{c_s} \right) \right]^{-1}$$

$P(\text{g mode}) \approx n\Delta P$

周期間隔一定

$$\Delta P = \frac{\pi}{\sqrt{2}} \left( \int_{r_1}^{r_2} N d \ln r \right)^{-1}$$

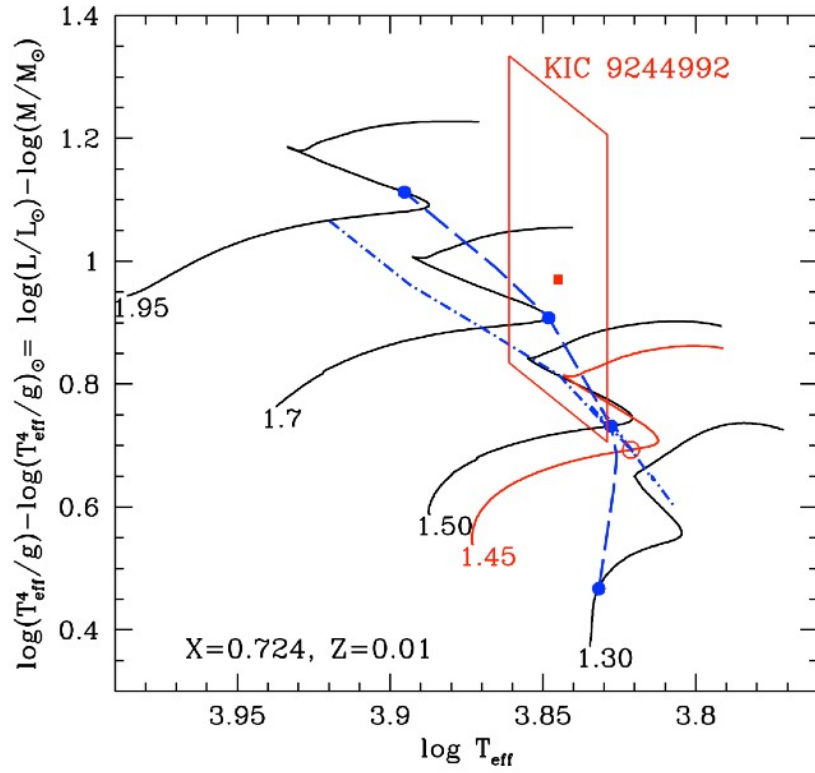
Brunt-Väisälä frequency  
(浮力による振動の基本振動数)  $N \propto \frac{g}{c_s}$



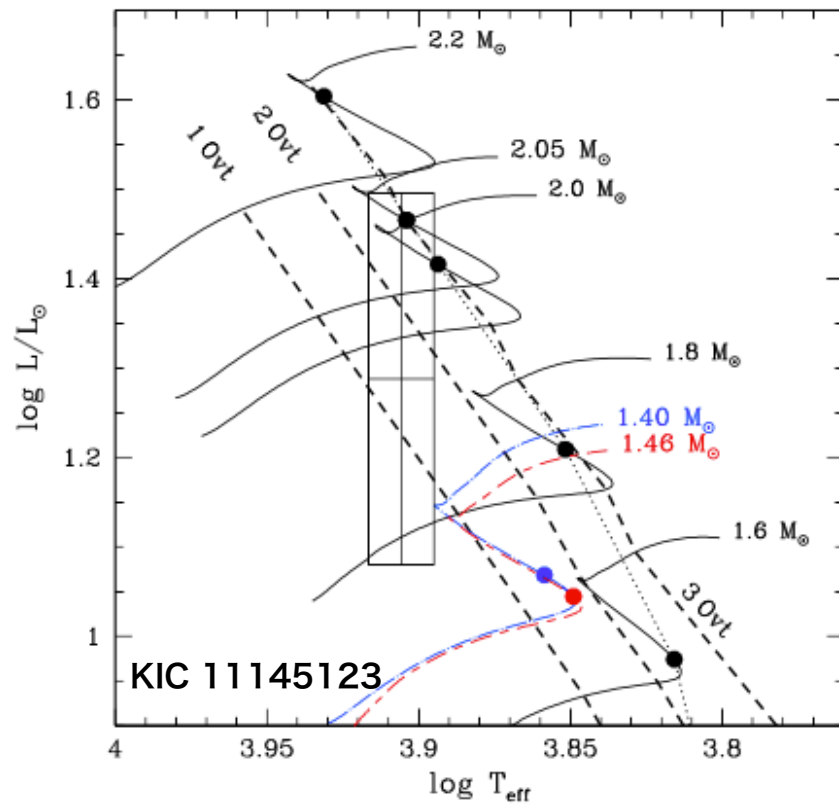
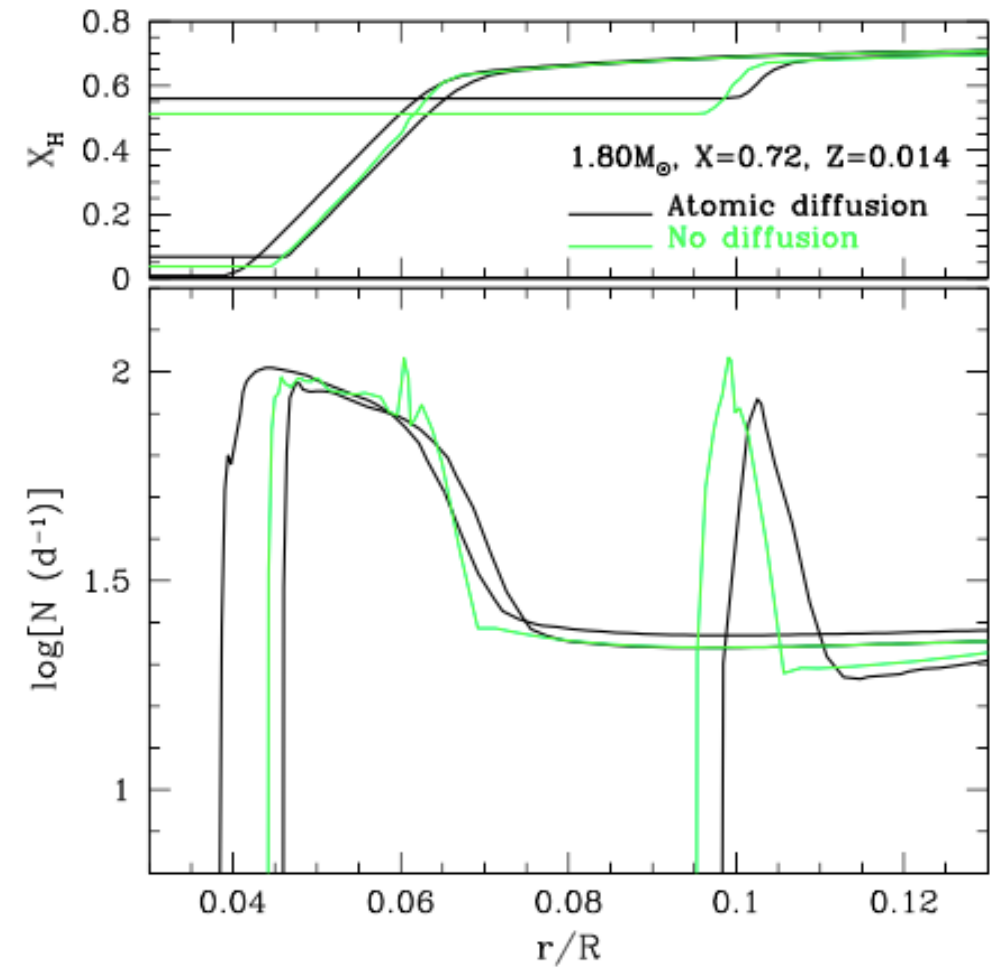
Bedding et al. (2011)

# Period spacing of g modes

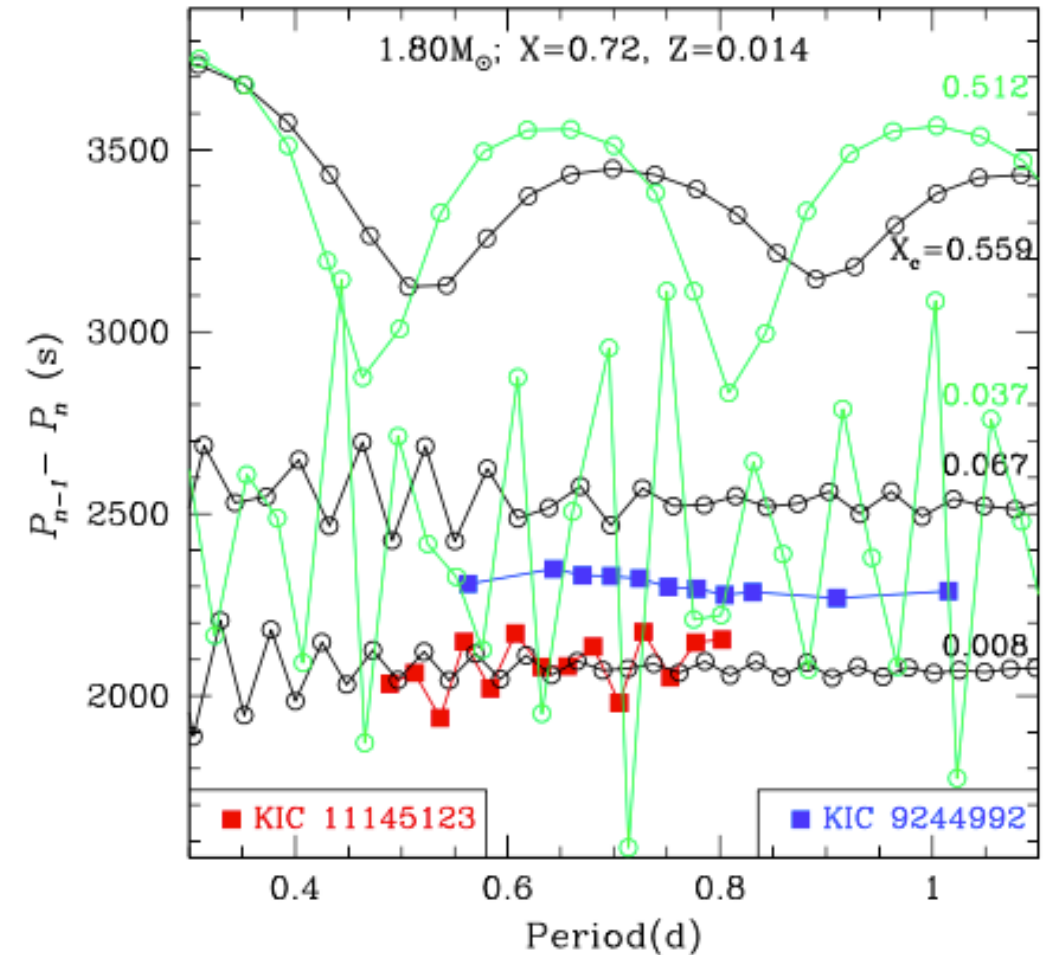
-- evolution stage &  
atomic (or turbulent) diffusion



Atomic diffusion  
or diffusion by weak  
turbulence must be  
occurring

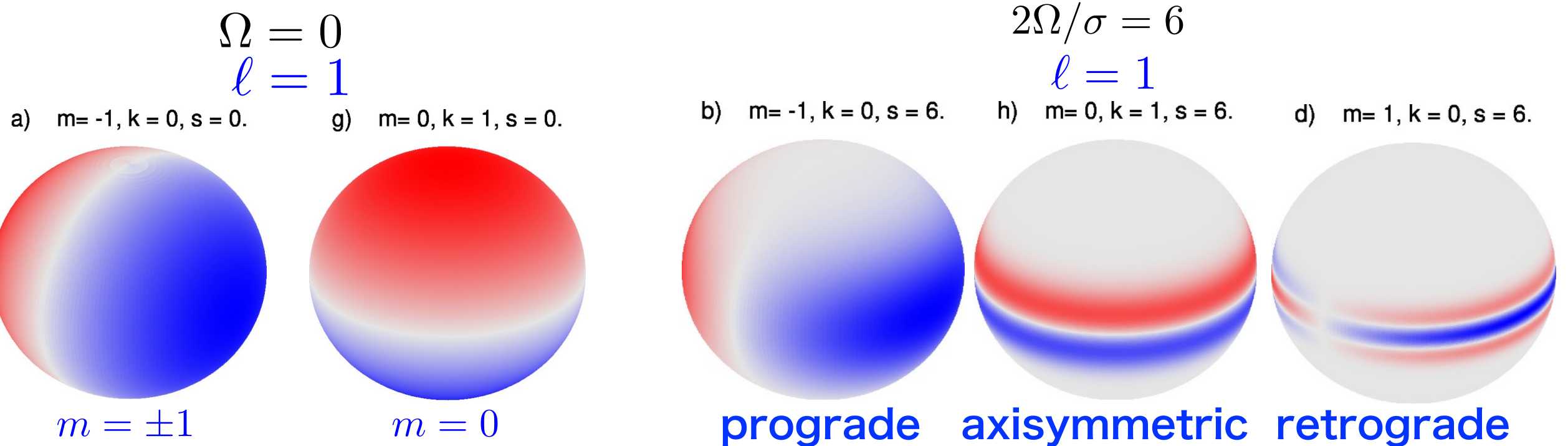
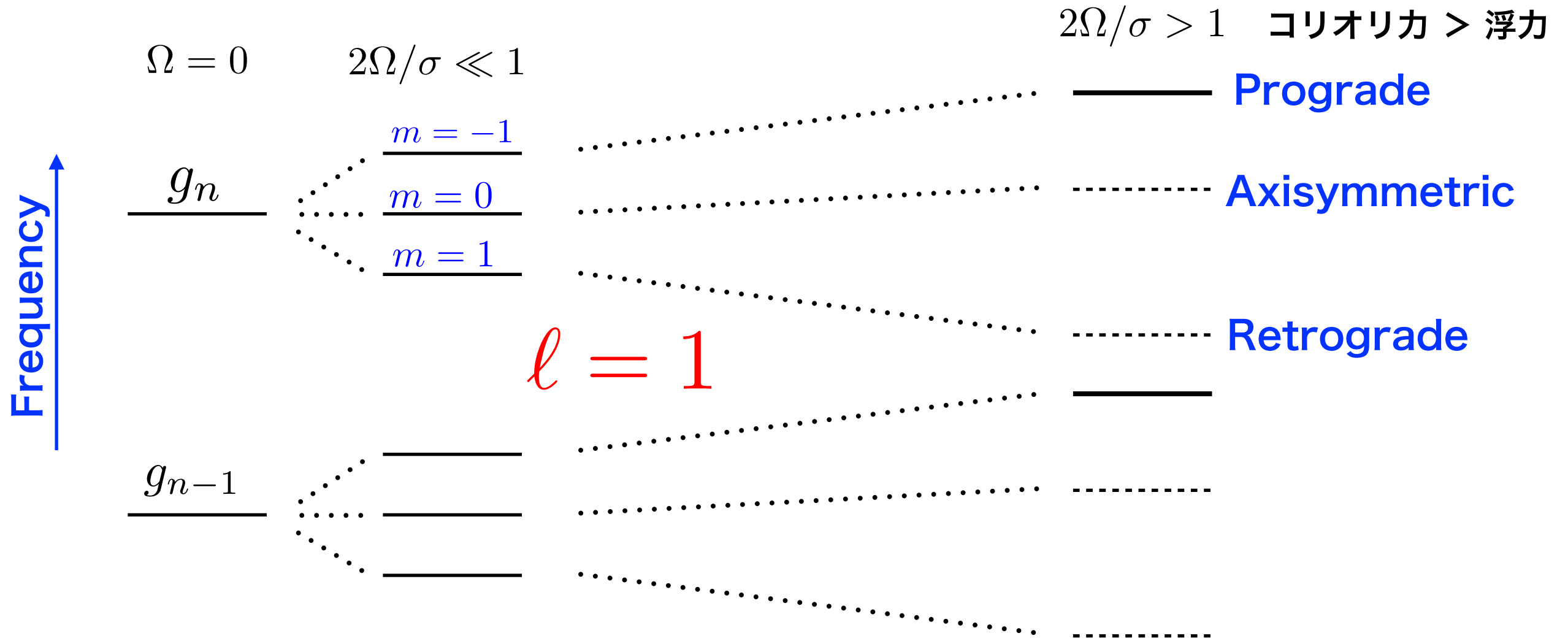


period-spacing of g modes





# Rotation effects on Nonradial pulsations



# Appearance of rotation effects

Slow rotation

Fast rotation

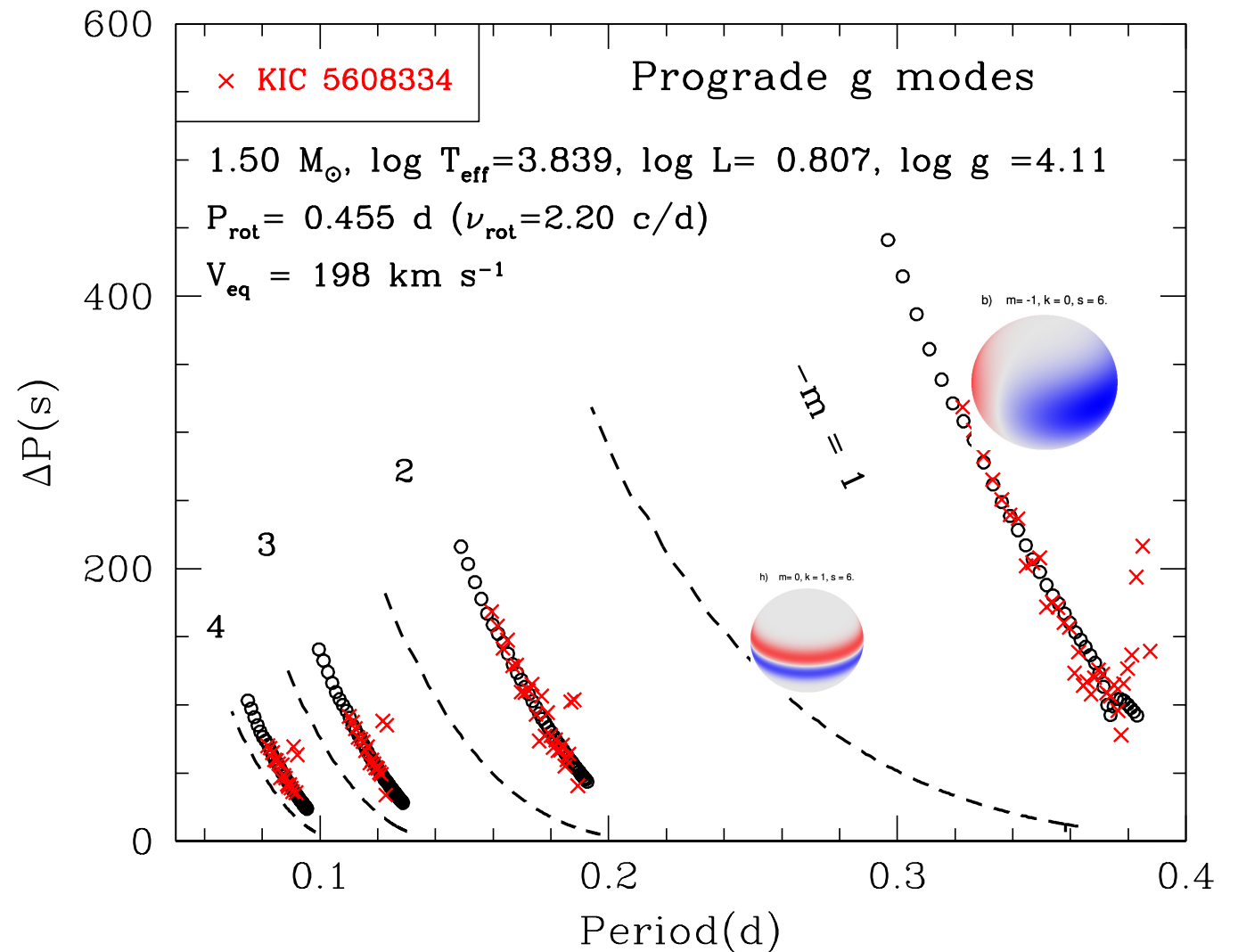
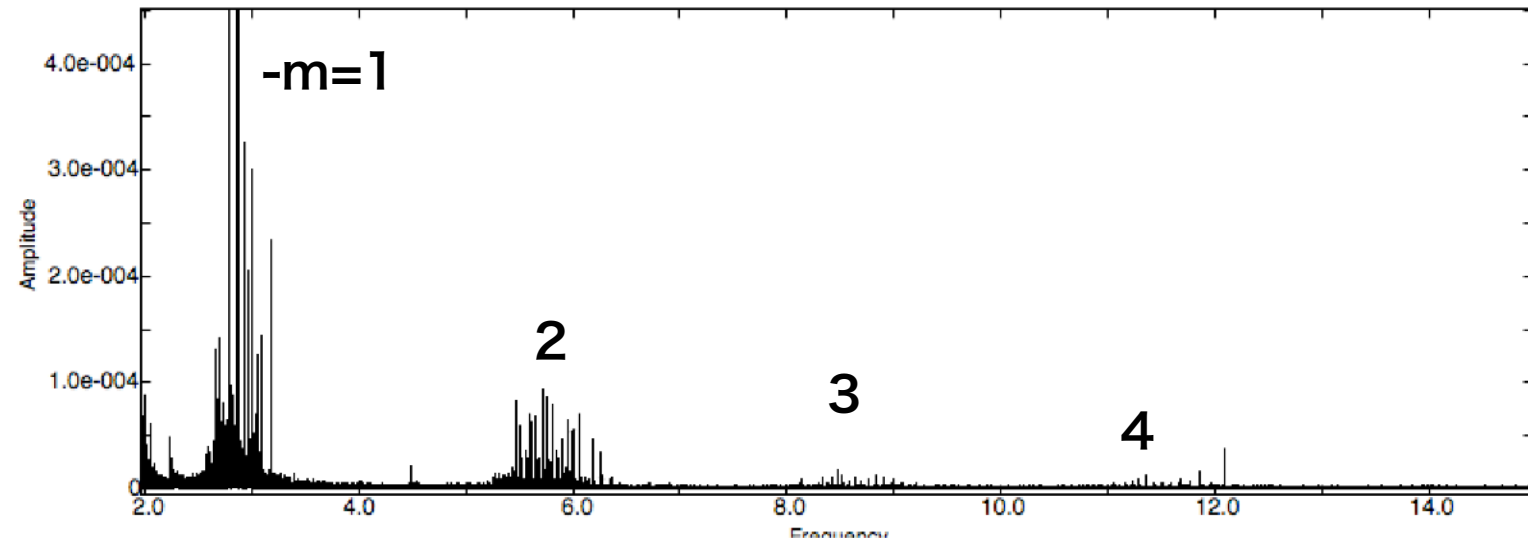
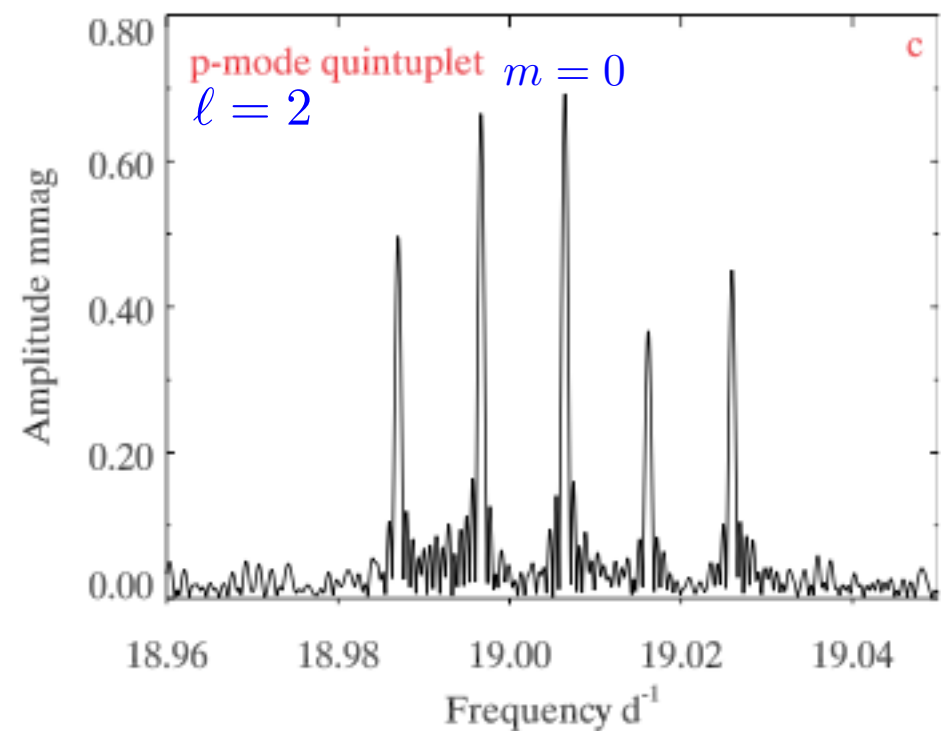
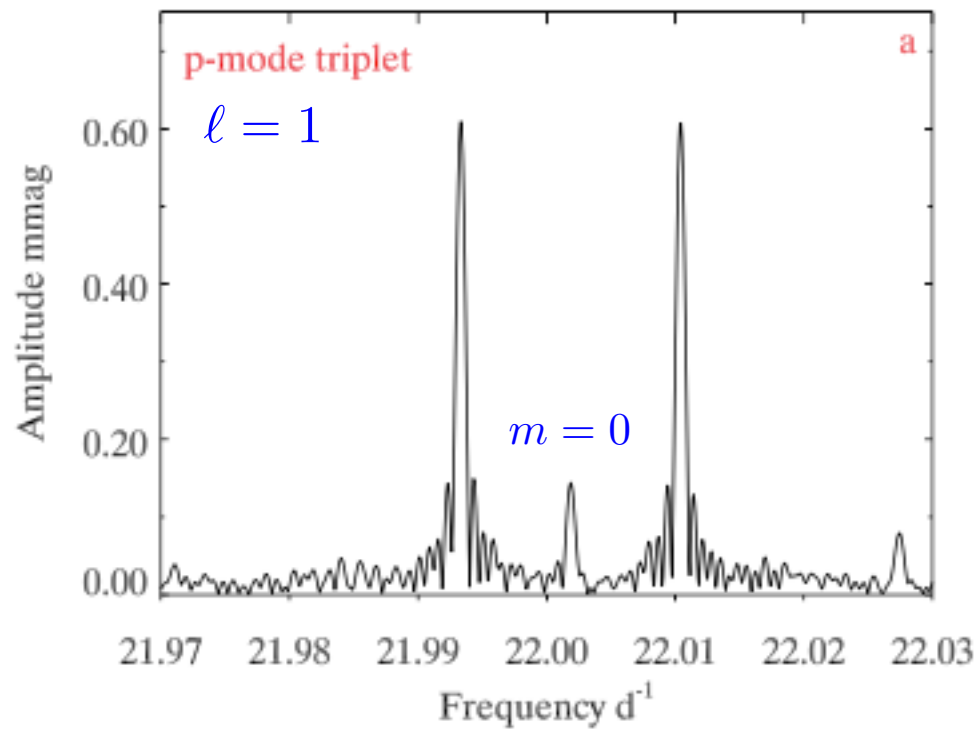
$$\frac{2\nu_{\text{rot}}}{\nu_{\text{nonrot}}} \ll 1 \quad \& \quad 2\pi\nu_{\text{rot}} \ll \sqrt{\frac{GM}{R^3}}$$

$$2\nu_{\text{rot}} > \nu_{\text{co-rot}}$$

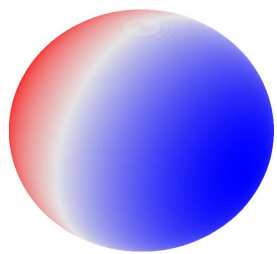
$$P_{\text{obs}} = (\nu_{\text{co-rot}} - m\nu_{\text{rot}})^{-1}$$

g modes

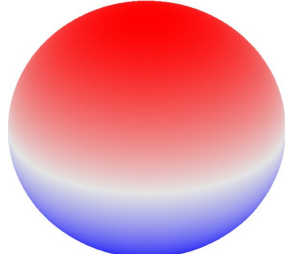
$$\nu_{\text{obs}} = \nu_{\text{non-rot}} - m(1 - C_{n,l})\nu_{\text{rot}}$$



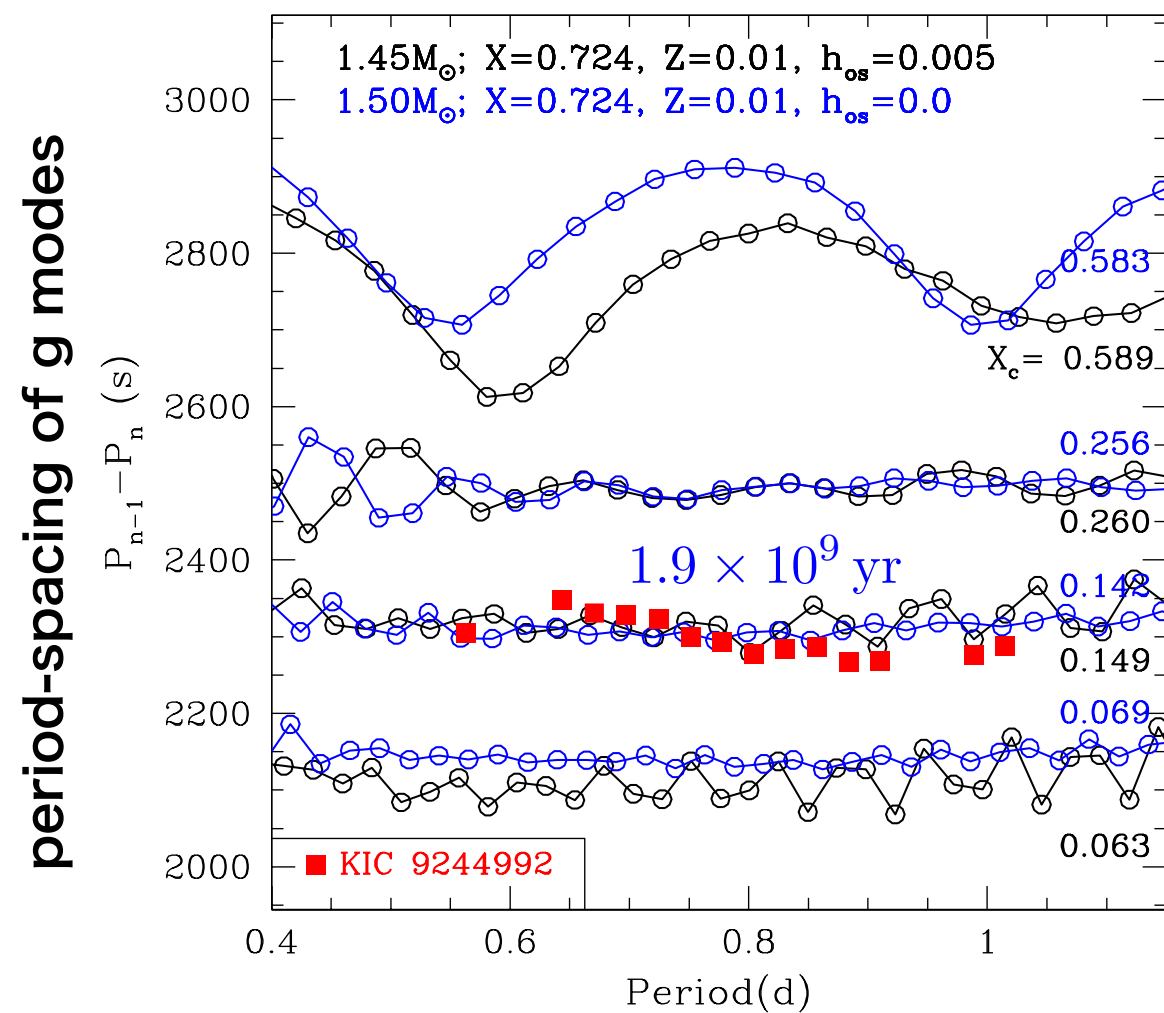
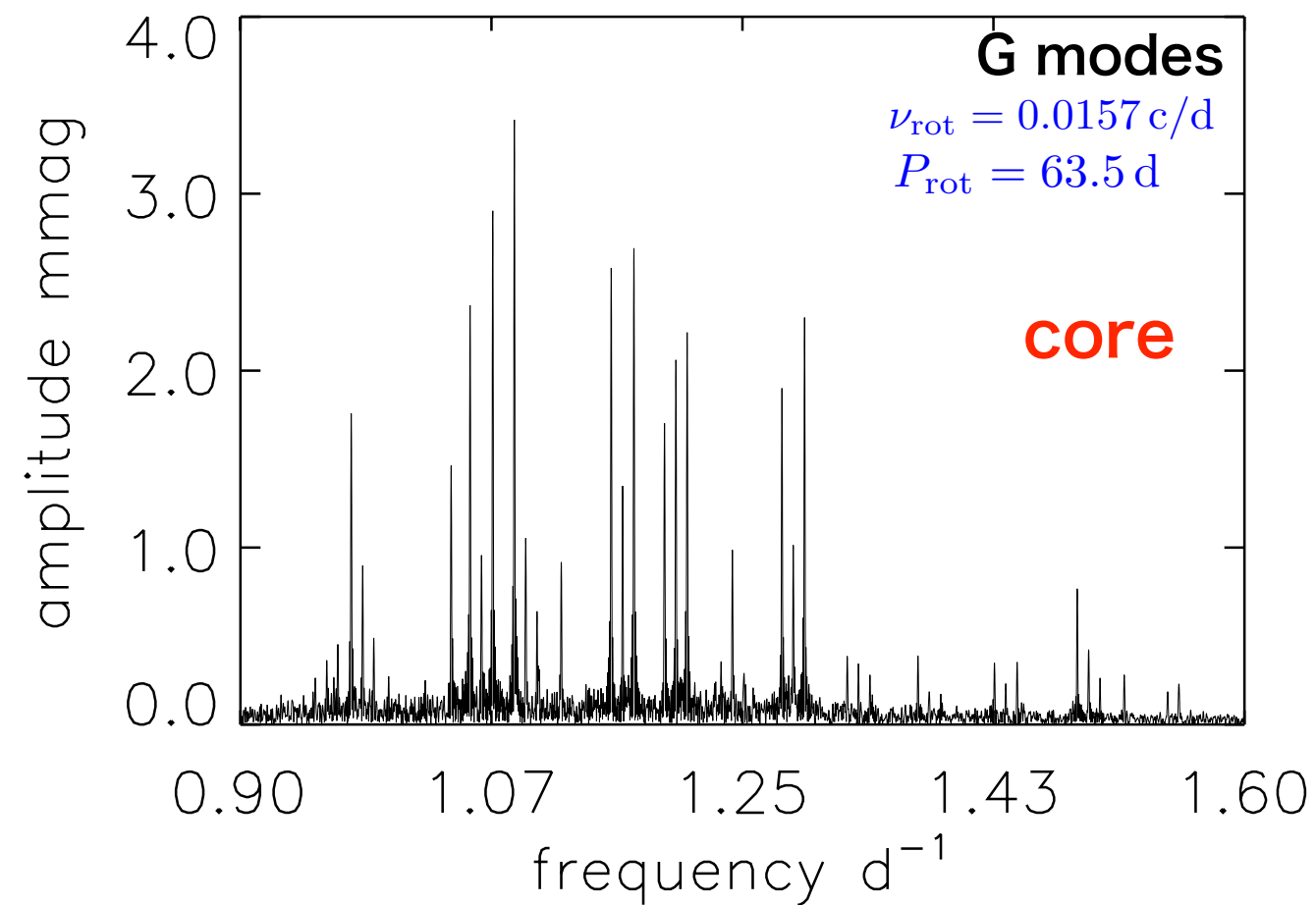
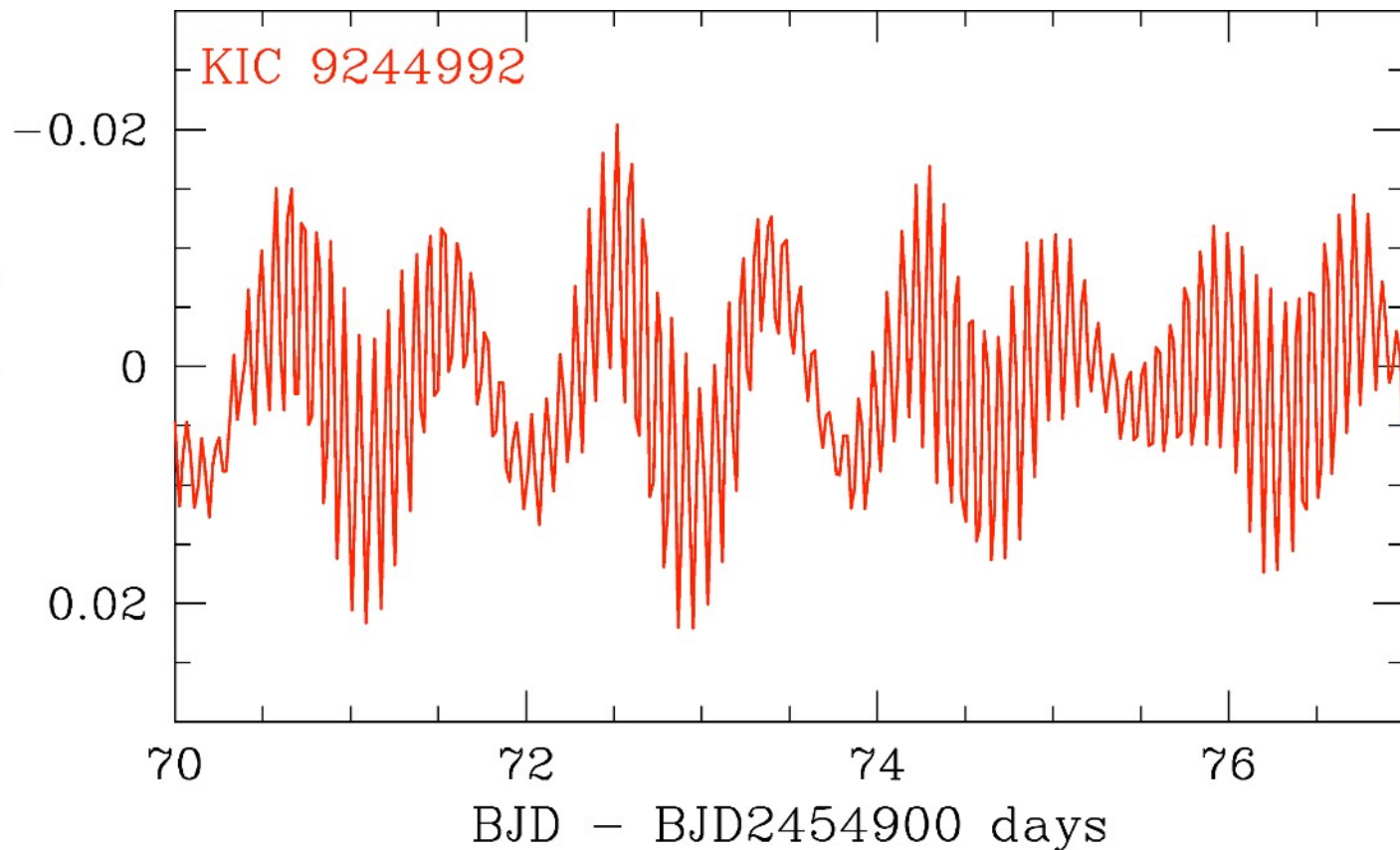
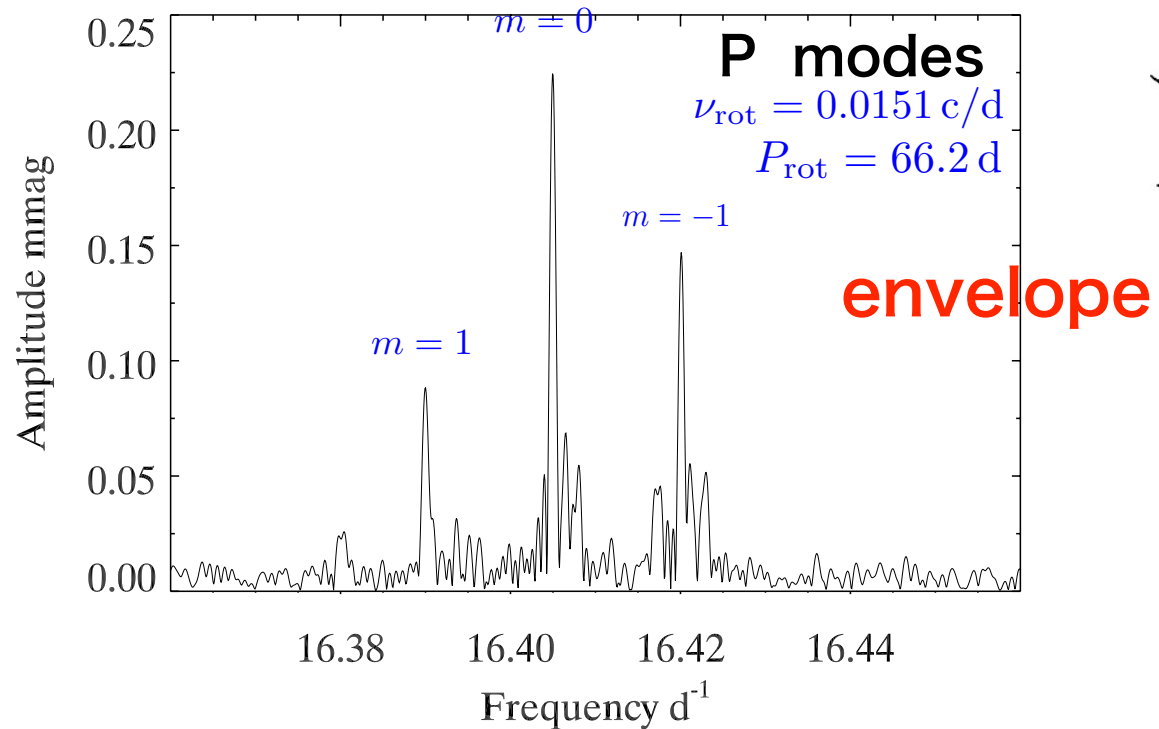




**KIC 9244992**



$$\nu_{\text{obs}} = \nu_{\text{non-rot}} - m(1 - C_{n,l})\nu_{\text{rot}}$$



# Rotation speeds in the core and the envelope

(g modes) (p modes)

Interior angular momentum of core hydrogen burning stars

3

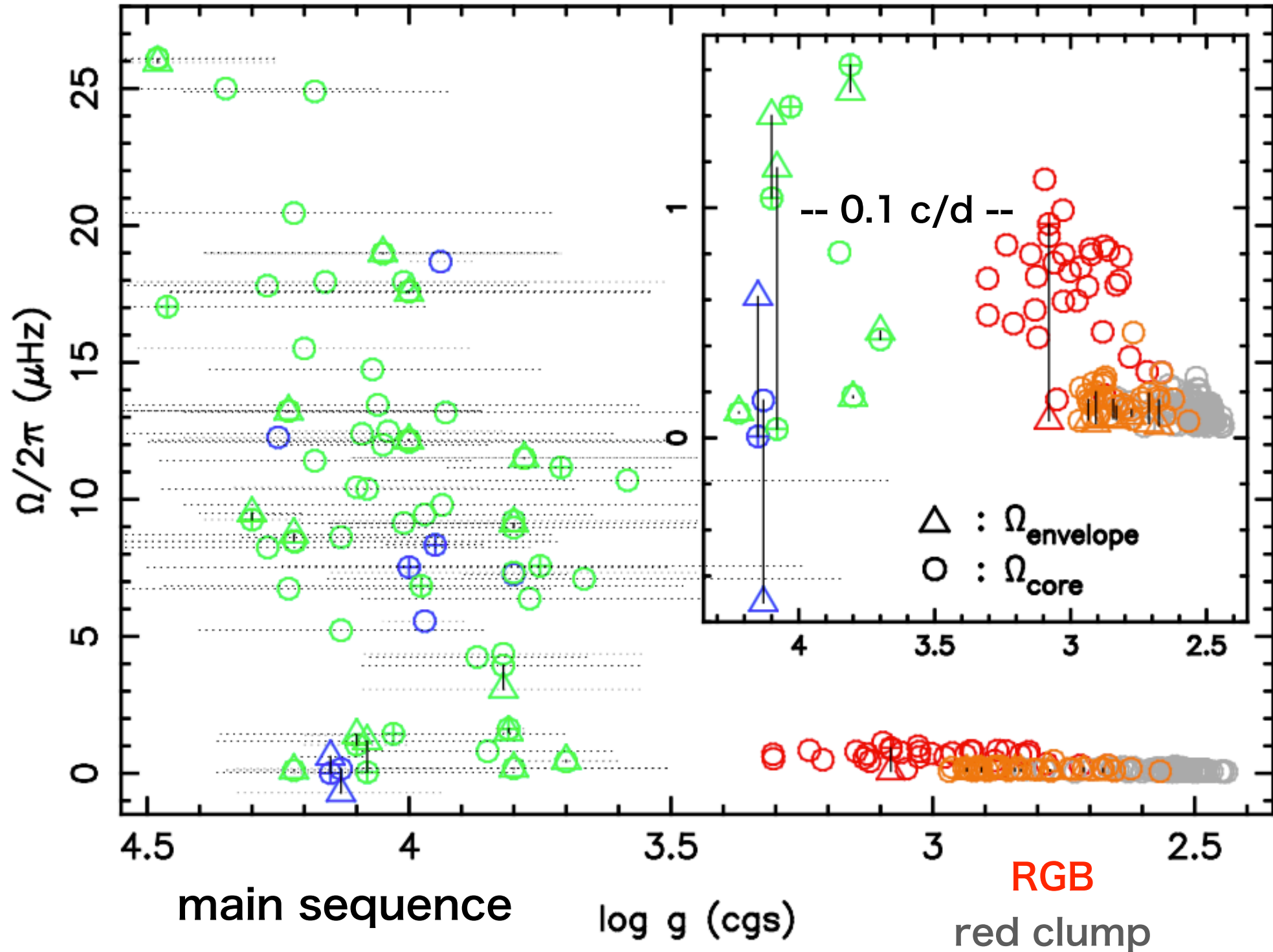
Rotation frequency

2 c/d

1 c/d

0.5 c/d

0.1 c/d

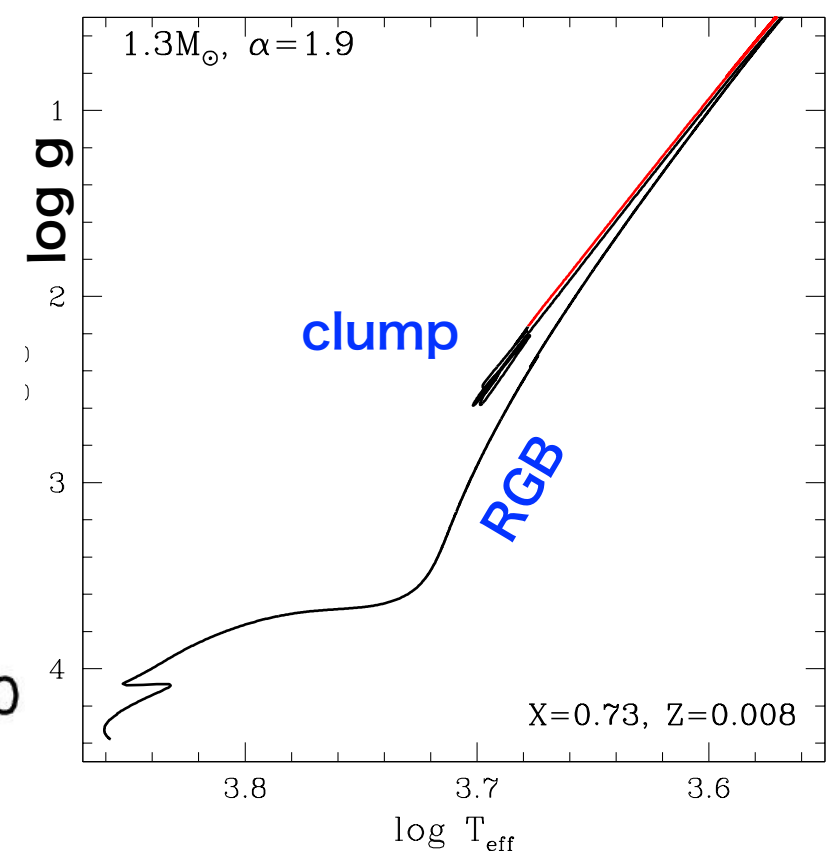
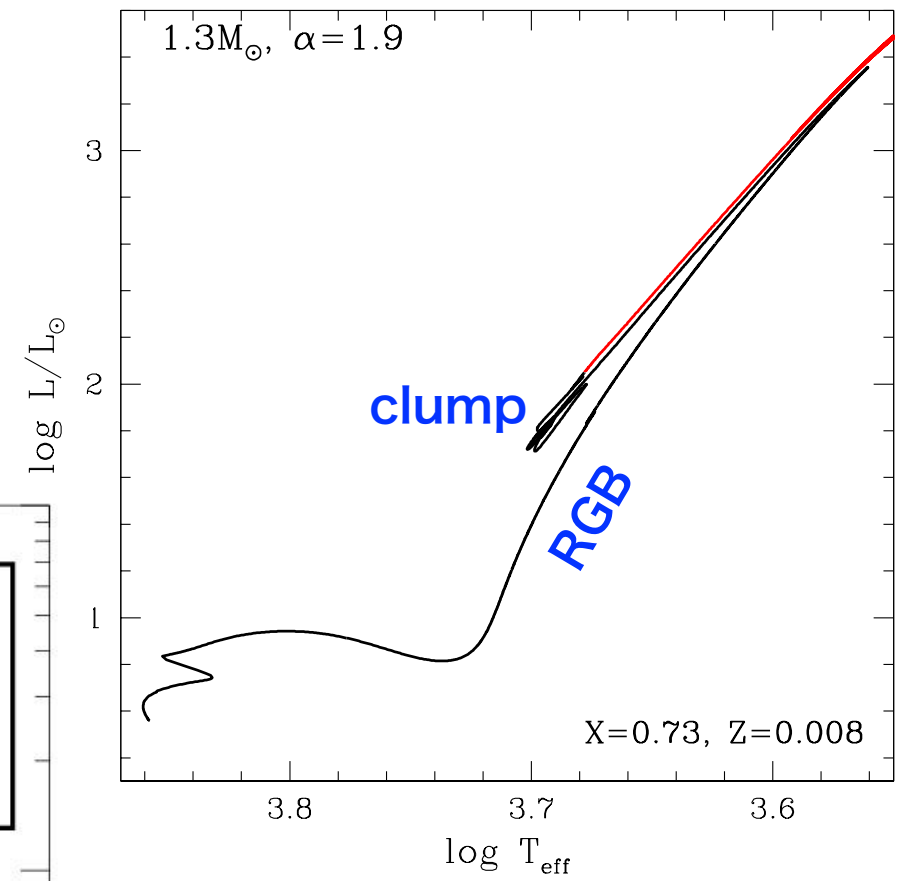
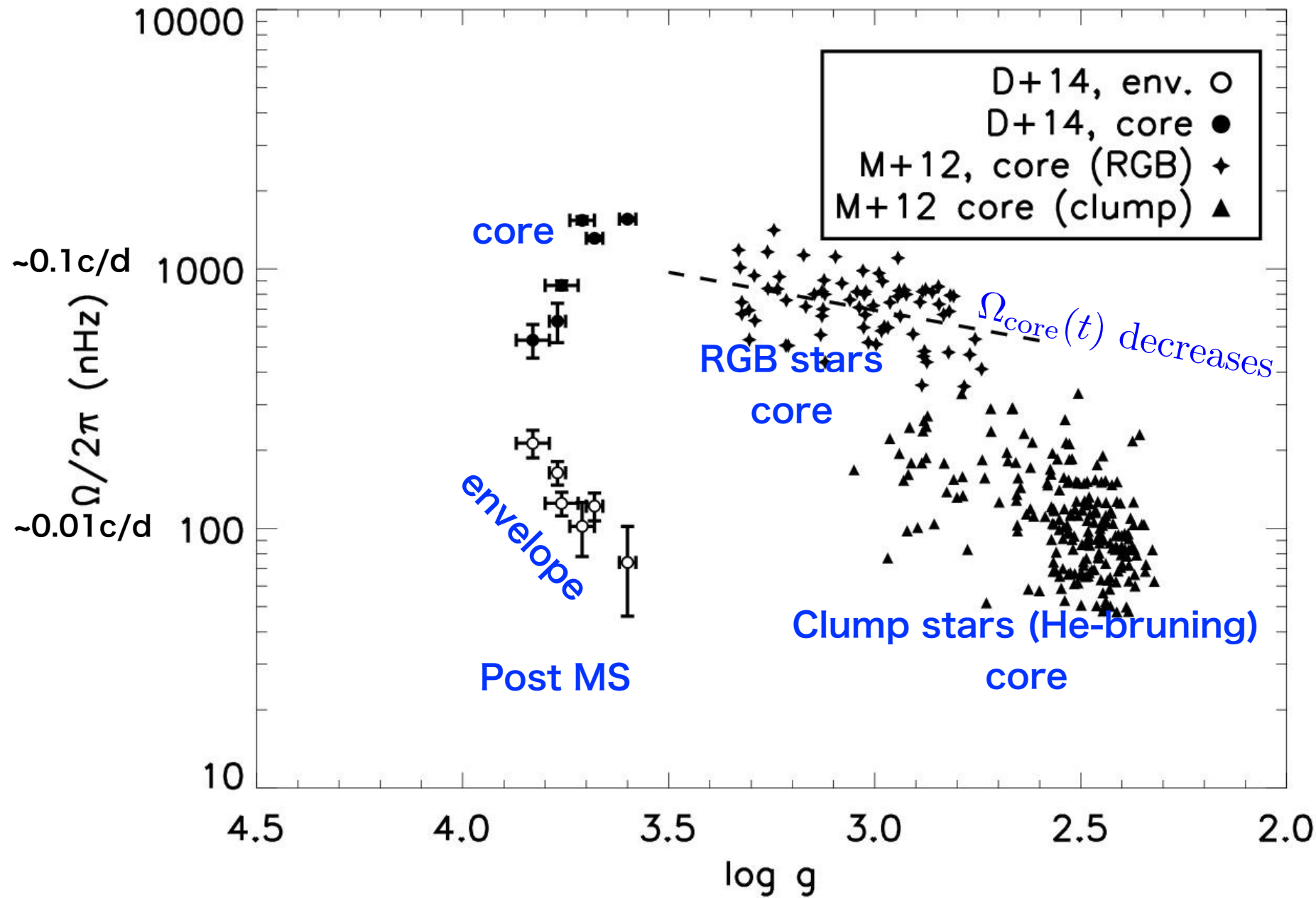


1.6 ~ 2.0  $M_{\odot}$  3 ~ 5  $M_{\odot}$

Aerts et al (2017)

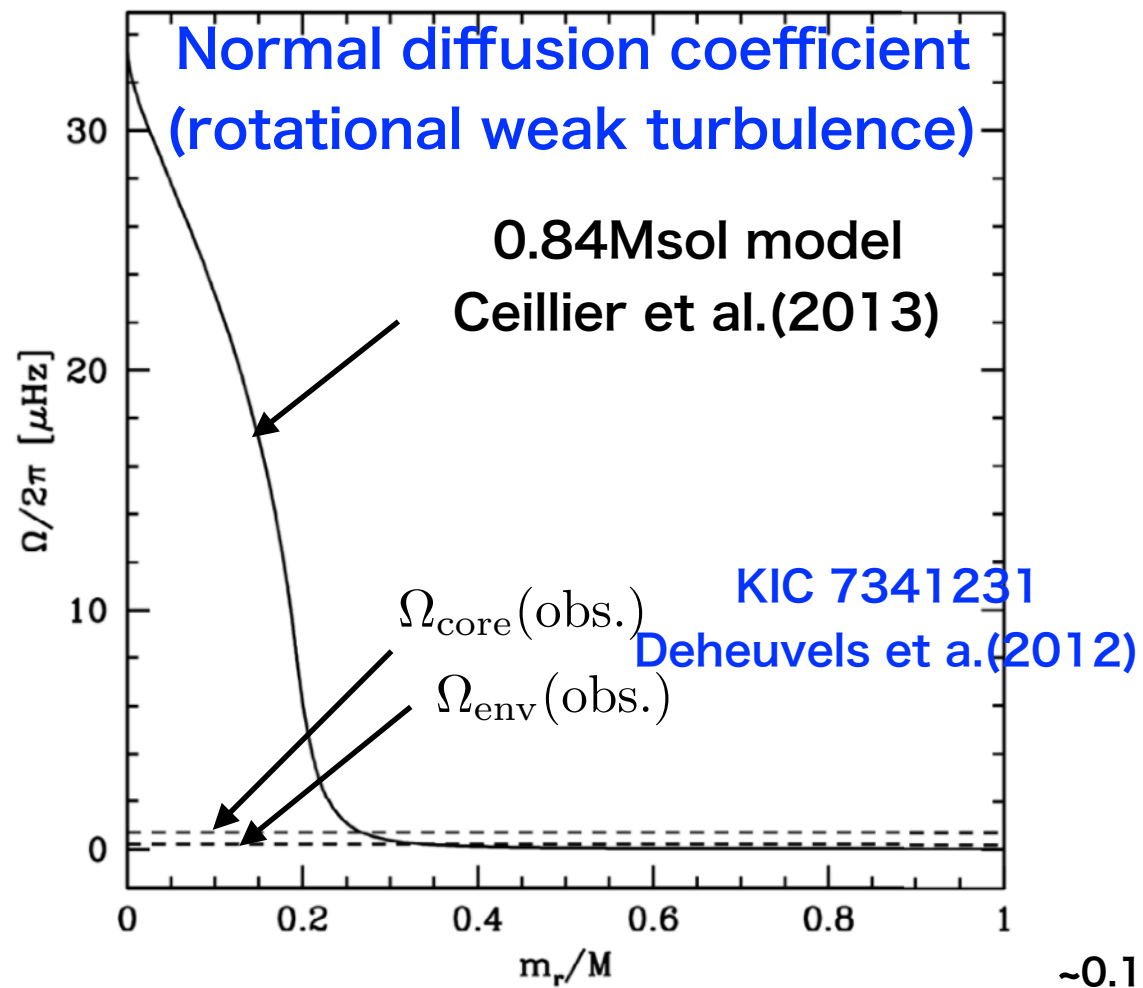


# sub-giant and RGB stars の自転速度の進化



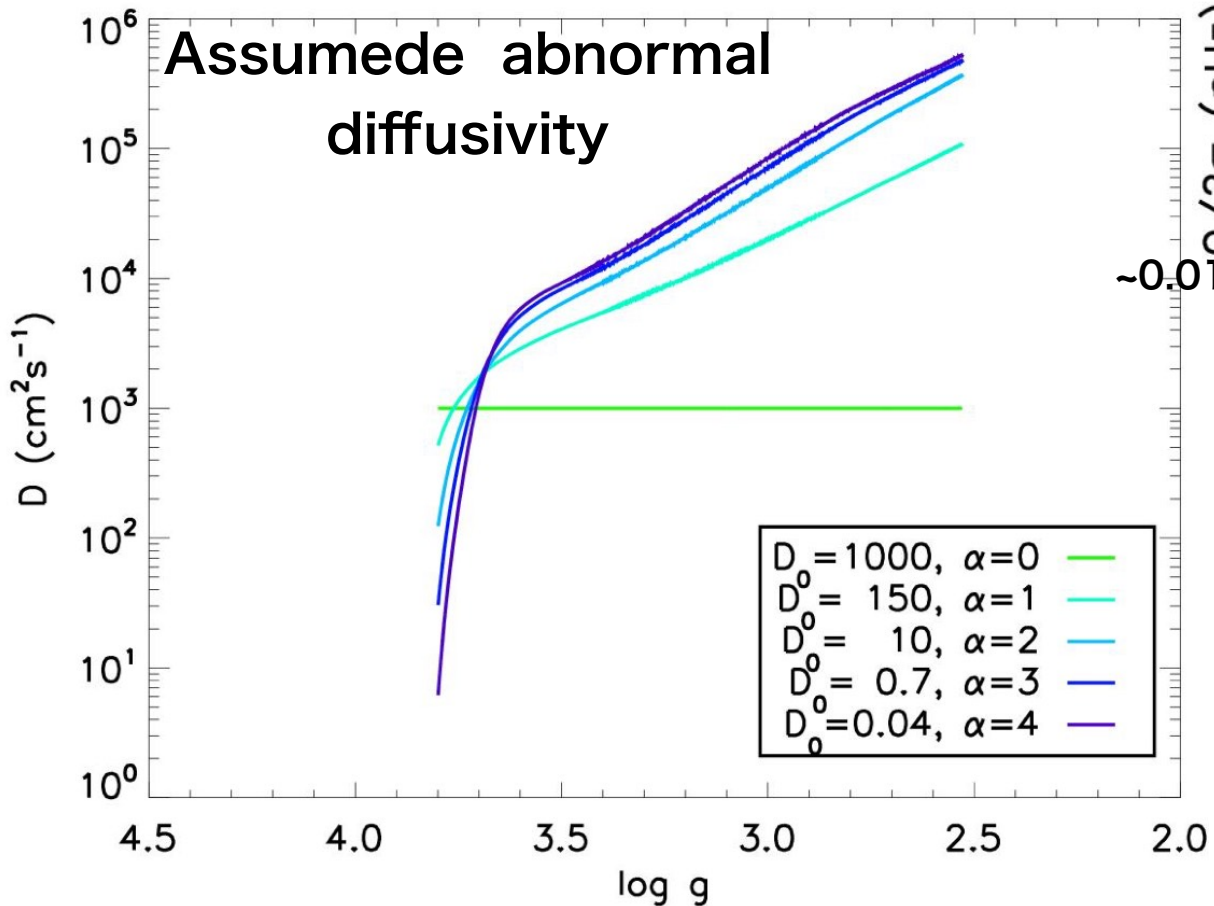
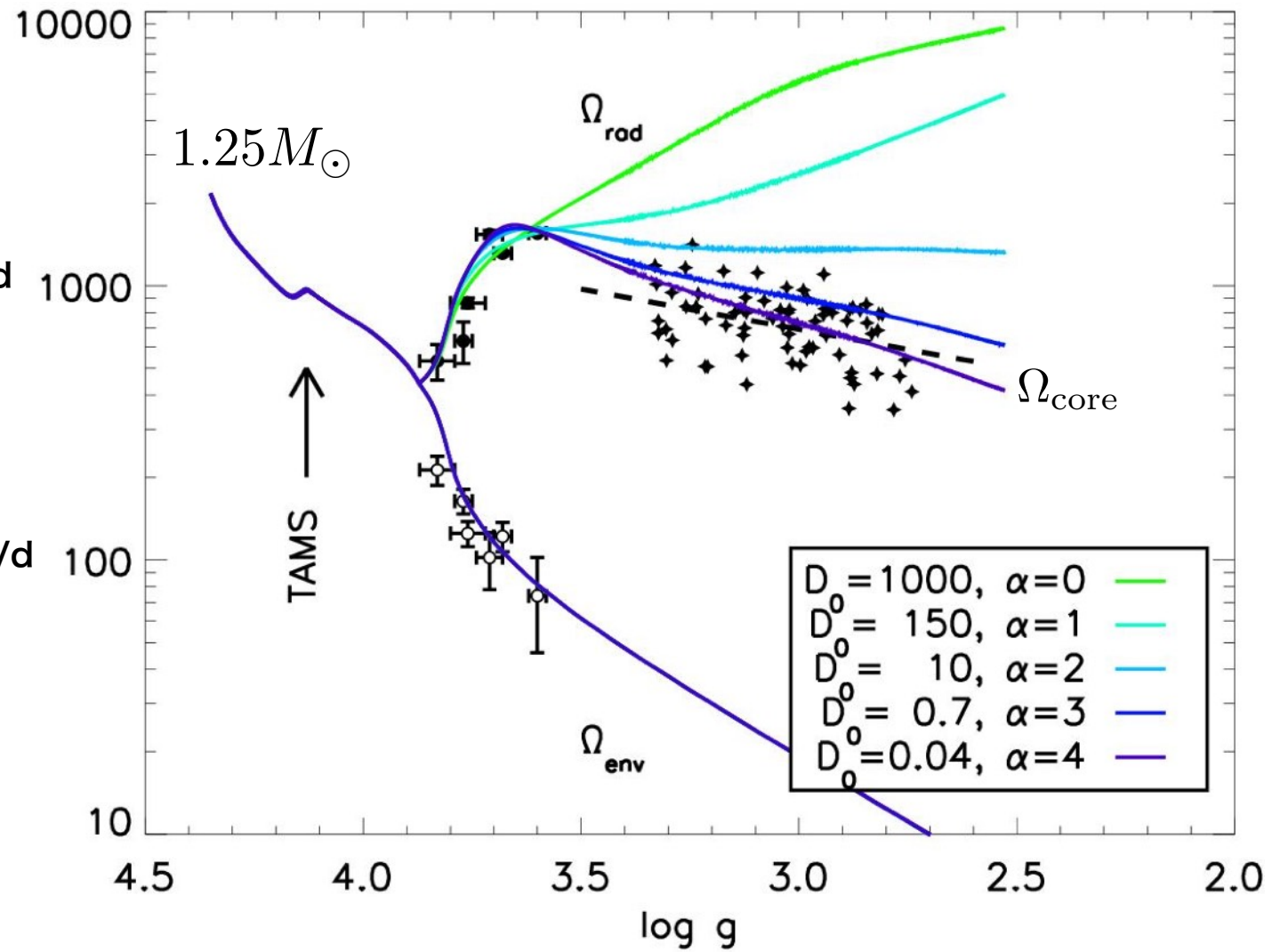
Spada et al. (2016)

# Evolution of the internal rotation frequency



$$\rho r^4 \frac{\partial \Omega}{\partial t} = \frac{\partial}{\partial r} \left[ \rho r^4 D \frac{\partial \Omega}{\partial r} \right]$$

$$D = D_0 \left( \frac{\Omega_{\text{core}}}{\Omega_{\text{env}}} \right)^\alpha$$



Spada et al. (2016)



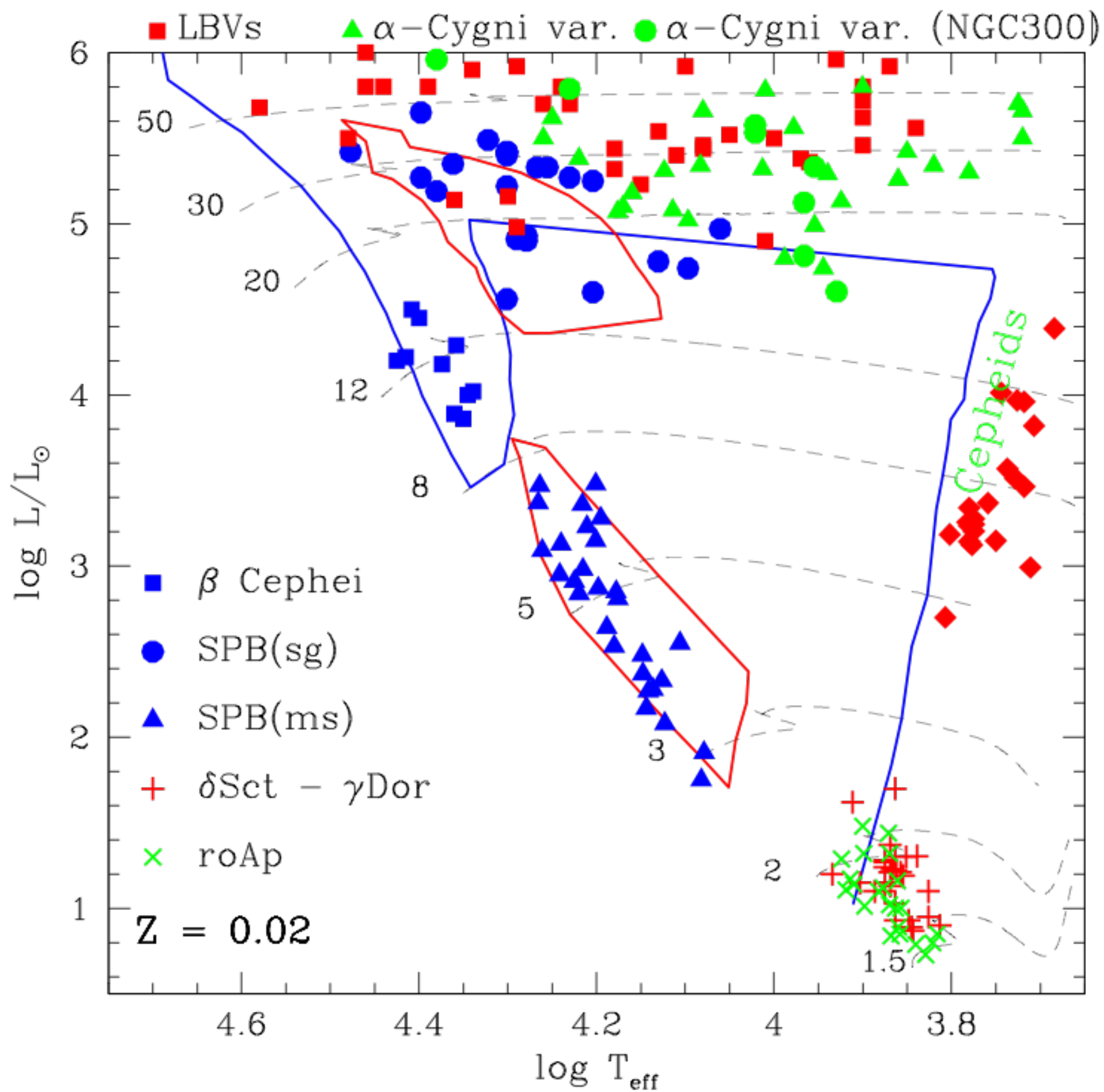
恒星の振動の観測 → 恒星進化段階、内部自転速度  
Red giants の Core/envelope differential rotation  
予想より格段に小さかった  
→ 恒星内部の angular momentum transport  
は通常考えられていたよりも格段に速い  
Diffusion coefficient should increase with time  
原因不明

---

Next :

脈動変光星のHR図上の分布 → 恒星内部の対流層  
赤色超巨星の質量放出

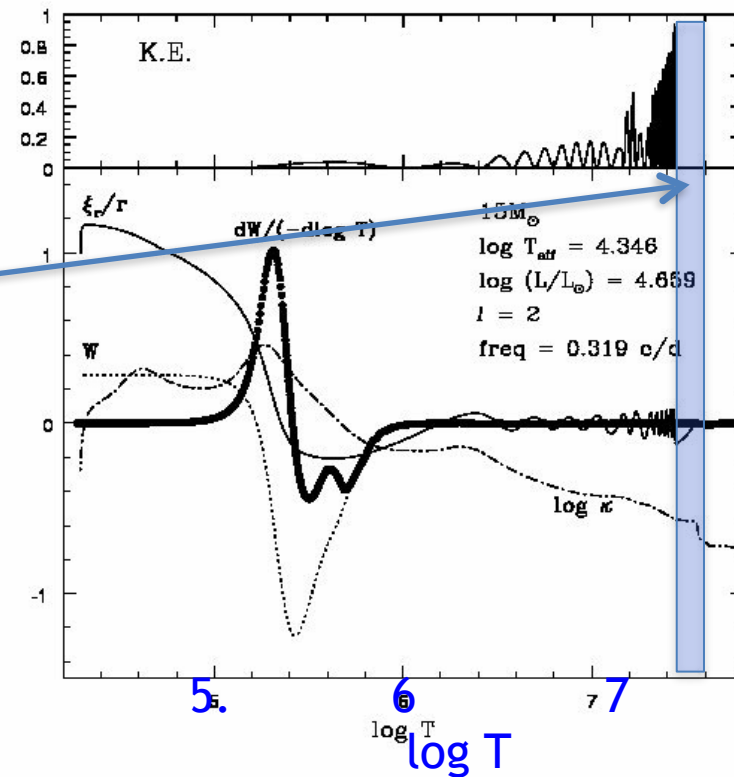
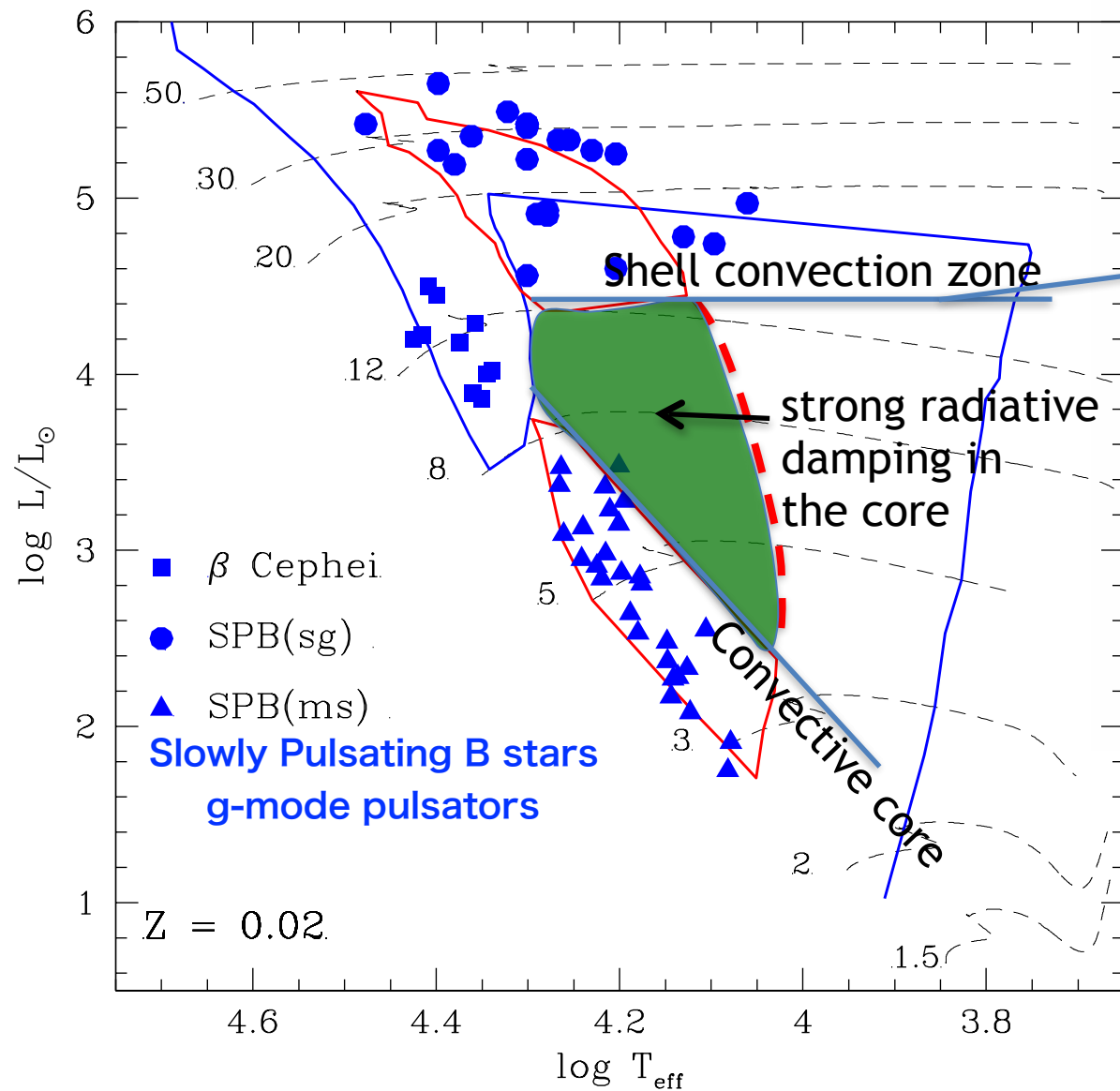
# B-A type pulsators and instability boundaries



# g-mode instability boundaries related with shell convection zone or convective core

**g-mode** は対流層に侵入できない

**M > 12 M<sub>sol</sub> : shell conv. zone occurs in post MS phase**



Shell convection zone reflect g-modes

---- no radiative damping in the core

Excitation

$\sim 2 \times 10^5 \text{ K}$

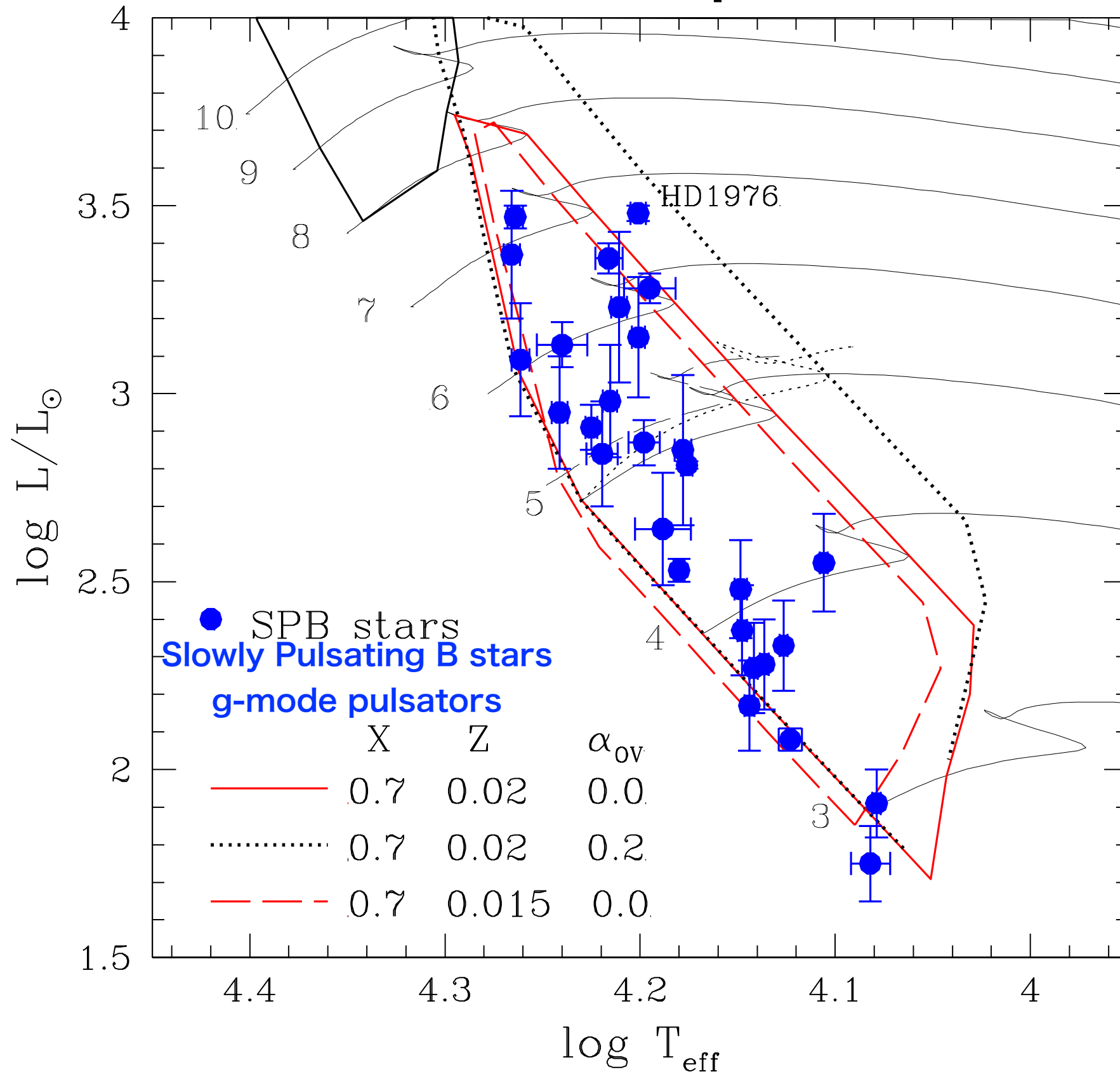
convection

strong dampint

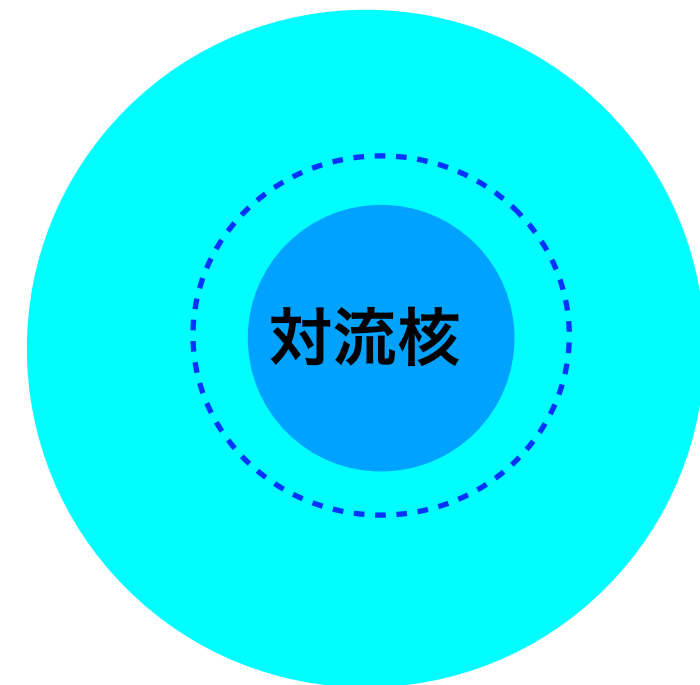
radiative core



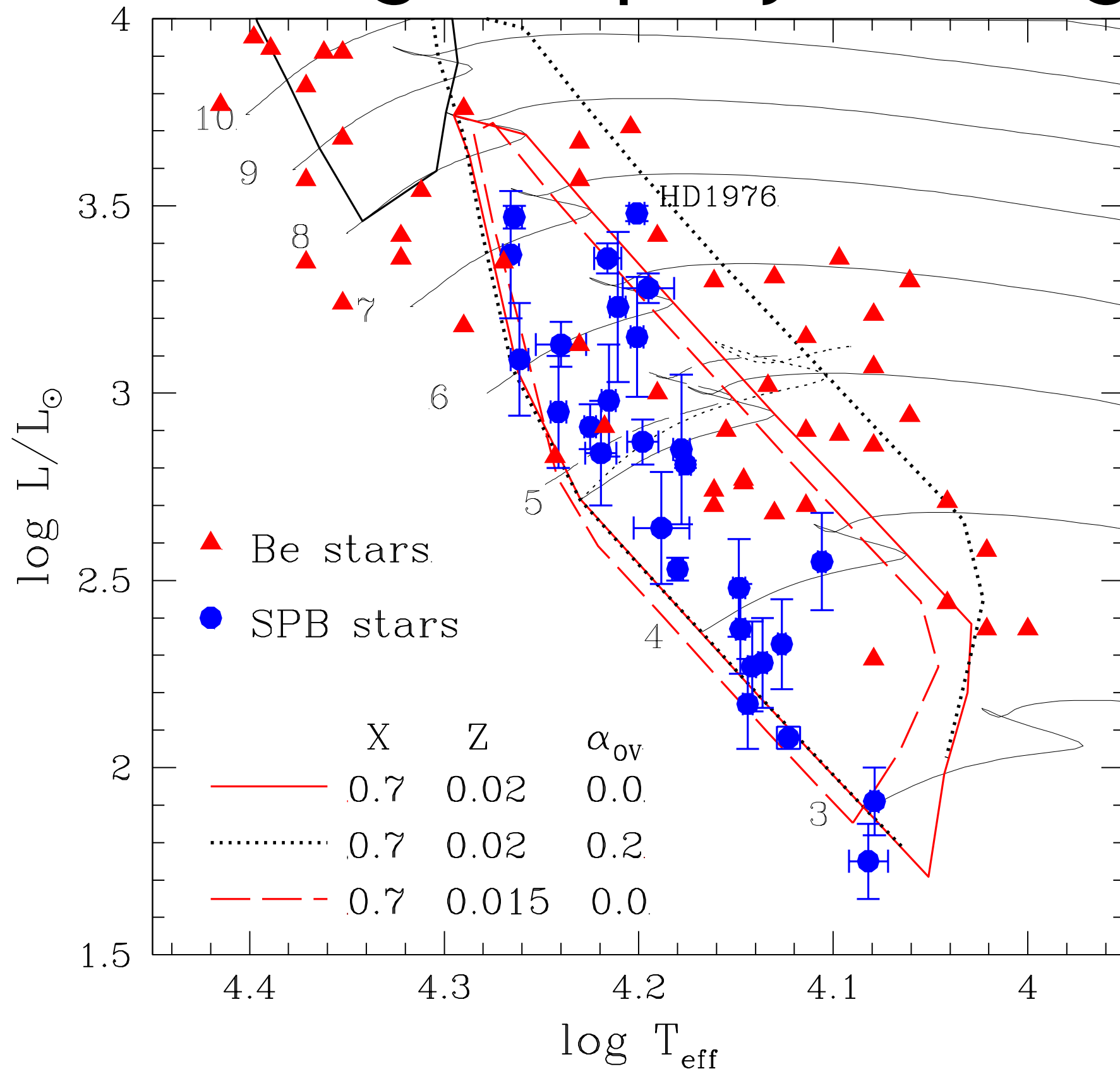
# Cool boundary of SPB instability indicate the end of main sequence with a conv. core



No core-overshooting is needed for SPB stars

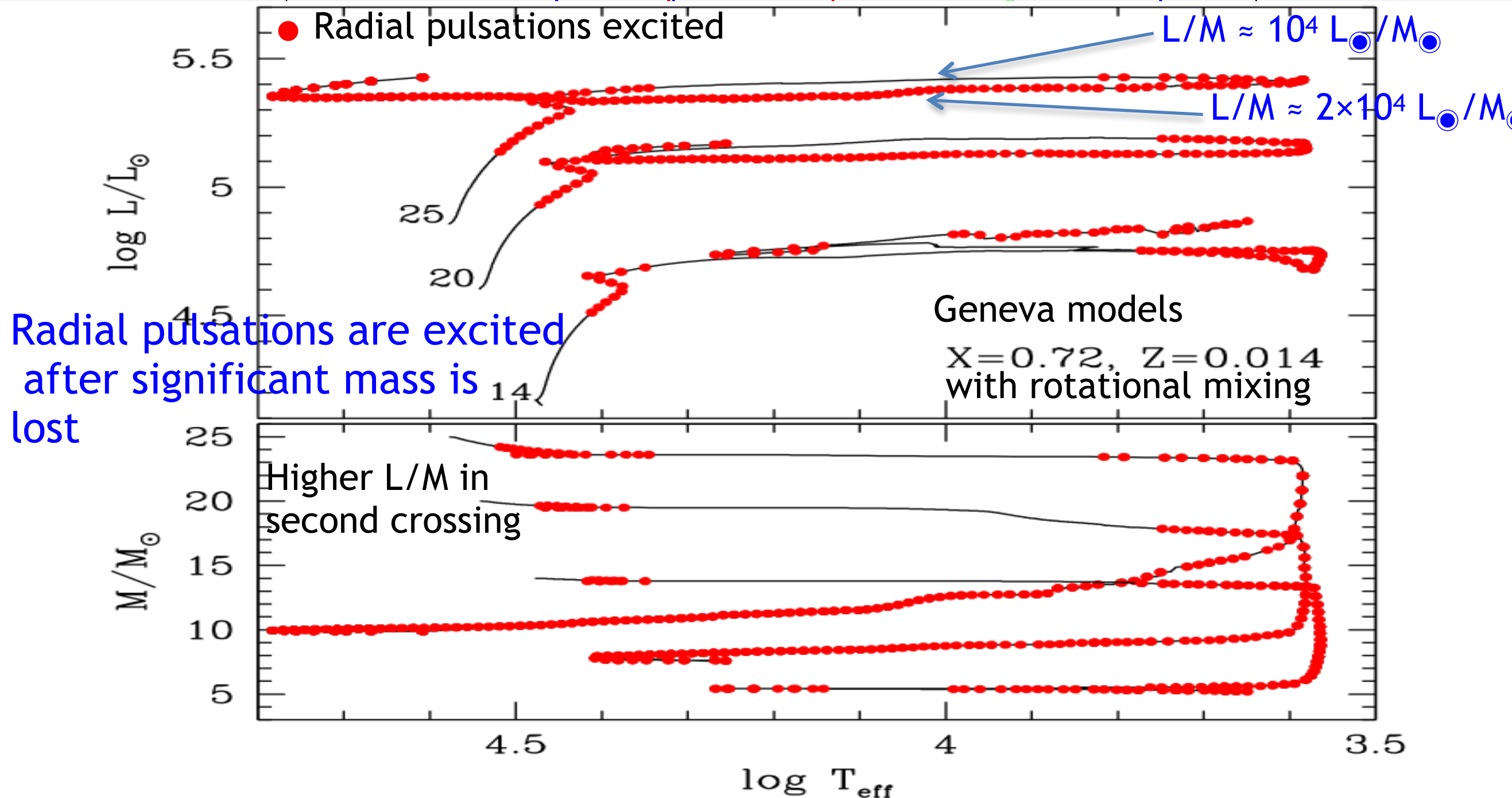
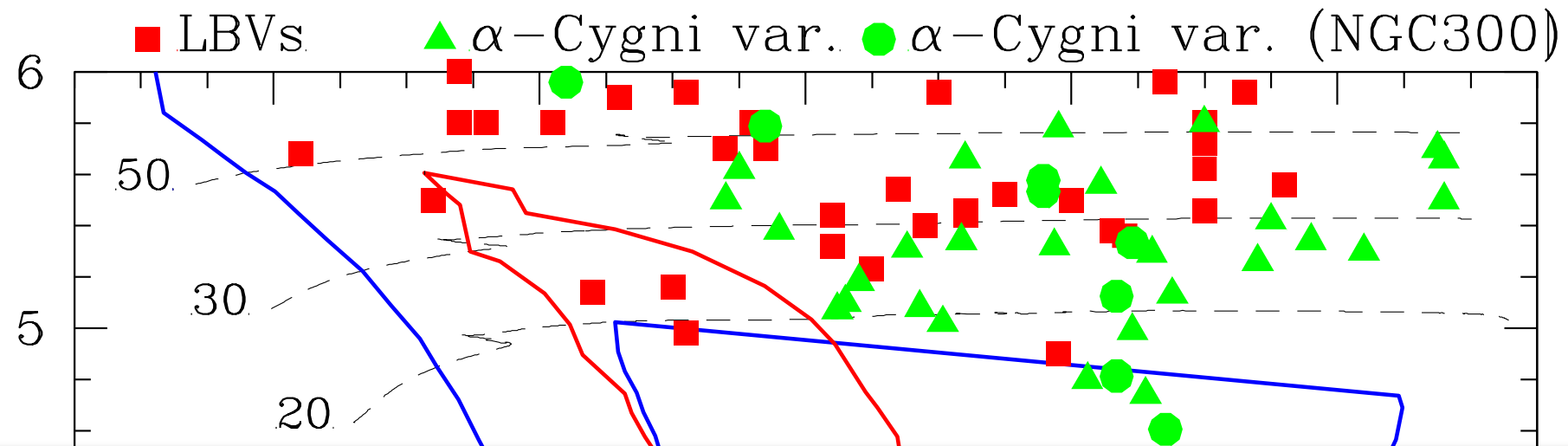


# Larger convective core or extensive mixing in rapidly rotating Be stars



Distribution of Be stars do indicate the presence of substantial overshooting or mixing around convective core

# $\alpha$ Cygni variables (radial pulsators)





大中質量脈動変光星分布 →

恒星内部の対流層、  
赤色超巨星からの質量放出

- Slow rotatorのconvective core overshooting は小さい
- Rapid rotator ではconvective core 周囲でのmixing
- $M > \sim 12 M_{\text{sol}}$  のpost MS stageでshell conv. zone 発生
- $M > \sim 20 M_{\text{sol}}$ : 赤色超巨星で質量放出後青色超巨星へ

---

Next:

恒星の脈動が示す恒星合体の証拠

1. Anomalous cepheids

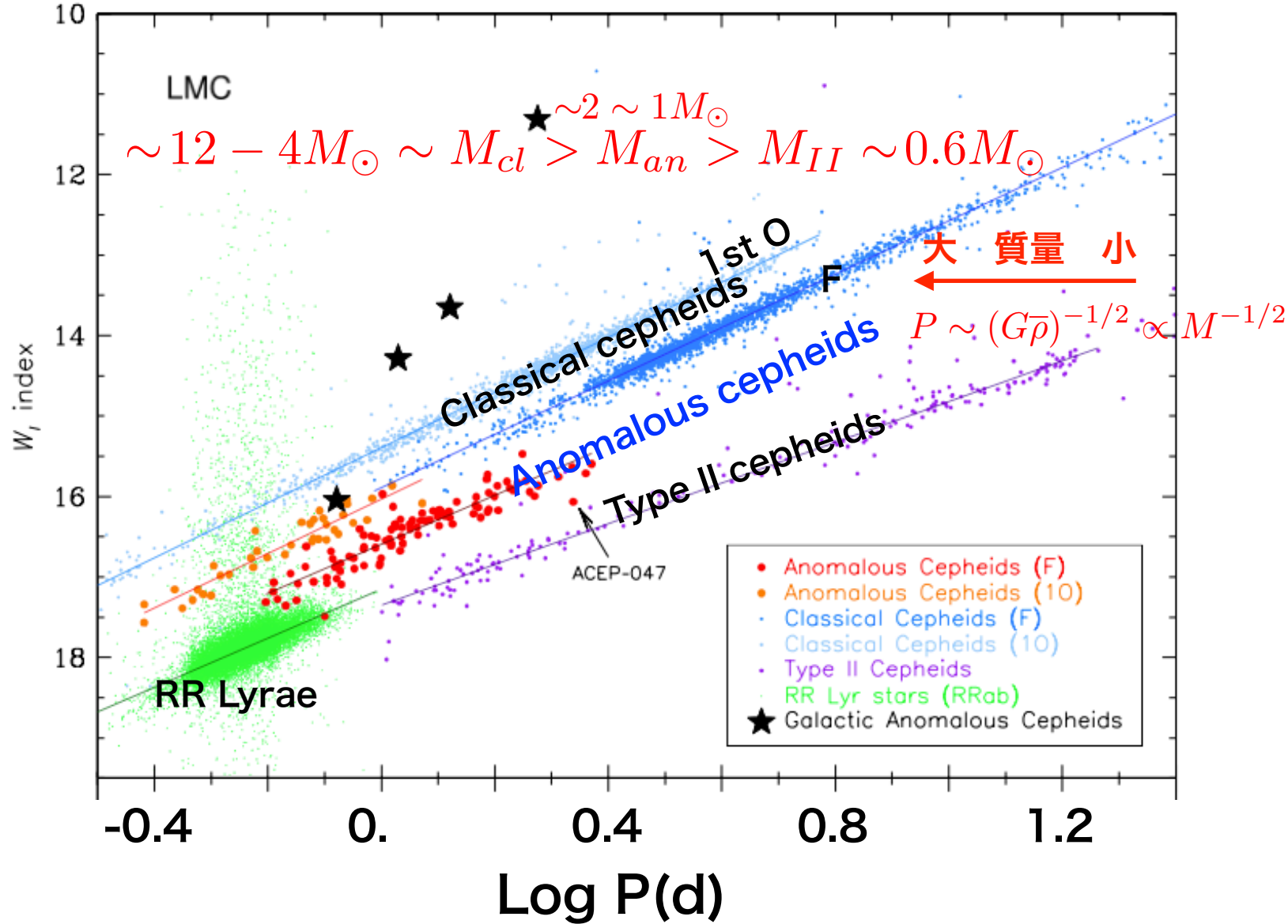
2つのred-giant core の合体？

2. He-star pulsators

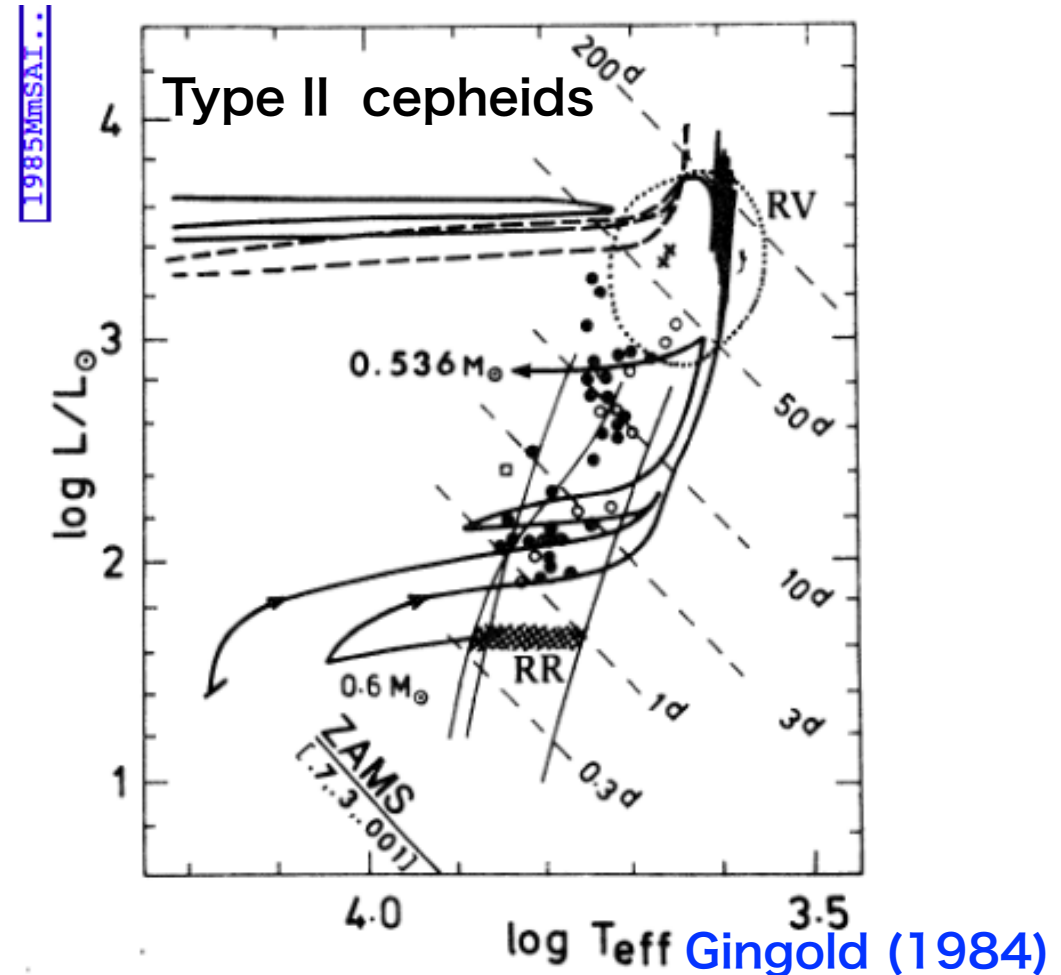
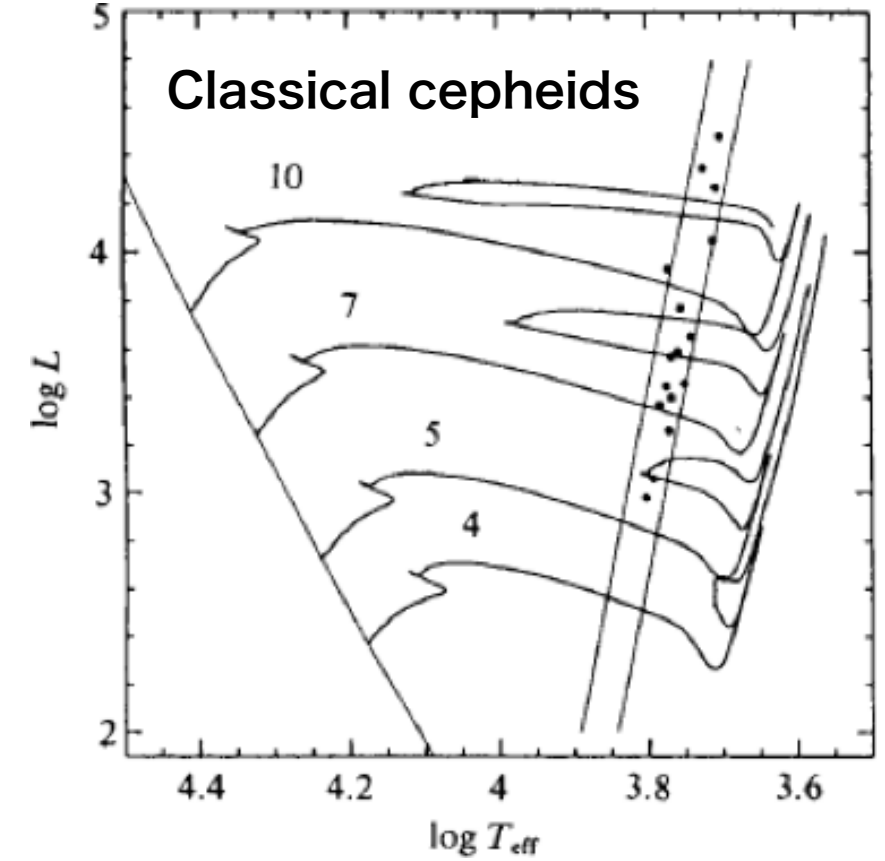
Double He-WD (low-mass WD) merger

# Classical, Anomalous, and Type II Cepheids

## Period-Luminosity relations

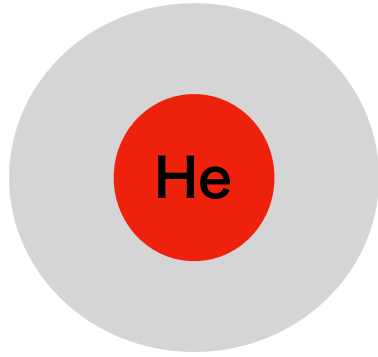


Soszynski et al(2015)  
(OGLE)

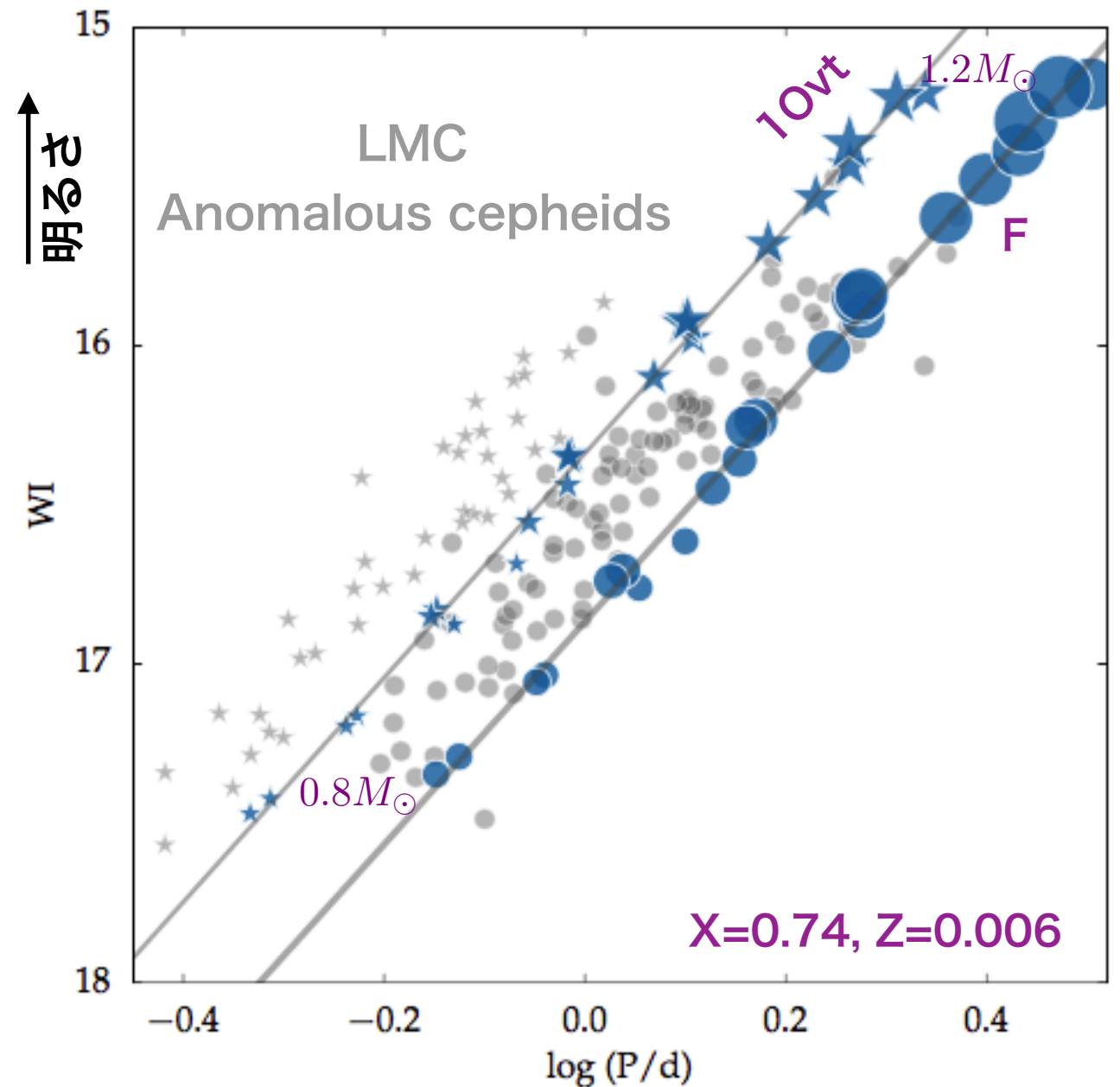
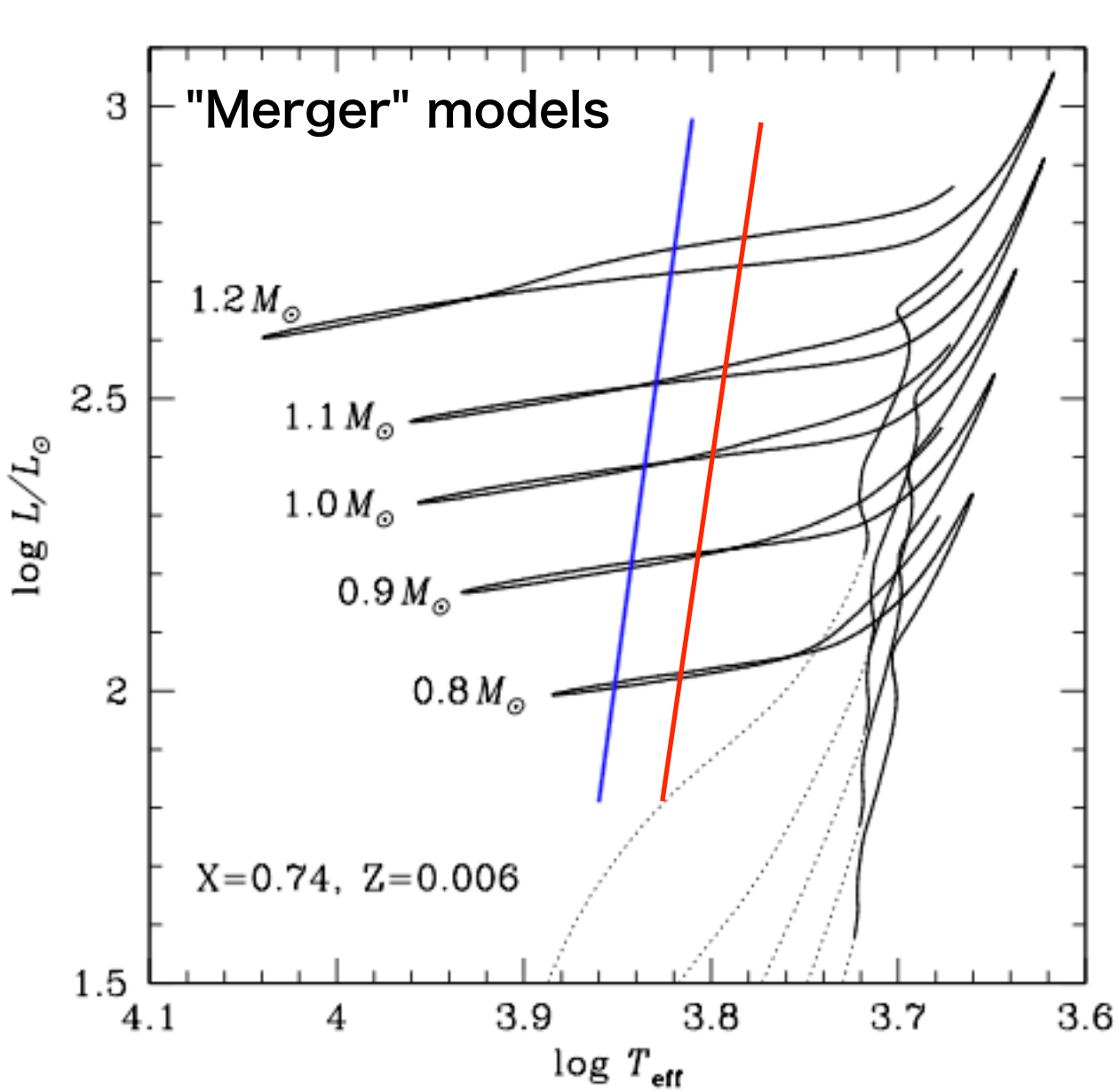
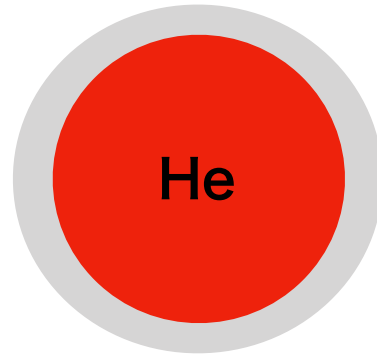


# Anomalous cepeheids は Red-giants He-core merger の産物？

Normal model

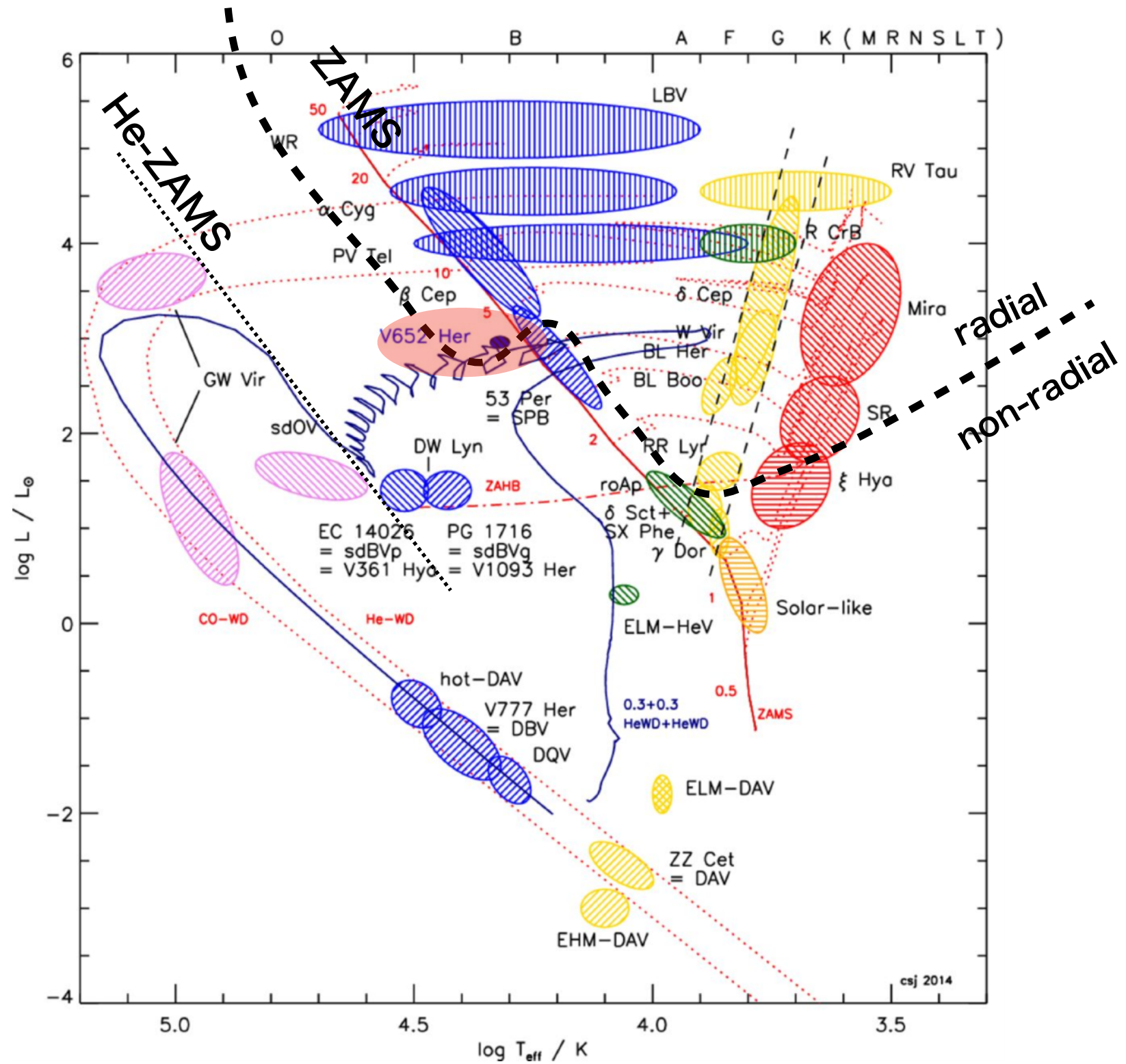


"Merged" model





# Pulsational variables in the HRD



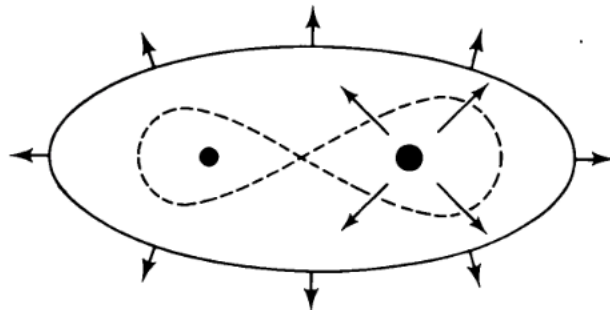
Jeffery et al. (2015)

# Merger of double He WDs

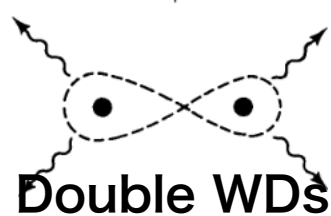
Spherical model: Helium accretion onto a white dwarf

Initial system:  $M_1 \sim M_2 \sim 3 \sim 5 M_\odot$

Second  
Common  
Envelope  
Stage



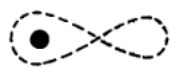
Initial System  
Gravitational  
Wave Radiation



Double WDs

$M_1 \sim M_2 \sim 0.4 \sim 0.5 M_\odot$

Start of  
Heavy Disk  
Formation



Heavy Disk  
Phase



Slow Accretion

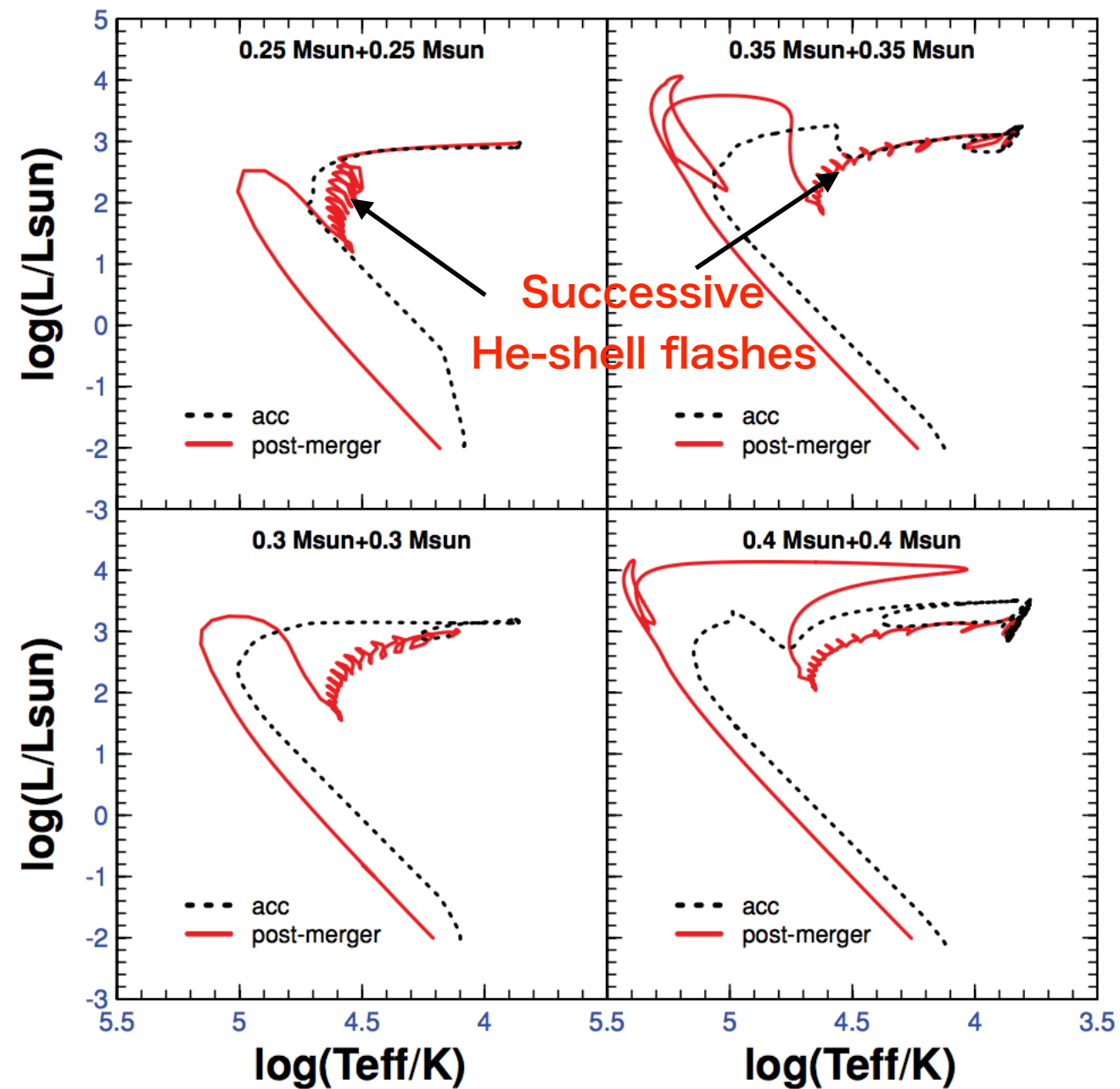
Fast Accretion

Final  
Outcome



Iben & Tutukov (1984)

Slow merger:  $\dot{M} = 10^{-5} M_\odot/\text{year}$



Zhang & Jeffery (2012)

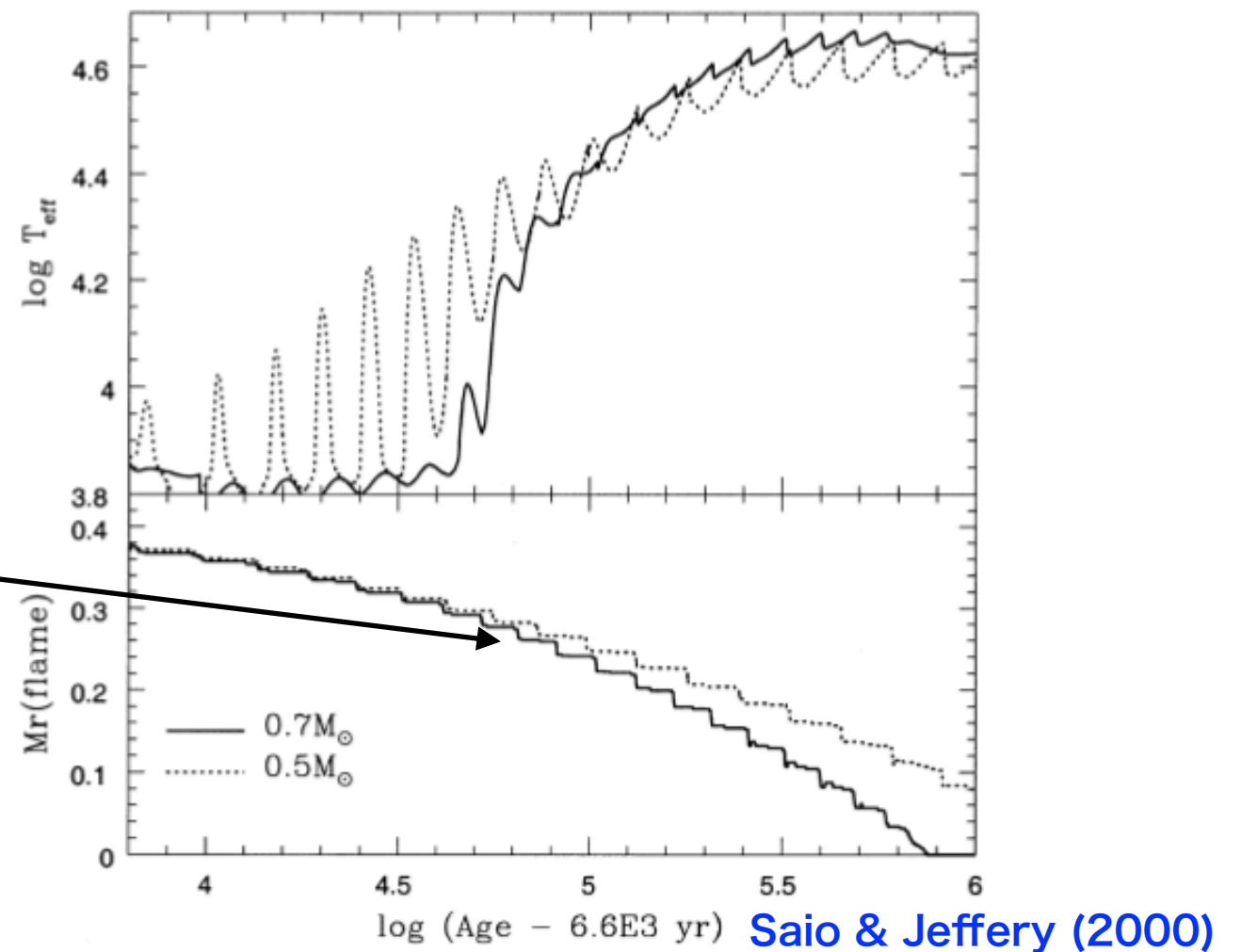
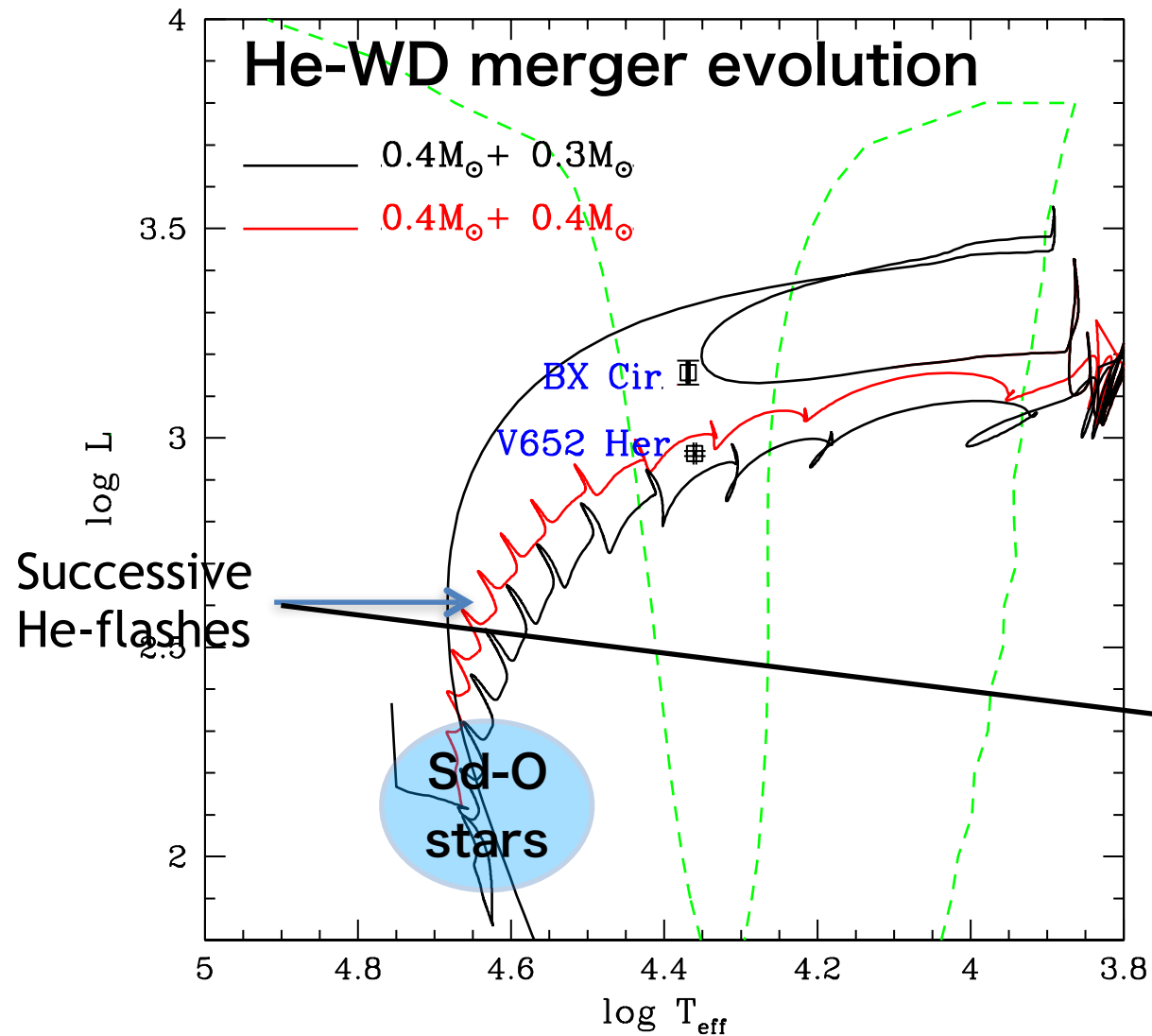
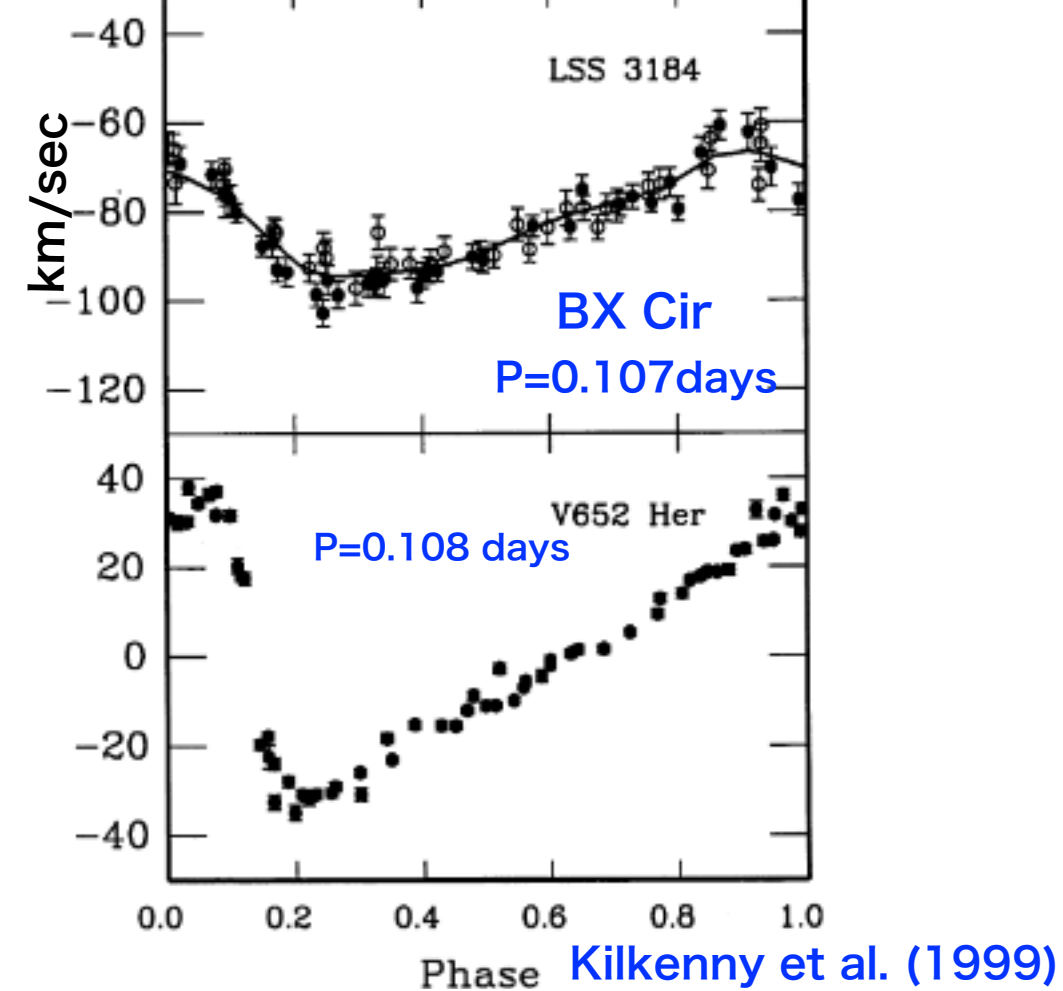
# Double He-WD merger models

## -- He-star pulsators

$$\dot{M}_{\text{acc}} = 1 \times 10^{-5} M_{\odot}/\text{yr}$$

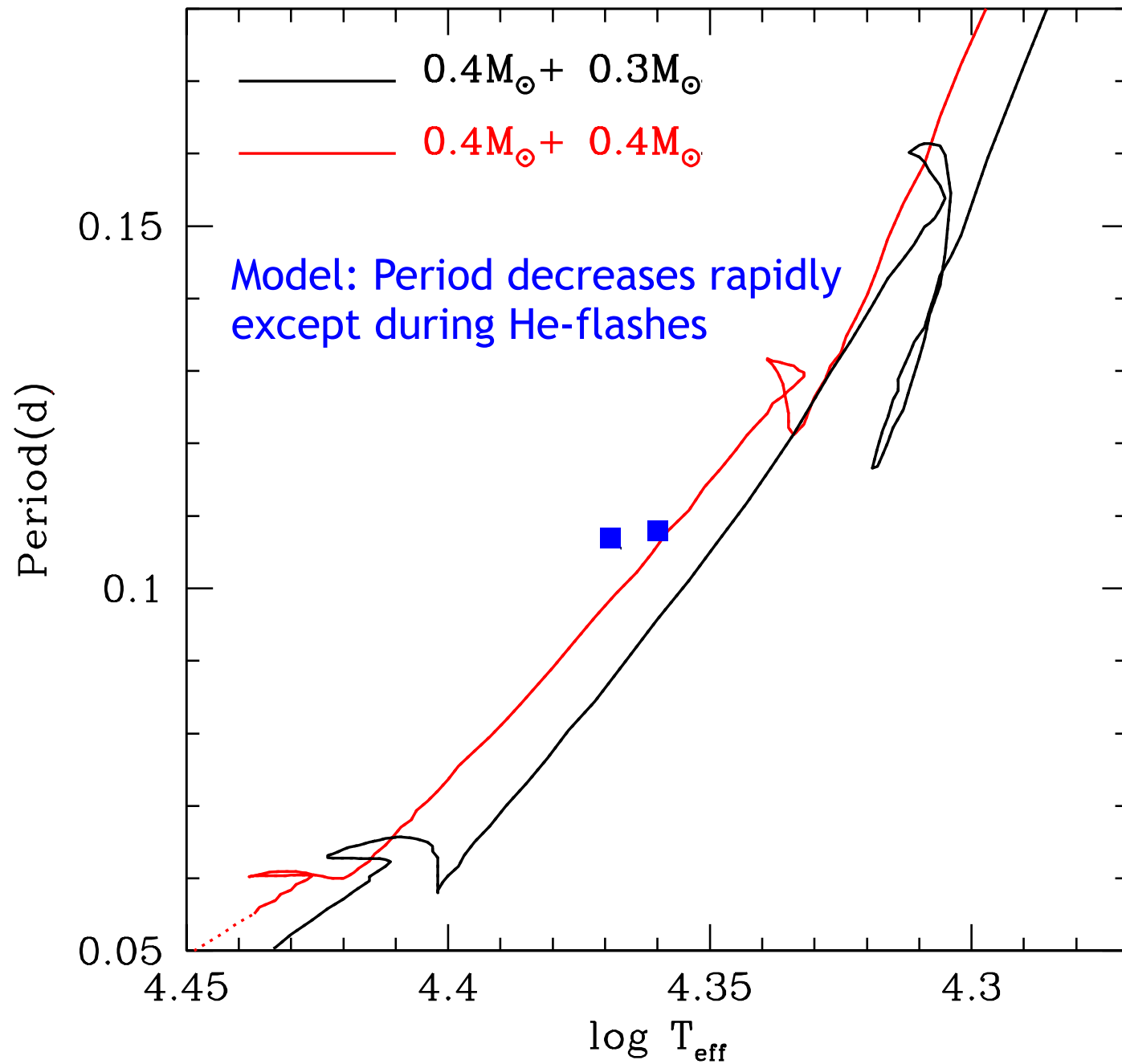
Accretion -> 外層加熱 -> 外層でHe flash発生  
 He flash が繰り返されながらその発生位置が中心へ  
 --> Helium ZAMS

その進化経路の途中に2つのHe星脈動星が存在  
 $M \sim 0.7 M_{\odot}$

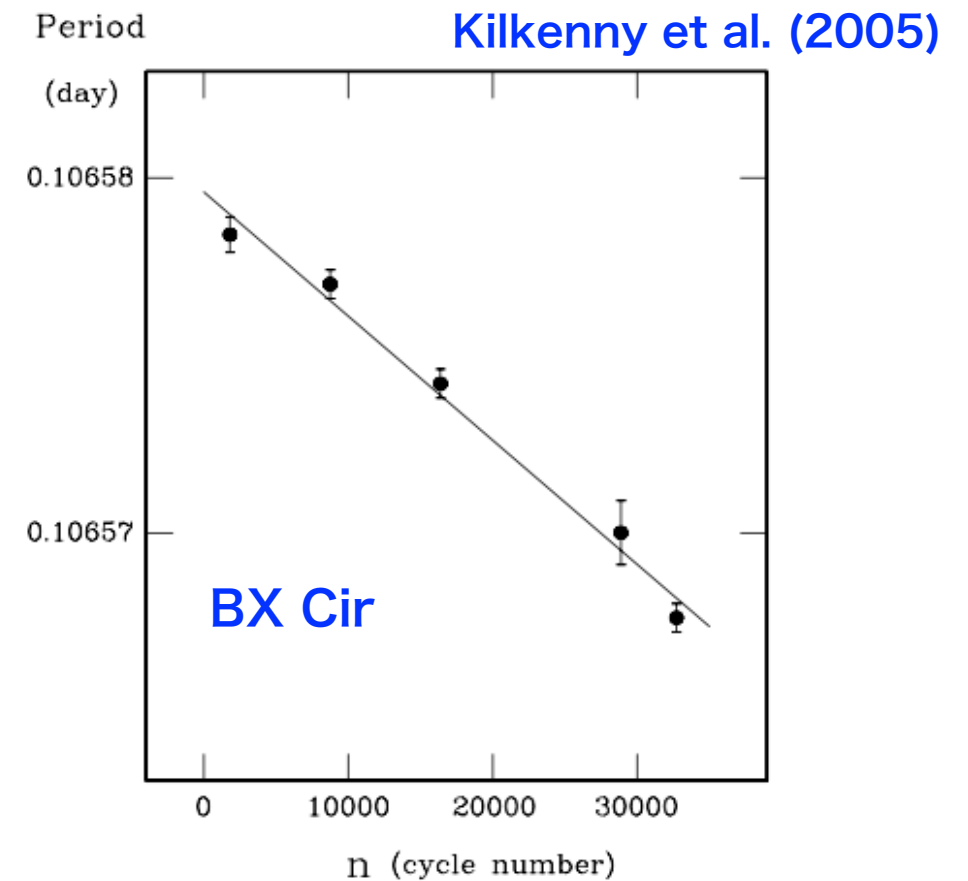
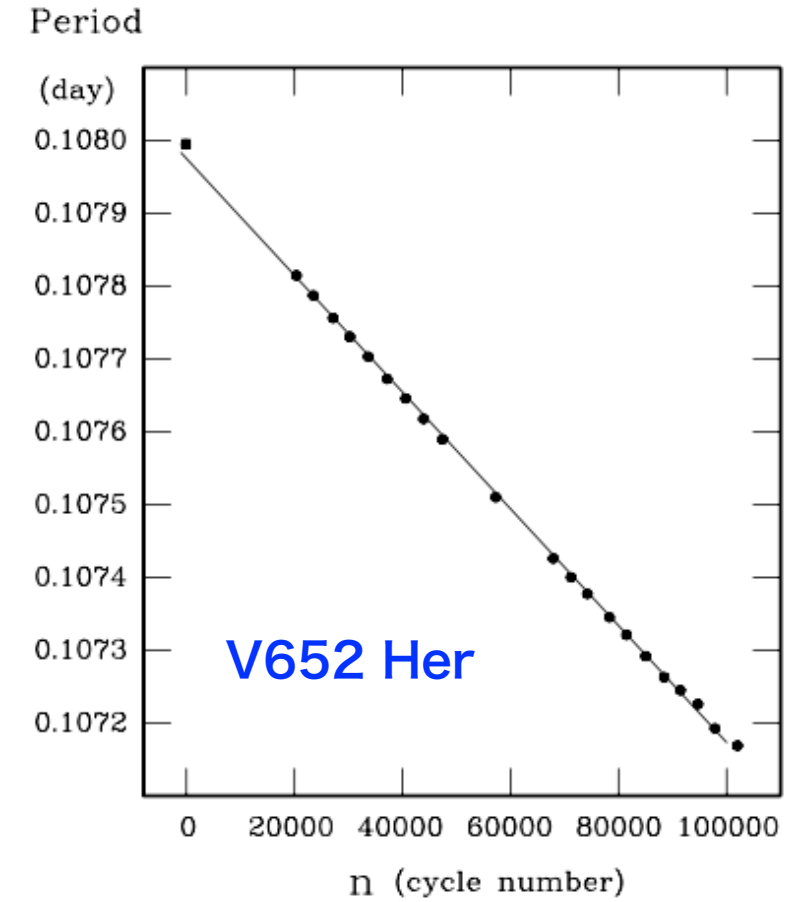




# Pulsation period changes with evolution



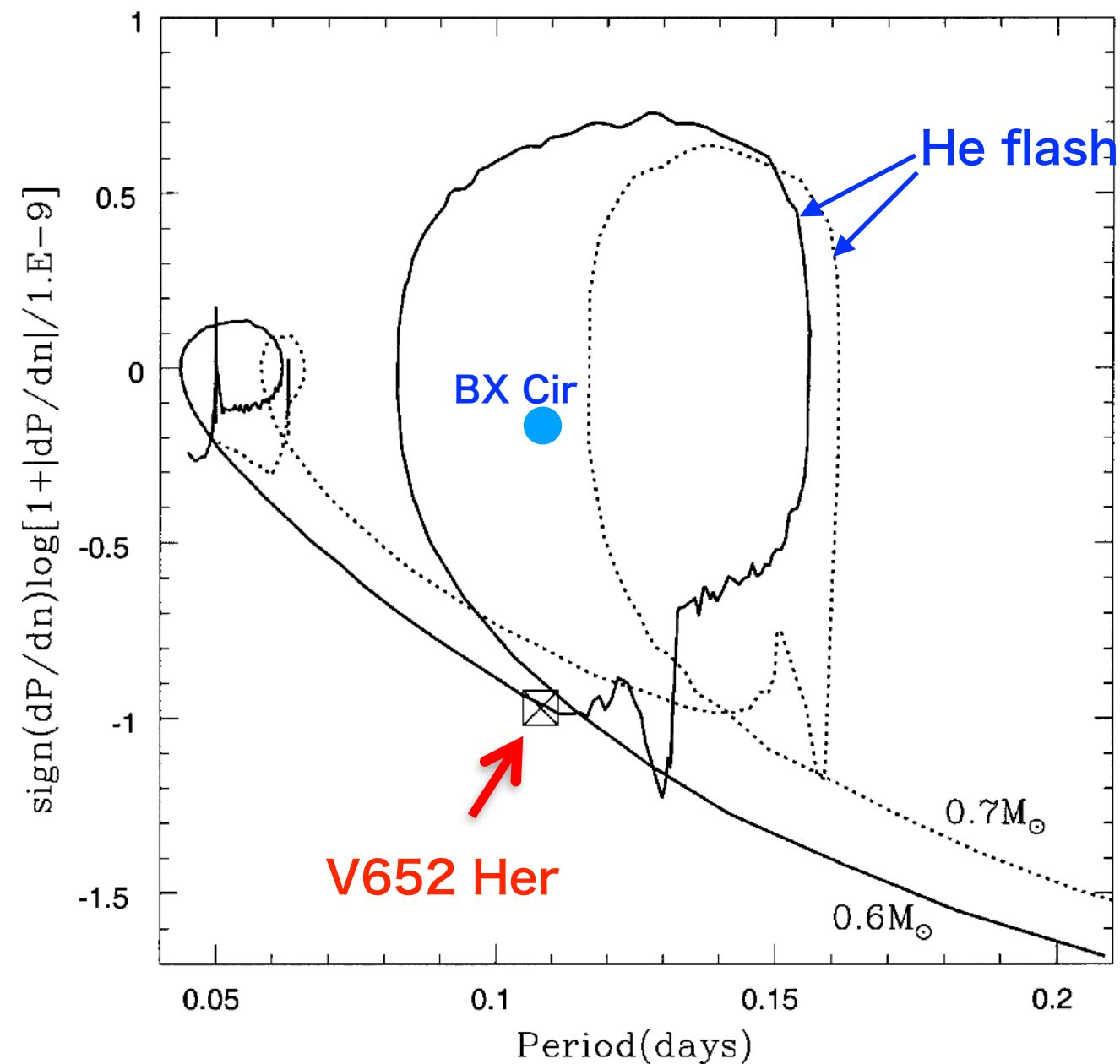
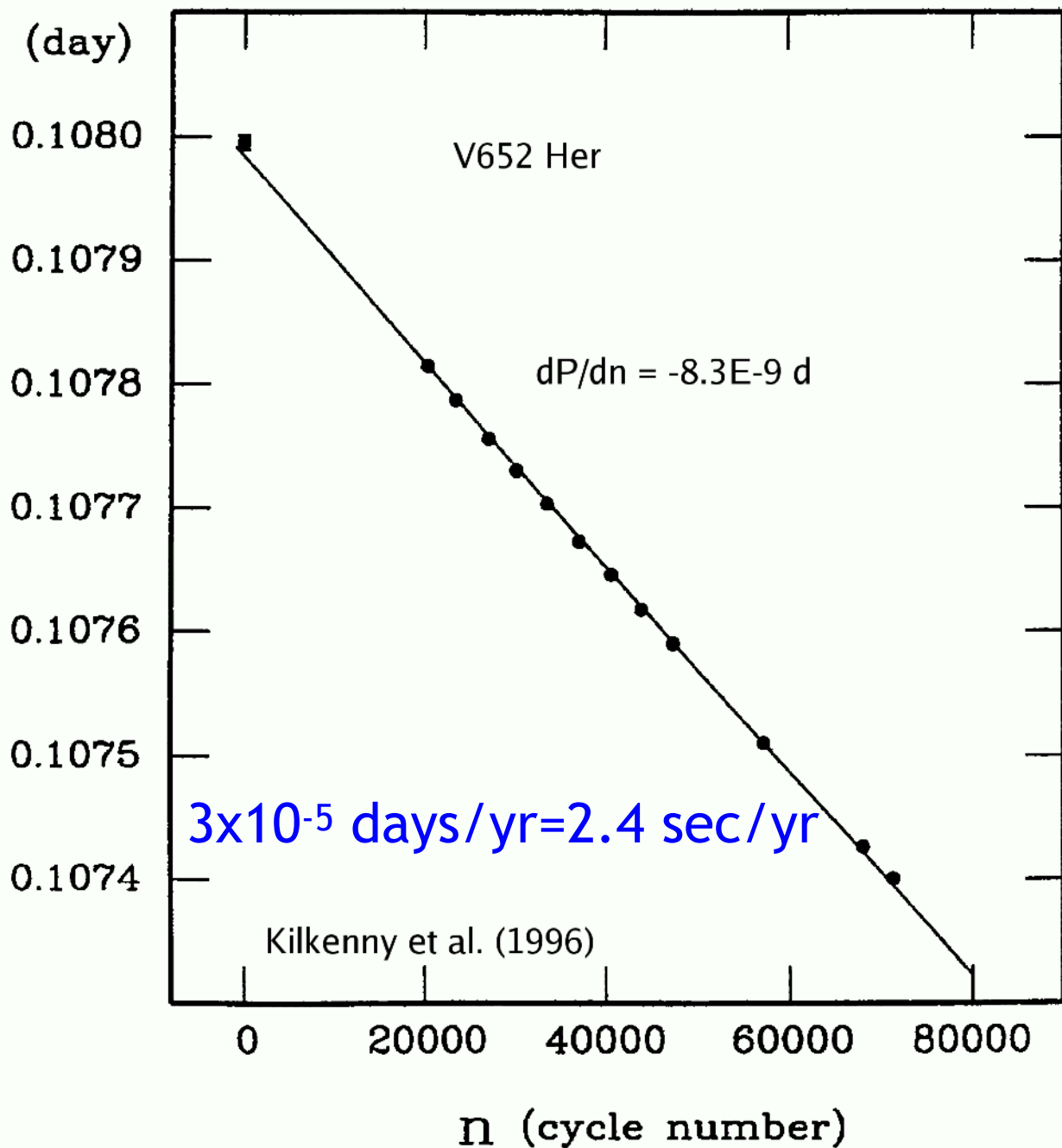
$$\Pi \propto \sqrt{\bar{\rho}} \propto R^{1.5}$$



# Period decrease rate of V652 Her agrees with a He-WD merger model

---> **WD merger が実際に起こった証拠**

'Instantaneous' Period

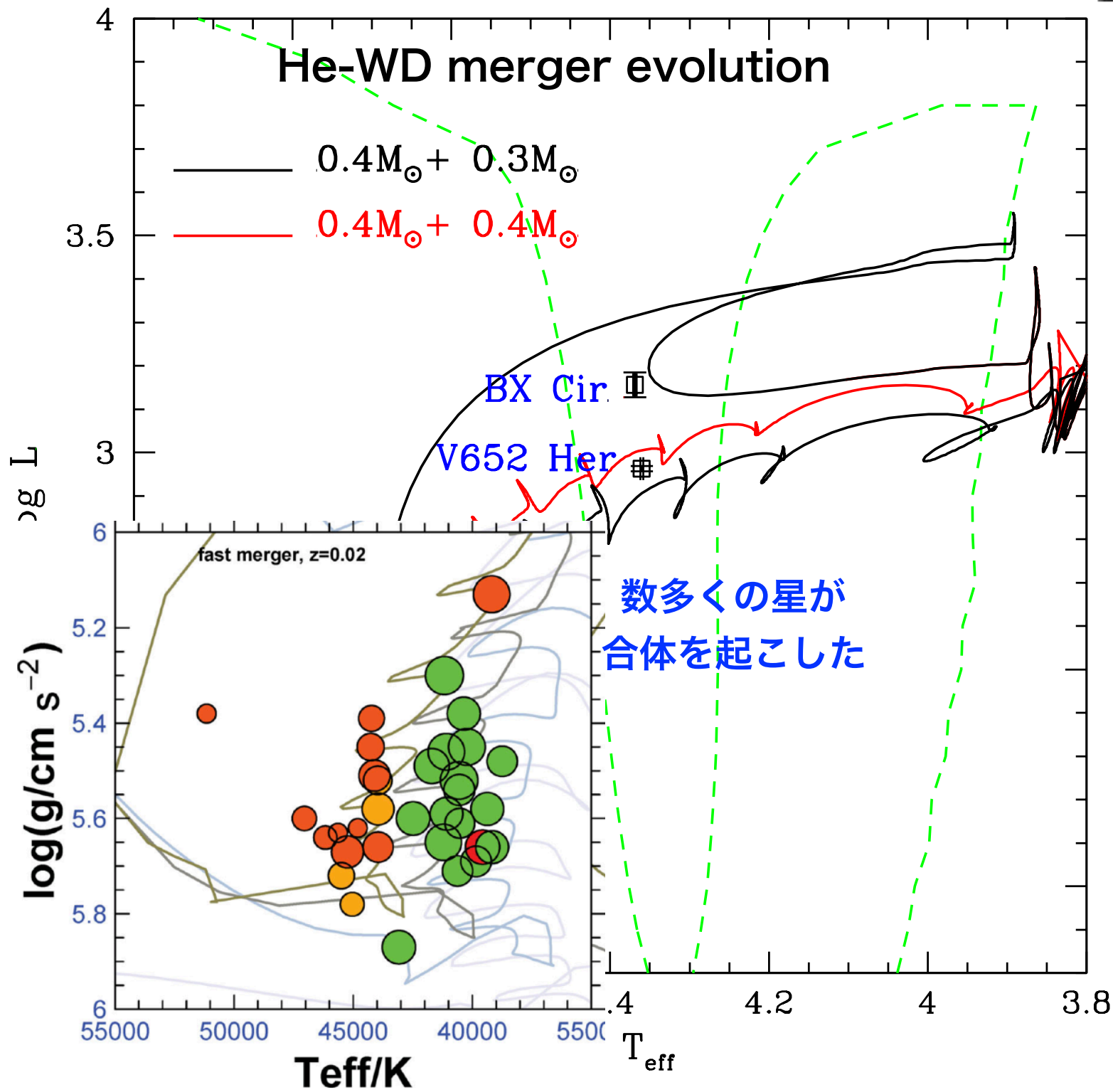


Saio & Jeffery (2000)

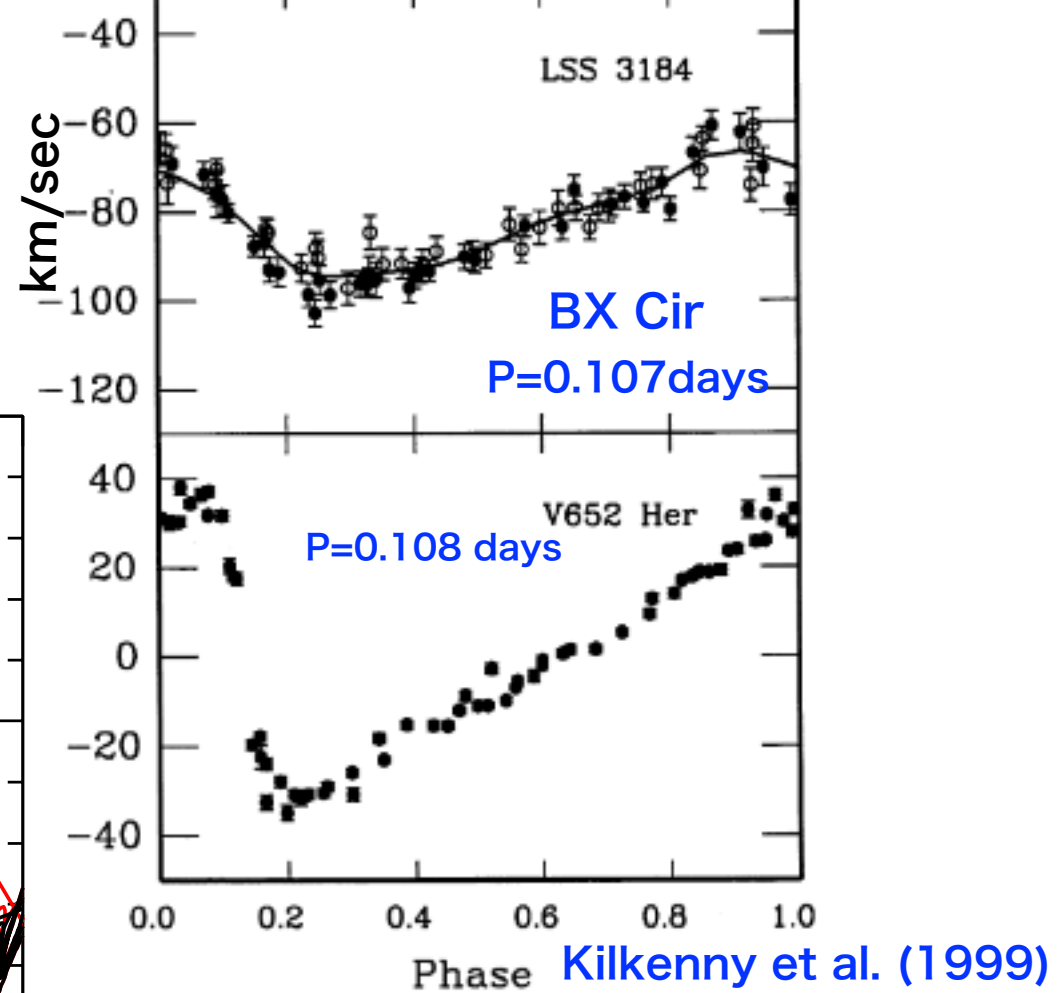
Figure 4. The rate of period change versus period for 0.7- and 0.6- $M_{\odot}$  cases, where  $dP/dn$  is the period change per cycle in days. The crossed square indicates the observed period and the period change rate of V652 Her (Kilkenny et al. 1996).

# Double He-WD merger models

## -- He-star pulsators



数多くの星が  
合体を起こした



Double RGB stars merger



Anomalous cepheids ?

Double He-WD (low-mass WD) merger



He-star pulsators & He-sdO

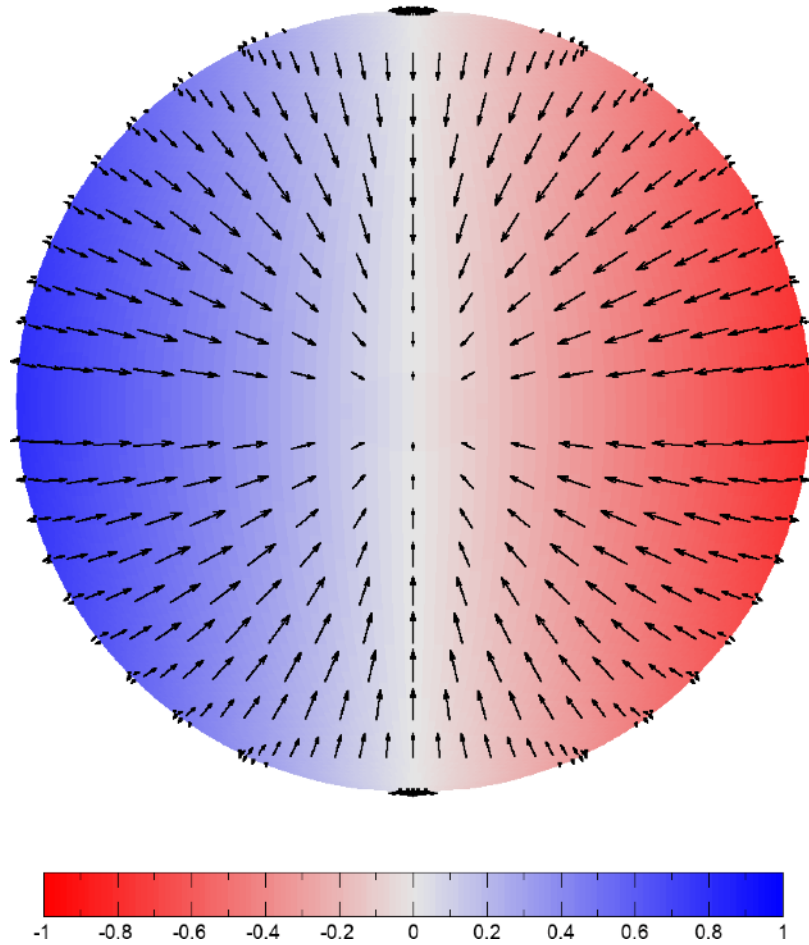
恒星の合体はそれほど稀な現象ではない



# g modes と r modes (浮力の影響を受けたglobal Rossby waves)

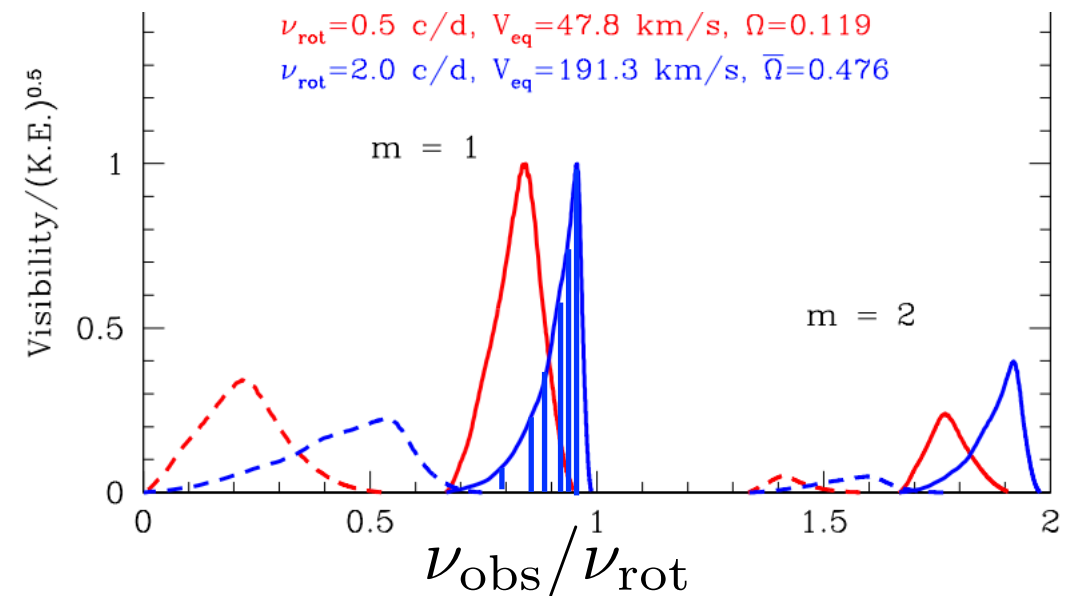
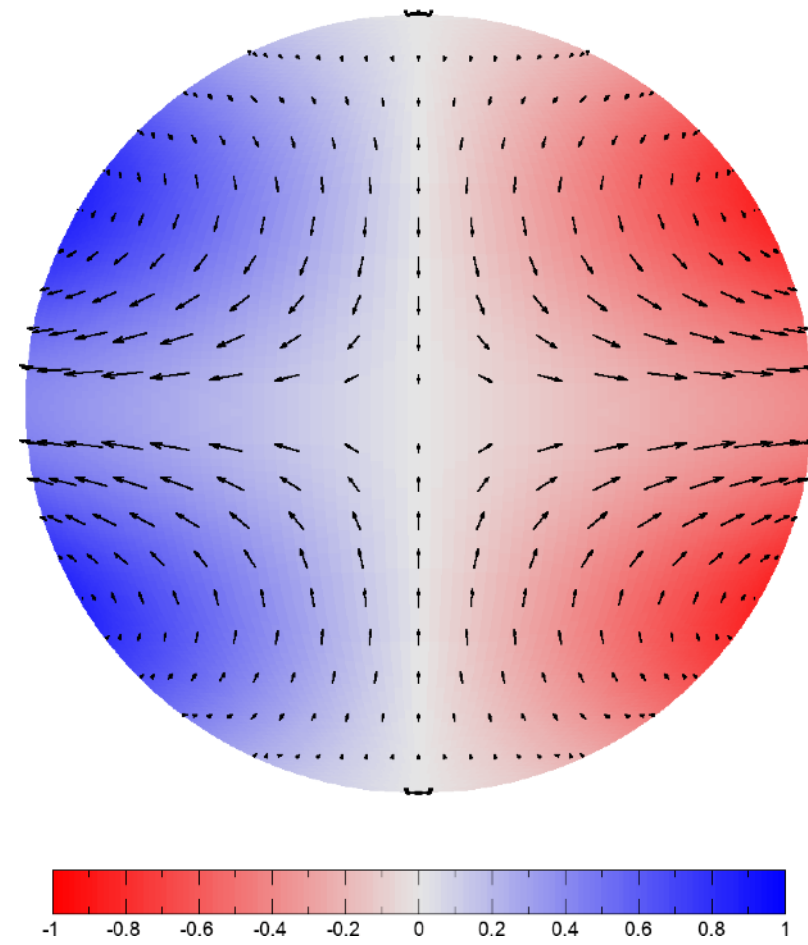
g mode

g mode:  $m = -1, k = 0, \text{spin} = 0.2$

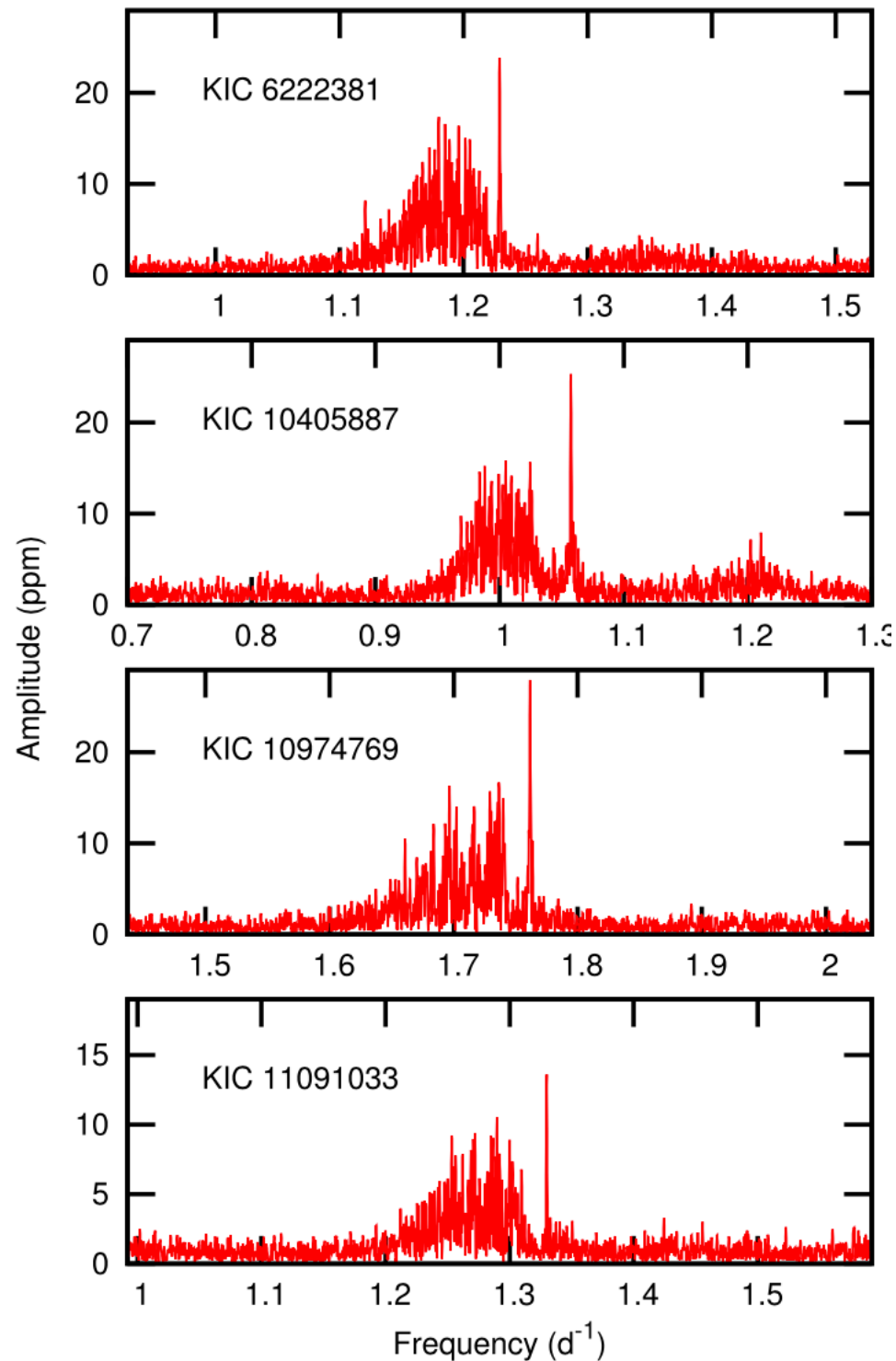


r mode

r mode:  $m = 1, k = -2, \text{spin} = 20.0$

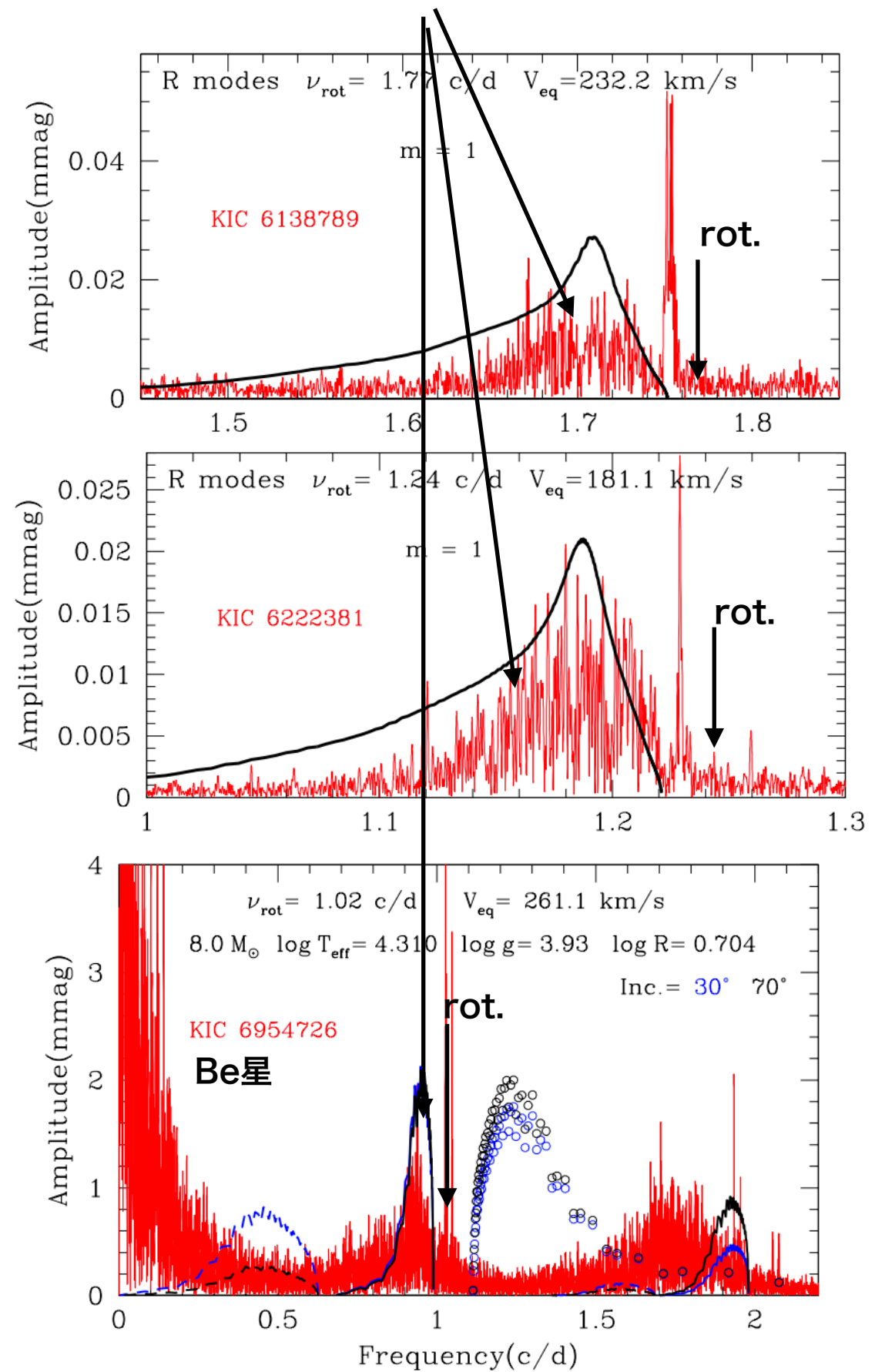


*Starspots on A stars* ]



Balona (2017)

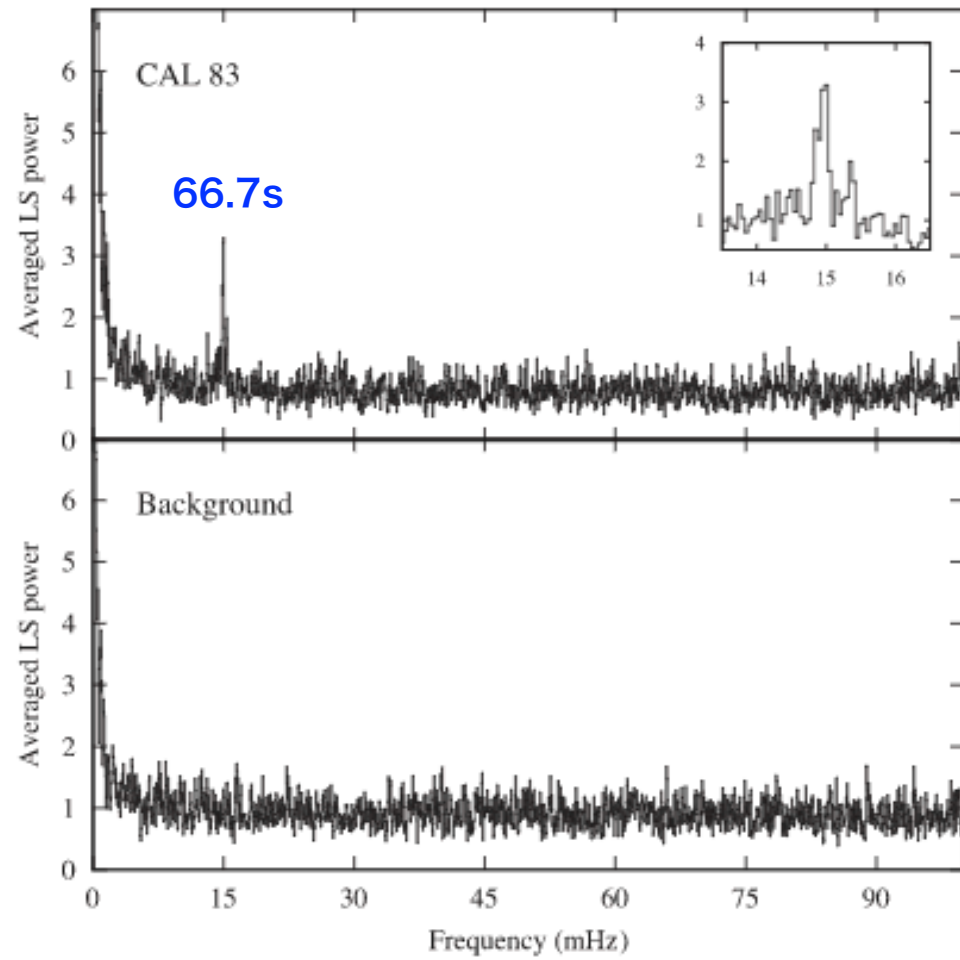
**r modes**



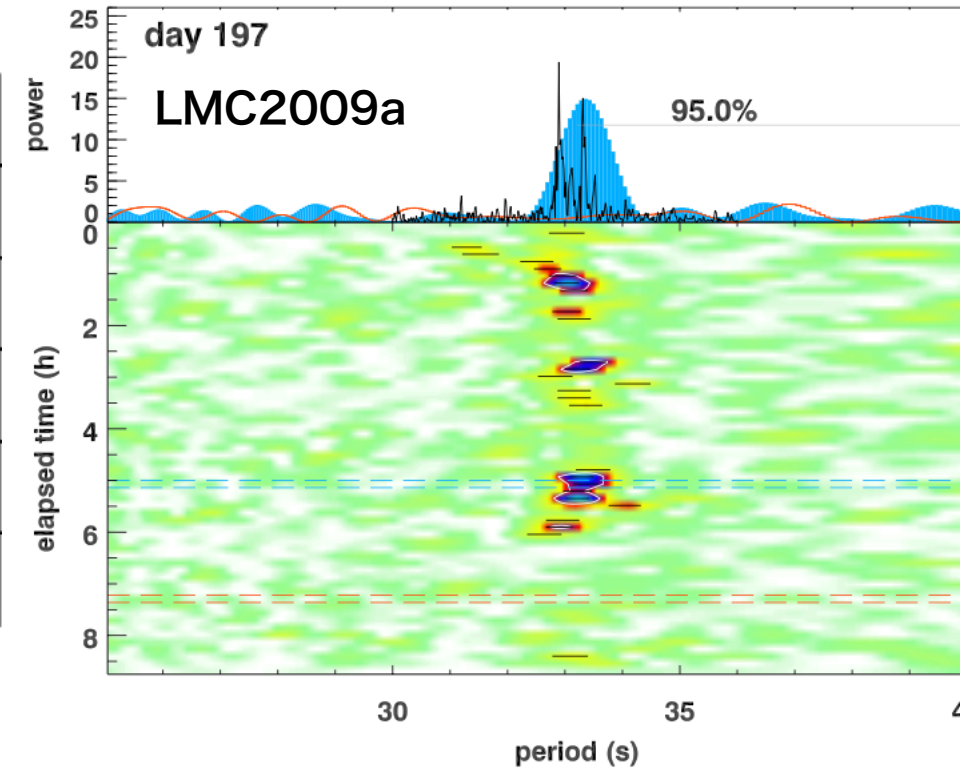
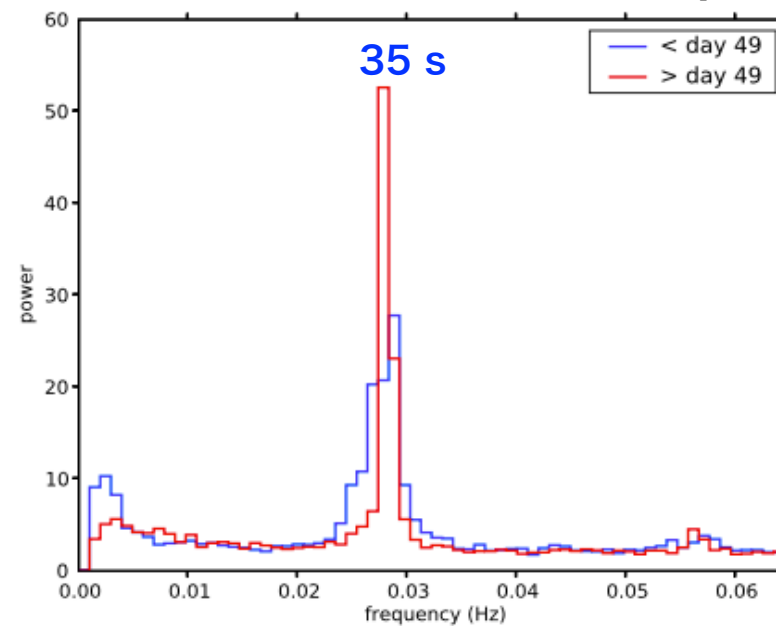
Saio et al.(2018)

# Short period oscillations in Super Soft Xray Sources r modes??

2952 *A. Odendaal et al. (2014)*

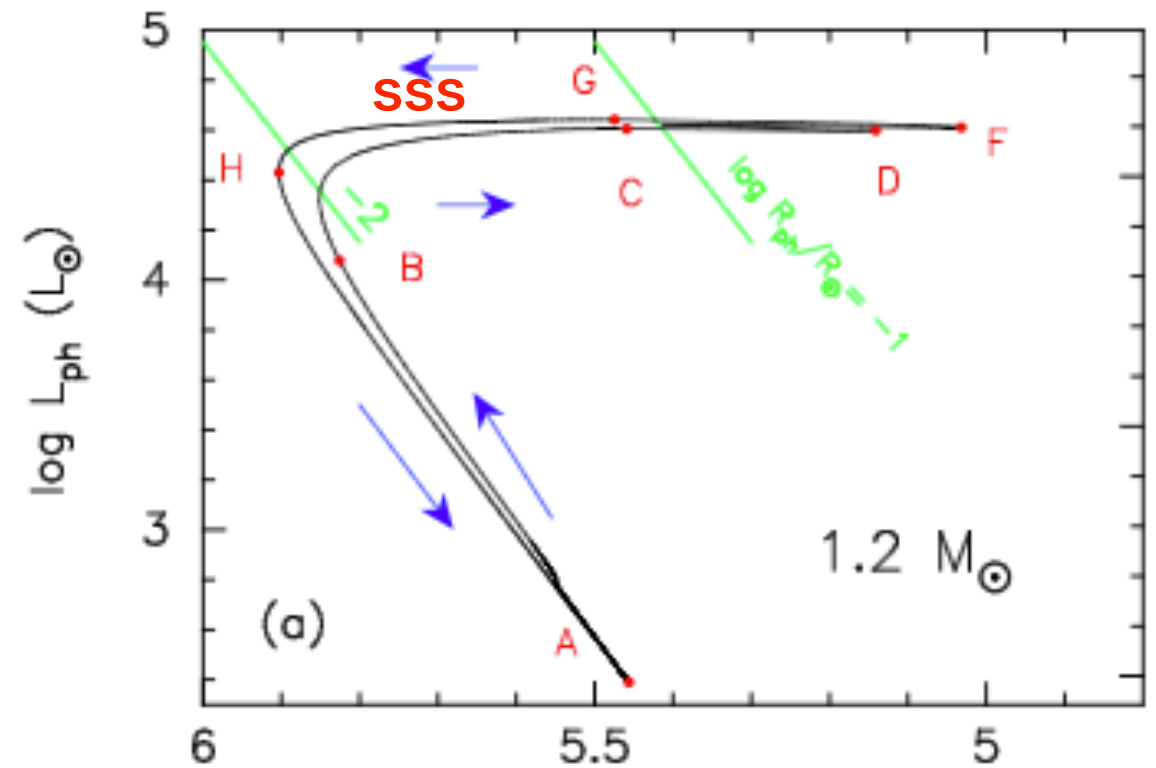
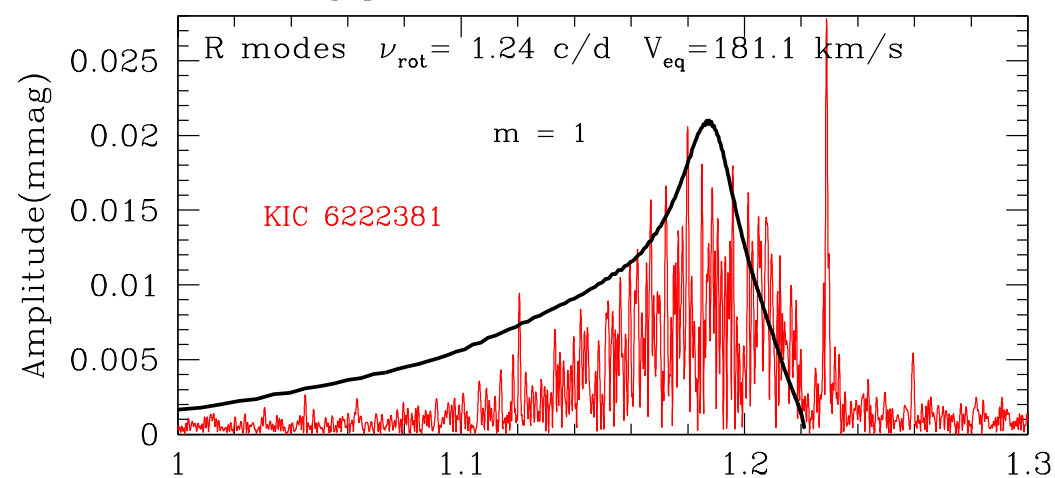


Osborne et al.(2011) RS Oph



*Ness et al. (2015)*

**A-type MS star; r modes**



*Kato et al (2017)*

# 星震学による恒星進化モデルの検証

齊尾英行（東北大学）

1. 恒星振動(脈動) についての introduction
2. 恒星振動から知る、主系列星・赤色巨星の進化段階と内部自転速度
3. 恒星の振動が示す対流領域の広がり・混合・質量放出など
4. 恒星の振動が示す恒星合体の起こった証拠
5. r modes (Rossby waves in stars)