

# Giant Planet Atmospheres and Spectra

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Direct measurements of the spectra of extrasolar giant planets are the keys to determining their physical and chemical nature. The goal of theory is to provide the tools and context with which such data are understood. It is only by putting spectral observations through the sieve of theory that the promise of exoplanet research can be realized. With the new *Spitzer* and HST data of transiting “hot Jupiters,” we have now dramatically entered the era of remote sensing. We are probing their atmospheric compositions and temperature profiles, are constraining their atmospheric dynamics, and are investigating their phase light curves. Soon, many non-transiting exoplanets with wide separations (analogs of Jupiter) will be imaged and their light curves and spectra measured. In this paper, we present the basic physics, chemistry, and spectroscopy necessary to model the current direct detections and to develop the more sophisticated theories for both close-in and wide-separation extrasolar giant planets that will be needed in the years to come as exoplanet research accelerates into its future.

## 1. INTRODUCTION

Our understanding of gas giant planets was informed for many decades by remote telescopic observations and in situ measurements of Jupiter and Saturn. These detailed investigations provided a fine-grained view of their atmospheric compositions, temperatures, dynamics, and cloud structures. However, they left us with a parochial view of the range of possible orbits, masses, and compositions that has now been shattered by the discovery of extrasolar giant planets (EGPs) in the hundreds. We have found gas giants in orbits from  $\sim 0.02$  AU to many AU, with masses from below Neptune’s to  $\sim 10 M_J$ , and around stars from M to F dwarfs. The corresponding stellar irradiation fluxes at the planet vary by a factor of  $\sim 10^5$ , and this variation translates into variations in atmosphere temperatures from  $\sim 100$  K to  $\sim 2500$  K. With such a range of temperatures and of orbital distances, masses, and ages, atmospheres can have starkly different compositions, can be clear or cloudy, and can evince dramatic day-night contrasts.

One must distinguish imaging of the planet itself by separating the light of planet and star, something that can currently be contemplated only for wide-separation planets, from measurements of the summed light when the orbit is tight and the planet can not be separately imaged. In the latter case, the planet’s light can be a non-trivial fraction of the total, particularly in the infrared. When transiting, such hot Jupiter systems provide an unprecedented opportunity to measure the planet’s emissions by the difference in the summed light of planet and star in and out of secondary eclipse and by the phase variation of that sum. Generally, the star itself will not vary with the period of the planet’s orbit. Moreover, in a complementary, but different, fash-

ion, the wavelength dependence of the transit depth is now being used to probe the composition of the planet’s atmosphere near the terminators. The extrasolar giant planets, by dint of their mass and luminosity, have been the first discovered, and will serve as stepping stones to the extrasolar terrestrial planets.

To understand in physical detail the growing bestiary of EGPs requires chemistry to determine compositions, molecular and atomic spectroscopy to derive opacities, radiative transfer to predict spectra, hydrodynamics to constrain atmospheric dynamics and heat redistribution, and cloud physics. In short, global 3D radiation-hydrodynamic general circulation models (GCMs) with multi-spectral, multi-angle, and non-equilibrium chemistry and kinetics will be needed. We are not there yet, but basic treatments have emerged that allow us to interpret and constrain day-night differences, profiles, molecular compositions, and phase light curves.

In this chapter we lay out some of the basic elements of any theoretical treatment of the atmospheres, spectra, and light curves of EGPs. This theory provides the necessary underpinnings for any progress in EGP studies, a subject that is engaging an increasing fraction of the world’s astronomical and planetary science communities. In §2.1, we summarize the techniques for calculating molecular abundances. We follow in §2.2 with an explication of general methods for assembling opacity tables. Section 2.3 touches on Rayleigh scattering, and then we continue in §2.4 with a tutorial on albedos and phase functions. In §2.5, we explain the nature of the transit radius. Section 2.7 contains a very useful analytic model for the atmospheric thermal profile of EGPs, which is a generalization for irradiated atmospheres of the classic Milne problem. This model incorporates a

condition for thermal inversions. Then, in §3 we summarize lessons learned and knowledge gained from the decades-long study of Jupiter and Saturn. This includes discussions of their spectra, cloud layers, temperatures, and compositions. Having set the stage, we review in §4.1 the general chemistry and atmospheric character of EGPs as a function of orbital distance and age. This subsection includes a diversion into the putative evolution of Jupiter itself. We follow this in §4.2 with a few paragraphs on theoretical EGP planet/star flux ratios as a function of wavelength and distance, focusing on wide-separation ( $> 0.2$  AU) EGPs. Then, in §4.3 we present highlights from recent campaigns of direct detection of transiting EGP atmospheres, with an emphasis on secondary eclipse measurements, the compositions inferred, atmospheric temperatures, and thermal inversions. Finally, in §5 we list some of the outstanding open issues and future prospects in the study of EGP atmospheres and spectra.

## 2. MODELING CONCEPTS AND EQUATIONS

In this section, we present the core ingredients necessary to construct theories of the atmospheres and spectra of EGPs. These includes general chemistry, opacities, and simple formalisms for the calculation of albedos and phase light curves. We discuss the concept of “transit radius” and include an analytic theory for the temperature profiles of irradiated exoplanets. The resulting approximate equations make clear the key role of opacity and its wavelength dependence in determining the character of EGP thermal profiles, in particular in creating thermal inversions when they arise. Such inversions have been inferred for many of the hot Jupiters seen in secondary eclipse and are emerging as one of the most exciting and puzzling features of current exoplanet research.

### 2.1 Calculation of Atomic and Molecular Abundances in Chemical Equilibrium

Before any opacities or atmospheric models can be calculated, the abundances of a mixture of a large number of species have to be determined for the given temperature and pressure. The assumption of chemical equilibrium is a good starting point, though non-equilibrium kinetics may play a role. Despite this, we present here a straightforward discussion of such calculations. Much of this presentation on abundances and that of §2.2 on opacities can be found in Burrows & Sharp (1999) or Sharp & Burrows (2007), to which the reader is referred. In addition, there are excellent reviews and/or accounts in Lodders (1999) Fegley & Lodders (1994,2001), Lodders & Fegley (2002), and Sharp & Huebner (1990).

For a given temperature, pressure, and composition, the equilibrium abundances of the various species can be determined by minimizing the total Gibbs free energy of the system. This requires a knowledge of the free energy of each species as a function of temperature, which is normally obtained from thermodynamic data. At the temperatures for

which data are tabulated, least-square fits can be made for a set of polynomials whose highest order is given by

$$\Delta G_{pi}(T) = aT^{-1} + b + cT + dT^2 + eT^3, \quad (1)$$

where  $a$ ,  $b$ ,  $c$ ,  $d$ , and  $e$  are fitted coefficients, and  $\Delta G_{pi}(T)$  is the fitted Gibbs free energy of formation at temperature  $T$  of species  $i$  in phase  $p$ . The polynomials are evaluated at the tabulated points and the deviations from the tabulated values are obtained.

In performing the calculation for a particular temperature, pressure, and composition, the Gibbs free energy for each species is obtained from the database using the fitted coefficients at the temperature required, then the total free energy of the system is minimized to obtain the abundances of the gas-phase species, together with any condensates. The total dimensionless free energy is given by

$$\frac{G(T)}{RT} = \sum_{i=1}^m \left[ n_{1i} \left\{ \frac{\Delta G_{1i}(T)}{RT} + \ln P + \ln \left( \frac{n_{1i}}{N} \right) \right\} \right] + \frac{1}{RT} \sum_{p=2}^{s+1} \left[ n_{p1} \Delta G_{p1}(T) \right], \quad (2)$$

where  $R$  is the gas constant ( $k_B N_A$ ), and for the first sum for the gas phase with  $p = 1$ ,  $P$  is the total pressure in atmospheres,  $N$  is the number of moles,  $m$  is the number of species,  $n_{1i}$  is the number of moles of species  $i$ , and  $\Delta G_{1i}(T)$  is the corresponding free energy of that species. The second sum is over the  $s$  condensed phases, which may include multiple phases of the same species, but except at a phase boundary, only one phase of a particular species in a condensed form is assumed present at any time, though one may consider solid or liquid solutions. Consequently,  $n_{p1}$  is the number of moles of a condensed species and  $\Delta G_{p1}(T)$  is the free energy of that species. Since there is only one species per phase, for convenience we generally set  $i$  equal to 1.

A subset of 30 gas-phase species out of nearly 350 gas-phase species are usually the most important and selected for detailed treatment. The species are the neutral atoms: H, He, Li, Na, K, Rb, Cs, Al, Ca, and Fe, the ions:  $e^-$ ,  $H^+$ , and  $H^-$ , the metal hydrides: MgH, CaH, FeH, CrH and TiH, with the remaining molecules being  $H_2$ ,  $N_2$ , CO, SiO, TiO, VO, CaOH,  $H_2O$ ,  $H_2S$ ,  $NH_3$ ,  $PH_3$ , and  $CH_4$ .

Figure 1 depicts a representative result (here at 1 atmosphere pressure and solar elemental abundances) for the temperature dependence of the equilibrium mixing ratios of water, methane, carbon monoxide, hydrogen sulfide, phosphene, molecular nitrogen, ammonia, TiO, and VO. The last two species may or may not play a role in EGP atmospheres, whereas the others certainly do.

### 2.2 Calculation of Atomic and Molecular Opacities

The calculation of the absorption cross sections and opacities of molecules is made more difficult than that for

atoms by the substantially larger number of transitions and levels involved. Polyatomic species can have hundreds of millions, even billions, of vibrational and rotational lines, multiple electronic states, and a complicating mix of isotopes. Since it is not possible to measure with precision many transitions to determine their oscillator strengths or Einstein  $A$  coefficients, ab initio calculations using quantum chemical techniques are frequently necessary. Such calculations can be, and frequently are, calibrated with only a few measurements at selected wavelengths, but the experimental determination of the quantum numbers of the upper and lower states of even a given measured transition can be ambiguous. Moreover, particularly for hot Jupiters, the high temperatures experienced require a knowledge of absorption transitions from excited states, the so-called “hot bands,” for which there are rarely measurements. For instance, the methane hot bands and some of the hot bands of water are completely unconstrained by current experiment, despite the fact that both water and methane are important greenhouse gases in the Earth’s atmosphere.

The situation is made even more difficult by the almost complete absence of calculations or measurements of line broadening coefficients or line profiles. The upshot is that theorists rely on imperfect and by-and-large uncalibrated compilations of theoretical line lists, and very approximate theories for line broadening. Some molecules are done better than others, but even for atoms, for which theory and measurement are rather better, line shapes are not well constrained. In the context of EGPs, this is particularly relevant for the alkali metals.

Despite these drawbacks, a rather sophisticated and extensive database of opacities for the constituents of EGPs has been assembled. In this subsection, taken in part from the review paper by Sharp & Burrows (2007), we summarize the techniques and methodologies needed to derive these opacities and use cgs units for specificity. Another useful review is that of Freedman, Marley, & Lodders (2008).

The calculation of the line strengths for each line of each species depends on the data available for the species being considered, so different methods have to be used. In order to reduce the chances of errors with input data in different forms, it is recommended to convert, if necessary, all the line strengths into the same uniform system, with the best being integrated line strengths in  $\text{cm}^2\text{s}^{-1}\text{species}^{-1}$ . These depend only on the temperature. The lines should then be broadened into a profile which is dependent on the pressure, then the absorption in  $\text{cm}^2\text{species}^{-1}$  across the profile should be computed, summing the contributions from any overlapping profiles. The absorption for each species obtained in this manner depends on the temperature and pressure. The total opacity of the gas is obtained by summing the individual contributions weighted by the corresponding number densities (in  $\text{cm}^{-3}$ ) for each of the species, yielding the total volume opacity in  $\text{cm}^2\text{cm}^{-3}$ , i.e.  $\text{cm}^{-1}$ . However, the total mass opacity in  $\text{cm}^2\text{g}^{-1}$  is usually the required result, and is obtained by dividing the volume opacity by the gas mass density.

In its most general LTE (Local Thermodynamic Equilibrium) form, the integrated strength  $S$  of a spectral line in  $\text{cm}^2\text{s}^{-1}\text{species}^{-1}$  is

$$S = \frac{\pi e^2 g_i f_{ij}}{m_e c} \frac{e^{-hcF_i/kT}}{Q(T)} \left[ 1 - e^{-hc(F_j - F_i)/kT} \right], \quad (3)$$

where  $g_i$  and  $f_{ij}$  are the statistical weight of the  $i^{\text{th}}$  energy level and the oscillator strength for a transition from that level to a higher level  $j$ ,  $F_i$ , and  $F_j$  are the term values (excitation energies) in  $\text{cm}^{-1}$  of the  $i^{\text{th}}$  and  $j^{\text{th}}$  levels participating in the transition, and  $Q(T)$  is the partition function of the species at some temperature  $T$ . The other symbols have their usual meanings. Note that the first term in eq. (3) gives the line strength in  $\text{cm}^2\text{s}^{-1}\text{absorber}^{-1}$ , the next term with the Boltzmann factor and the partition function converts this to the required line strength, and the last term is the stimulated emission correction factor, where  $F_j - F_i$  is the transition frequency in wavenumbers, i.e.  $\bar{\nu}$  in  $\text{cm}^{-1}$ . Although monochromatic opacities are frequently displayed as functions of wavelength, it is recommended that all opacity calculations be performed internally in wavenumbers, even if some of the input data are given in wavelengths, since most molecular spectroscopic constants and energy levels are expressed in  $\text{cm}^{-1}$ , and adopting a uniform system of units reduces the chances of error. Note that some of the data available are not expressed in the form of oscillator strengths and statistical weights, collectively given as  $gf$ -values, but in other forms that must be converted to the required lines strengths.

The general expression for calculating the partition function is given by

$$Q(T) = \sum_{i=1}^n g_i e^{-hcF_i/kT}, \quad (4)$$

where the summation is performed over the first  $n$  levels, whose contributions are required at the highest temperatures of interest. The term value of the lowest level  $F_1$ , i.e. the ground state, is zero by construction.

Figure 2 portrays a representative set of absorption cross sections as a function of wavelength in the infrared for the vibration-rotation transitions of  $\text{H}_2\text{O}$ ,  $\text{NH}_3$ , and  $\text{CH}_4$ . Many of the most important absorption bands in EGP atmospheres are shown and these were calculated using the formalism described in this subsection.

### 2.3 Rayleigh Scattering

Rayleigh scattering is a conservative scattering process by atoms and molecules. Although strong in the ultraviolet/blue, the scattering cross sections quickly fade toward the red region of the spectrum ( $\propto \lambda^{-4}$ ). Rayleigh scattering has little effect on the spectra of isolated brown dwarfs, but irradiated EGPs reflect a non-zero fraction of the incident intensity.

The Rayleigh scattering cross sections are derived from polarizabilities, which are in turn derived from refractive indices. The refractive indices are readily available at 5893 Å (Na D) and are assumed not to vary strongly with wavelength. The Rayleigh cross sections are derived via,

$$\sigma_{Ray} = \frac{8}{3}\pi k^4 \left( \frac{n-1}{2\pi L_0} \right)^2, \quad (5)$$

where  $n$  is the index of refraction,  $k$  is the wavenumber ( $2\pi/\lambda$ ), and  $L_0$  is Loschmidt's number, the number of molecules per cubic centimeter at STP ( $= 2.687 \times 10^{19}$ ). Given the strong inverse dependence on wavelength of eq. (5), Rayleigh scattering is most pronounced in the blue and ultraviolet and is ultimately responsible for the Earth's blue sky.

## 2.4 Albedos and Phase Functions

Objects in the solar system, such as planets, asteroids, and moons, are seen and studied in reflected solar light. The brightness of the reflection depends upon the orbital distance, the stellar flux, the reflectivity of the object, the detector angle (the “phase angle”), and the object's radius. The reflectivity, in the guise of an “albedo” (defined below), bears the stamp of the composition of its surface and/or atmosphere, and its wavelength dependence is a distinctive and discriminating signature. Solar-system objects are too cold to emit much in the optical, where the Sun is brightest, but emit in the mid-infrared, where the peak of a  $\sim 40$ -800 K black body resides. Hence, there is a simple and obvious separation in their spectra between reflection and emission bumps that allows an unambiguous definition of the albedo and its interpretation as a dimensionless reflectivity bounded by a value of “one” (however, see below), the latter implying full reflection and no absorption.

However, some EGPs, the close-in and transiting variants, are so near their central stars that their surface and atmospheric temperatures can be quite large ( $\sim 1000$ -2500 K). Hot planets (due to either proximity or youth) can be self-luminous in the near infrared (and even in the optical). As a result, the reflection and emission components can overlap in wavelength space, and are not so cleanly separated, as they are for solar-system objects. The upshot is that the albedo and “reflectivity” might be misnomers, particularly in the near-IR. Nevertheless, the planet/star flux ratio as a function of wavelength is an important probe of EGP atmospheres and has to date been used with profit to diagnose their thermal and compositional character. This is true despite the fact that the associated albedos could be far above one at some wavelengths<sup>1</sup>. With this caveat in mind and the traditional interpretation intact for planets at greater orbital distances and older ages similar to the Jupiter/Sun pair, we proceed to develop the formalism by which the

planet/star flux ratio is calculated, the albedo is defined, and why they are important. In the process we distinguish the geometric albedo ( $A_g$ ), the spherical albedo ( $A_s$ ), and the Bond albedo ( $A_B$ ), and connect them to the planet/star flux ratio,  $F_p/F_*$ . We also introduce the “phase function,” by which the observed light curve is described. Much of the development below is taken from papers by Sudarsky, Burrows, & Pinto (2000), Sudarsky, Burrows, Hubeny, & Li (2005), and Burrows, Sudarsky, & Hubeny (2004). The papers by Marley et al. (1999) and Burrows, Ibgui, & Hubeny (2008) are also good resources on this general topic.

Planetary phase is a function of the observer-planet-star orientation, and the angle whose vertex lies at the planet is known as the *phase angle* ( $\alpha$ ). The formalism for the computation of planetary brightness as a function of phase angle has been presented by numerous authors. Following Sobolev (1975), one can relate the planetary latitude ( $\psi$ ) and longitude ( $\xi$ ) to the cosine of the angle of incident radiation ( $\mu_0$ ) and the cosine of the angle of emergent radiation ( $\mu$ ) at each point on the planet's surface:

$$\mu_0 = \cos \psi \cos(\alpha - \xi) \quad (6)$$

and

$$\mu = \cos \psi \cos \xi, \quad (7)$$

where latitude is measured from the orbital plane and longitude is measured from the observer's line of sight. The phase angle is then,

$$\alpha = \cos^{-1} \left( \mu \mu_0 - [(1 - \mu^2)(1 - \mu_0^2)]^{1/2} \cos \phi \right), \quad (8)$$

where  $\phi$  is the azimuthal angle between the incident and emergent radiation at a point on the planet's surface. The emergent intensity from a given planetary latitude and longitude is

$$I(\mu, \mu_0, \phi) = \mu_0 S \rho(\mu, \mu_0, \phi), \quad (9)$$

where the incident flux on a patch of the planet's surface is  $\pi \mu_0 S$ , and  $\rho(\mu, \mu_0, \phi)$  is the reflection coefficient. In order to compute the energy reflected off the entire planet, one must integrate over the surface of the planet. For a given planetary phase, the energy per time per unit area per unit solid angle received by an observer is

$$E(\alpha) = 2S \frac{R_p^2}{d^2} \int_{\alpha-\pi/2}^{\pi/2} \cos(\alpha - \xi) \cos(\xi) d\xi \times \int_0^{\pi/2} \rho(\mu, \mu_0, \phi) \cos^3 \psi d\psi, \quad (10)$$

where  $R_p$  is the planet's radius and  $d$  is the distance to the observer. This quantity is related to the *geometric albedo* ( $A_g$ ), the reflectivity of an object at full phase ( $\alpha = 0$ ) relative to that of a perfect Lambert disk (for which  $\rho(\mu, \mu_0, \phi) = 1$ ) of the same radius under the same incident flux, by

$$A_g = \frac{E(0)d^2}{\pi S R_p^2}, \quad (11)$$

<sup>1</sup>Note that if the complete radiative transfer solution with stellar irradiation is derived, the concept of an albedo is redundant and unnecessary.

where  $E(0)$  is  $E(\alpha)$  at  $\alpha = 0$ . A planet in orbit about its central star displays a range of phases, and the planet/star flux ratio is given by

$$\frac{F_p}{F_*} = A_g \left( \frac{R_p}{a} \right)^2 \Phi(\alpha), \quad (12)$$

where  $\Phi(\alpha)$  is the classical *phase function*, which is equal to  $E(\alpha)/E(0)$ ,  $R_p$  is the planet's radius, and  $a$  is its orbital distance. This formula is one of the core relationships in the study of irradiated and reflecting EGPs.

$\Phi(\alpha)$  is normalized to be 1.0 at full face, thereby defining the geometric albedo, and is a decreasing function of  $\alpha$ . For Lambert reflection, an incident ray on a planetary patch emerges uniformly over the exit hemisphere,  $A_g$  is  $2/3$  for purely scattering atmospheres, and  $\Phi(\alpha)$  is given by the formula:

$$\Phi(\alpha) = \frac{\sin(\alpha) + (\pi - \alpha) \cos(\alpha)}{\pi}. \quad (13)$$

However, EGP atmospheres are absorbing and the anisotropy of the single scattering phase function for grains, droplets, or molecules results in non-Lambertian behavior. For instance, back-scattering off cloud particles can introduce an "opposition" effect for which the planet appears anomalously bright at small  $\alpha$ . Figure 3 provides some theoretical EGP phase functions taken from Sudarsky et al. (2005) in which this effect is clearly seen. Figure 4 depicts the corresponding phase curves for some the solar system objects. These two figures together suggest a likely range for exoplanets.

Both  $A_g$  and  $\Phi(\alpha)$  are functions of wavelength, but the wavelength-dependence of  $A_g$  is the most extreme. In fact, for cloud-free atmospheres, due to strong absorption by molecular bands,  $A_g$  can be as low as 0.03, making such objects very "black." Rayleigh scattering serves to support  $A_g$ , but mostly in the blue and UV, where various exotic trace molecules can decrease it. The presence of clouds increases  $A_g$  significantly. For instance, at  $0.48 \mu\text{m}$ , Jupiter's geometric albedo is  $\sim 0.46$  and Saturn's is 0.39 (Karkoschka 1999). However, for orbital distances less than 1.5 AU, we expect the atmospheres of most EGPs to be clear. The albedo is correspondingly low. As a consequence, the theoretical albedo is very non-monotonic with distance, ranging in the visible from perhaps  $\sim 0.3$  at 0.05 AU, to  $\sim 0.05$  at 0.2 AU, to  $\sim 0.4$  at 4 AU, to  $\sim 0.7$  at 15 AU. In the visible ( $\sim 0.55 \mu\text{m}$ ), the geometric albedo for a hot Jupiter is severely suppressed by Na-D at  $0.589 \mu\text{m}$ . Due to a methane feature, the geometric albedo can vary from 0.05 at  $\sim 0.6 \mu\text{m}$  to  $\sim 0.4$  at  $0.625 \mu\text{m}$ . Hence, variations with wavelength and with orbital distance by factors of 2 to 10 are expected.

$\Phi(\alpha)$  and  $A_g$  must be calculated or measured, but the sole dependence of  $\Phi(\alpha)$  on  $\alpha$  belies the complications introduced by an orbit's inclination angle ( $i$ ), eccentricity ( $e$ ), and argument of periastron ( $\omega$ ). Along with the period ( $P$ ) and an arbitrary zero of time, these are most of the so-called

Keplerian elements of an orbit. Figures 5 and 6 in Chapter 2 of this volume define these orientational and orbital parameters. In the plane of the orbit, the angle between the planet and the periastron/periapse (point of closest approach to the star) at the star is  $\theta$ . In celestial mechanics,  $\theta$  is the so-called "true anomaly." For an edge-on orbit ( $i = 90^\circ$ ), and one for which the line of nodes is perpendicular to the line of sight (longitude of the ascending node,  $\Omega$ , equals  $90^\circ$ ) and parallel to the star-periastron line ( $\omega = 0^\circ$ ),  $\theta$  is complementary to  $\alpha$  ( $\alpha = 90^\circ - \theta$ ). As a result,  $\theta = 0^\circ$  at  $\alpha = 90^\circ$  (greatest elongation) and increases with time. Also, for such an edge-on orbit,  $\alpha = 0^\circ$  at superior conjunction. In general,

$$\cos(\alpha) = \sin(\theta + \omega) \sin(i) \sin(\Omega) - \cos(\Omega) \cos(\theta + \omega). \quad (14)$$

Since it is common to define the observing coordinate system such that  $\Omega = 90^\circ$ , we have the simpler formula:

$$\cos(\alpha) = \sin(\theta + \omega) \sin(i). \quad (15)$$

In order to produce a model light curve for a planet orbiting its central star, one must relate the planet's orbital angle ( $\theta$ , the true anomaly), as measured from periapse, to the time ( $t$ ) in the planet's orbit:

$$t(\theta) = \frac{-(1 - e^2)^{1/2} P}{2\pi} \left( \frac{e \sin \theta}{1 + e \cos \theta} - 2(1 - e^2)^{-1/2} \tan^{-1} \left[ \frac{(1 - e^2)^{1/2} \tan(\theta/2)}{1 + e} \right] \right), \quad (16)$$

where  $P$  is the orbital period and  $e$  is the eccentricity. By combining eq. (16) and (15), we derive the exact phase of any orbit at any time.

For a circular orbit,  $R$  is equal to the semi-major axis ( $a$ ). However, a planet in an eccentric orbit can experience significant variation in  $R$ , and, therefore, stellar irradiation (by a factor of  $(\frac{1+e}{1-e})^2$ ). For example, if  $e = 0.3$ , the stellar flux varies by  $\sim 3.5$  along its orbit. For  $e = 0.6$ , this variation is a factor of 16! Such eccentricities are by no means rare in the sample of known EGPs. Therefore, in response to a changing stellar flux it is possible for the composition of an EGP atmosphere to change significantly during its orbit, for clouds to appear and disappear, and for there to be lags in the accommodation of a planet's atmosphere to a varying irradiation regime. Ignoring the latter, eqs. (12) and (14) can be combined with  $\Phi(\alpha)$  and the standard Keplerian formula connecting  $\theta$  and time for an orbit with a given  $P$  and  $e$  to derive an EGP's light curve as a function of wavelength,  $i$ ,  $e$ ,  $\Omega$ ,  $\omega$ , and time. Depending upon orientation and eccentricity, the brightness of an EGP can vary in its orbit not at all (for a face-on EGP in a circular orbit) or quite dramatically (e.g., for highly eccentric orbits at high inclination angles). Since astrometric measurements of stellar wobble induced by EGPs can yield the entire orbit (including inclination), data from the Space Interferometry Mission (SIM) (Unwin & Shao 2000) or Gaia (Perryman 2003) could provide important supplementary data to aid in the interpretation of direct detections of EGPs.

The *spherical albedo* is the fraction of incident light reflected by a sphere at all angles. For a theoretical object with no absorptive opacity, all incident radiation is scattered, resulting in a spherical albedo of unity. The spherical albedo is related to the geometric albedo by  $A_s = qA_g$ , where  $q$  is the *phase integral*:

$$q = 2 \int_0^\pi \Phi(\alpha) \sin \alpha d\alpha. \quad (17)$$

For isotropic surface reflection (Lambert reflection)  $q = \frac{3}{2}$ , while for pure Rayleigh scattering  $q = \frac{4}{3}$ . Although not written explicitly, all of the above quantities are functions of wavelength.

Van de Hulst (1974) derived a solution for the spherical albedo of a planet covered with a semi-infinite homogeneous cloud layer. Given a single-scattering albedo of  $\sigma$  ( $= \sigma_{scat}/\sigma_{total}$ ) and a scattering asymmetry factor of  $g = \langle \cos \theta \rangle$  (the average cosine of the scattering angle), van de Hulst's expression for the spherical albedo of such an atmosphere is

$$A_s \approx \frac{(1 - 0.139s)(1 - s)}{1 + 1.170s}, \quad (18)$$

where

$$s = \left[ \frac{1 - \sigma}{1 - \sigma g} \right]^{1/2}. \quad (19)$$

The Henyey-Greenstein single-scattering phase function,

$$p(\theta) = \frac{1 - g^2}{(1 + g^2 - 2g \cos \theta)^{3/2}}, \quad (20)$$

is frequently used as a fit to the overall scattering phase function, where again  $g = \langle \cos \theta \rangle$ . Other phase functions can be used, but their specific angular dependence has been found to be less important than the value of the integral,  $g$ , itself. In addition, Rayleigh and cloud particle scattering are both likely to result in significant polarization of the reflected light from an EGP (Seager, Whitney, & Sasselov 2000). The degree of polarization will depend strongly on orbital phase angle and wavelength, and can reach many tens of percent. However, polarization may be difficult to measure. To date, there is no credible evidence for polarized light from any EGP. The degree of polarization in the optical and UV is expected to be largest.

The important *Bond albedo*,  $A_B$ , is the ratio of the total reflected and total incident powers. It is obtained by weighting the spherical albedo by the spectrum of the illuminating source and integrating over all wavelengths:

$$A_B = \frac{\int_0^\infty A_{s,\lambda} I_{inc,\lambda} d\lambda}{\int_0^\infty I_{inc,\lambda} d\lambda}, \quad (21)$$

where the  $\lambda$  subscript signifies that the incident intensity varies with wavelength.

With the Bond albedo, one can make a crude estimate of the "effective temperature" of the planet's emission component in response to irradiation. Under the assumption that

the incident total power is equal to the emitted power, one derives:

$$T_{\text{eff}} = T_* \left( \frac{fR_*}{a} \right)^{1/2} (1 - A_B)^{1/4}, \quad (22)$$

where  $T_*$  is the stellar effective temperature,  $a$  is the orbital distance,  $R_*$  is the stellar radius, and  $f$  is a measure of the degree of heat redistribution around the planet. It is equal to 1/4 if the reradiation is isotropic, and 1/2 if the planet reemits only on the day side and uniformly. Note that  $T_{\text{eff}}$  is independent of the planet's radius.

Eq. (22) is useful in estimating the temperatures achieved by radiating planets, but has conceptual limitations. First, it presumes that the planet is not self-luminous and radiating the residual heat of formation in its core. This assumption is not true for young and/or massive EGPs. It is not true of Jupiter. Second, it encourages the notion that the reflection and emission peaks are well-separated. This is not correct for the hot Jupiters, for which the two components overlap and merge. Third, in radiative transfer theory and equilibrium, the true flux from a planet is the *net* flux. Without internal heat sources, this is *zero* for irradiated planets. Finally, eq. (22) is often used to determine the temperature of an atmosphere. However, EGP atmospheres have temperature *profiles*. In their radiative zones the temperatures can vary by factors of  $\sim 3$ , as can the effective photospheric temperatures in the near- and mid-IR. Hence, one should employ eq. (22) to obtain atmospheric temperatures only when very approximate numbers are desired. Importantly, calculating the irradiated planet's spectrum with a  $T_{\text{eff}}$  derived using eq. (22) results in large errors across the entire wavelength range that can severely compromise the interpretation of data.

## 2.5 The Transit Radius

A transiting planet reveals its radius ( $R_p$ ) by the magnitude of the diminution in the stellar light during the planet's traverse of the stellar disk. This is the primary eclipse. In fact, it is the ratio of the planet and star radii that is most directly measured, so a knowledge of the star's radius is central to extracting this important quantity. With a radius and a mass (for transiting planets, the inclination must be near 90° and the inclination degeneracy is broken), we can compare with theories of the planet's physical structure and evolution. However, since the effective edge of the planetary disk is determined by the opacity of the atmosphere at the wavelength of observation, the radius of a gas giant is wavelength-dependent. Importantly, the variation with wavelength of the measured radius can serve as an ersatz atmospheric "spectrum." From this spectrum, one can determine the atmosphere's constituent atoms and molecules. Specifically, the apparent radius is larger at wavelengths for which the opacity is larger and smaller at wavelengths for which the opacity is smaller. For example, the planet should be larger in the sodium D line at  $\sim 5890 \text{ \AA}$  (as in fact

was found for HD 209245b) than just outside it. It should be larger near the absorption peaks of the water spectrum for those planets with atmospheric water than in the corresponding troughs.

However, the “transit radius” is not the same as the classical photospheric radius of an atmosphere. The latter is determined by the depth in the atmosphere where  $\tau_\nu = 2/3$  in the *radial* direction. The transit radius is where this same condition obtains along the *chord* from the star, perpendicular to the radius to the center. At the spherical radius where a light beam experiences  $\tau_\nu = 2/3$ ,  $\tau_\nu$  along the chord can be much larger. Therefore, to achieve the  $\tau_\nu = 2/3$  condition along the chord pushes the transit radius (also referred to as an “impact parameter”) to larger values. It is only at this greater altitude and lower pressure that the chord optical depth is  $\sim 2/3$ . An important difference between the transit radius spectrum and the actual “emission” spectrum from a classical photosphere (such as is relevant at secondary eclipse) is that in the latter case, if the atmosphere were isothermal the spectrum would be a black body and there would be no composition information. However, the transit radius spectrum always manifests the wavelength dependence of the opacities of its atmospheric constituents, even if the atmosphere were isothermal. This difference can be exploited to maximize the scientific return from the study of a given transiting EGP. In sum, if the atmosphere is extended and if the monochromatic opacity at the measurement wavelength is large, the transit radius and the photosphere radius can be rather different and the distinction should always be kept in mind.

A difficulty in interpreting transit radius spectra is that one is probing the planetary limb, the terminator. This means that when comparing with data models must incorporate profiles on both the day side and night side, and at both the equator and poles. In particular the day side and the night side can be at different temperatures and have different compositions. This complication is not always appreciated.

One can estimate the magnitude of the excess of the transit radius over the photospheric radius using a simple exponential atmosphere (see also Fortney 2005). The wavelength-dependent optical depth,  $\tau_{\text{chord}}$ , along a chord followed by the stellar beam through the planet’s upper atmosphere, is approximately:

$$\tau_{\text{chord}} \sim \kappa \rho_{ph} H \sqrt{\frac{2\pi R_p}{H}} e^{-\left(\frac{\Delta R_{ch}}{H}\right)}, \quad (23)$$

where  $\kappa$  is the wavelength-dependent opacity,  $\rho_{ph}$  is the mass density at the photosphere,  $\Delta R_{ch}$  is the excess radius over and above the  $\tau_{ph} = \frac{2}{3}$  radius (the radius of the traditional photosphere), and  $H$  is the atmospheric density scale height. The latter is given approximately by  $kT/\mu gm_p$ , where  $\mu$  is the mean molecular weight,  $g$  is the surface gravity,  $T$  is some representative atmospheric temperature, and  $m_p$  is the proton mass. By definition, and assuming an exponential atmosphere,  $\tau_{ph} = \kappa \rho_{ph} H = \frac{2}{3}$ . For  $\tau_{\text{chord}}$  to equal

$\frac{2}{3}$ , this yields

$$\Delta R_{ch} = H \ln \sqrt{\frac{2\pi R_p}{H}} \sim 5 H. \quad (24)$$

This excess can be from  $\sim 1\%$  to  $\sim 10\%$ , depending upon the wavelength, temperature, gravity, and deviations from a strictly exponential profile. It is smallest for high-gravity planets at larger orbital distances, whereas in the UV near Lyman- $\alpha$ , and with a planetary wind, this excess for HD 209458b is measured to be a factor of 2–3.

At times, the transit radius spectrum is called the “transmission spectrum.” Since what is measured is the effective area of the planet, not the spectrum of light transmitted through the planetary limb, this is a slight misnomer. One is measuring the atmospheric edge position (relative to some zero-point) as a function of wavelength, and not the light transmitted through the finite extent of the atmosphere. To properly do the latter would require a resolved image of the planet that distinguishes the atmosphere from the opaque central planetary disk. Note also that when the atmospheric opacity is low (and, hence, light is more easily “transmitted”), the dip in the stellar flux (what is actually measured) is smaller, not larger. Nevertheless, this rather pedantic point does not inhibit one from profiting from “transmission spectrum” measurements.

## 2.6 Analytic Model for the Temperature Profile of an Irradiated Planet

One can derive a model for the temperature profile of an irradiated EGP atmosphere that is a generalization of the classical Milne problem for an isolated atmosphere. This model can incorporate the difference between the opacity to the insulating (“optical”) and emitting (“infrared”) radiation streams, contains a theory for stratospheres and thermal inversions, and a condition for their emergence. The mathematical development of this analytic theory is taken from Hubeny, Burrows, & Sudarsky (2003), to which the reader is referred for further details. The paper by Chevalier, Pelkowski, & Rutily (2007) is also of some considerable utility.

The equation of hydrostatic equilibrium is fundamental in atmospheric theory, and obtains as long as the Mach number of the gas is low. It can be written:

$$\begin{aligned} \frac{dP}{dz} &= -g\rho \\ \frac{dP}{dm} &= g, \end{aligned} \quad (25)$$

where  $P$  is the pressure,  $g$  is the acceleration due to gravity (generally assumed constant),  $\rho$  is the mass density,  $z$  is the altitude, and  $m$  is the areal (column) mass density defined by  $dm = -\rho dz$ . Note that for a constant  $g$ , the pressure and the column mass are directly proportional.

If the atmosphere is convective, the temperature gradient follows an adiabat and is given by:

$$\frac{d \ln T}{d \ln P} = C_p / R, \quad (26)$$

where  $C_p$  is the specific heat at constant pressure and  $R$  is the gas constant. Given the temperature and pressure at any point in the convective region, together with the specific heat (which can be determined using the composition), the temperature at any atmospheric pressure can be determined. With that knowledge, eq. (26) can then be used to determine the altitude scale. Hence, the combination of the equation of hydrostatic equilibrium and eq. (26) can be used to determine the adiabatic lapse rate for a given specific heat, pressure, and temperature.

However, for most of a strongly irradiated atmosphere, and in radiative zones in general, radiation carries the energy flux. The radiative transfer equation is written as

$$\mu \frac{dI_{\nu\mu}}{dm} = \chi_\nu (I_{\nu\mu} - S_\nu), \quad (27)$$

where  $I_{\nu\mu}$  is the specific intensity of radiation as a function of frequency,  $\nu$ , angle  $\mu$  (the cosine of the angle of propagation with respect to the normal to the surface), and the geometrical coordinate, taken here as the column (areal) mass  $m$ . The monochromatic optical depth is defined as  $d\tau_\nu = \chi_\nu dm$ .

$S_\nu$  is the source function, given in LTE by

$$S_\nu = \frac{\kappa_\nu}{\chi_\nu} B_\nu + \frac{\sigma_\nu}{\chi_\nu} J_\nu. \quad (28)$$

Here  $\kappa_\nu$  is the true absorption coefficient,  $\sigma_\nu$  is the scattering coefficient,  $B_\nu$  is the black body function,  $J_\nu$  is the zeroth angular moment of the specific intensity, and  $\chi_\nu = \kappa_\nu + \sigma_\nu$  is the total absorption coefficient. The zeroth moment is equal to the radiation energy density, divided by  $4\pi$ . All coefficients are per unit mass.

The first moment of the transfer equation is written

$$\frac{dH_\nu}{dm} = \chi_\nu (J_\nu - S_\nu), \quad (29)$$

which can be rewritten, using equation (28) as

$$\frac{dH_\nu}{dm} = \kappa_\nu (J_\nu - B_\nu). \quad (30)$$

$H_\nu$  is the first angular moment of the specific intensity and is equal to the radiation flux, divided by  $4\pi$ . Integrating over frequency one obtains

$$\frac{dH}{dm} = \kappa_J J - \kappa_B B, \quad (31)$$

where  $\kappa_J$  and  $\kappa_B$  are the absorption and Planck mean opacities, respectively, defined by

$$\kappa_J = \frac{\int_0^\infty \kappa_\nu J_\nu d\nu}{\int_0^\infty J_\nu d\nu}, \quad (32)$$

and

$$\kappa_B = \frac{\int_0^\infty \kappa_\nu B_\nu d\nu}{\int_0^\infty B_\nu d\nu}. \quad (33)$$

These two opacities are often assumed to be equal. However, one should distinguish them here because the difference between  $\kappa_J$  and  $\kappa_B$  turns out to be crucial in the case of strongly irradiated atmospheres.

The second moment of the transfer equation is

$$\frac{dK_\nu}{dm} = \chi_\nu H_\nu, \quad (34)$$

and integrating over frequency one obtains

$$\frac{dK}{dm} = \chi_H H, \quad (35)$$

where

$$\chi_H = \frac{\int_0^\infty \chi_\nu H_\nu d\nu}{\int_0^\infty H_\nu d\nu} \quad (36)$$

which is referred to as the flux mean opacity.

Finally, the radiative equilibrium equation is written as

$$\int_0^\infty \kappa_\nu (J_\nu - B_\nu) d\nu = 0. \quad (37)$$

Using the above mean opacities, this can be rewritten

$$\kappa_J J - \kappa_B B = 0. \quad (38)$$

Substituting (38) into (31), one obtains another form of the radiative equilibrium equation,

$$\frac{dH}{dm} = 0, \quad \text{or} \quad H = \text{const} \equiv (\sigma/4\pi) T_{\text{eff}}^4, \quad (39)$$

where  $\sigma$  is the Stefan-Boltzmann constant.

From equation (38), one has  $B = (\kappa_J/\kappa_B)J$ , which yields an expression for  $T$  through  $J$  using the well-known relation  $B = \sigma T^4$ . To determine  $J$ , one uses the solution of the second moment of the transfer equation  $K(\tau_H) = H\tau_H = (\sigma/4\pi) T_{\text{eff}}^4 \tau_H$ , where  $\tau_H$  is the optical depth using the flux-mean opacity, and expresses the moment  $K$  through  $J$  by means of the Eddington factor,  $f_K \equiv K/J$ . Similarly, one expresses the surface flux through the second Eddington factor,  $f_H \equiv H(0)/J(0)$  (see also Hubeny 1990):

$$T^4 = \frac{3}{4} T_{\text{eff}}^4 \frac{\kappa_J}{\kappa_B} \left[ \frac{1}{3f_K} \tau_H + \frac{1}{3f_H} \right] + \frac{\kappa_J}{\kappa_B} W T_*^4. \quad (40)$$

where  $W$  is the dilution factor,  $(R_*/a)^2$ . This solution is exact within LTE and is the generalization of the classical Milne atmosphere solution.

The usual LTE-gray model consists in assuming all the mean opacities to be equal to the Rosseland mean opacity. If one adopts the Eddington approximation ( $f_K = 1/3$ ;  $f_H = 1/\sqrt{3}$ ), then one obtains a simple expression

$$T^4 = \frac{3}{4} T_{\text{eff}}^4 \left( \tau + 1/\sqrt{3} \right) + W T_*^4. \quad (41)$$

We will consider the most interesting case, namely strong irradiation, defined by  $W T_*^4 \gg T_{\text{eff}}^4$ . In this case, the



second term in the brackets is negligible, and one may define a *penetration depth* as the optical depth where the usual thermal part ( $\propto T_{\text{eff}}^4$ ) and the irradiation part ( $\propto WT_*^4$ ) are nearly equal, to wit

$$\tau_{\text{pen}} = W \left( \frac{T_*}{T_{\text{eff}}} \right)^4. \quad (42)$$

The behavior of the local temperature in the case of a strict gray model is very simple – it is essentially constant,  $T = T_0 \equiv W^{1/4}T_*$  for  $\tau < \tau_{\text{pen}}$ , and follows the usual distribution  $T \propto \tau^{1/4}T_{\text{eff}}$  in deep layers,  $\tau > \tau_{\text{pen}}$ . In the general case, one has to retain the ratio of the absorption and Planck mean (assuming still that the flux mean opacity is well approximated by the Rosseland mean). In the irradiation-dominated layers ( $\tau < \tau_{\text{pen}}$ ), the temperature is given by

$$T = \gamma W^{1/4} T_*, \quad (43)$$

where

$$\gamma \equiv (\kappa_J/\kappa_B)^{1/4}. \quad (44)$$

$\gamma$  is approximately 1 for no or weakly irradiated atmospheres. However, in the case of strong irradiation,  $\gamma$  may differ significantly from unity. Moreover, it may be a strong function of temperature, and, to a lesser extent, of density. This is easily seen by noting that in optically-thin regions, the local mean intensity is essentially equal to twice the irradiation intensity, since the incoming intensity is equal to irradiation intensity, and the outgoing intensity is roughly equal to it as well. The reason is that in order to conserve the total flux when it is much smaller than the partial flux in the inward or outward direction, both fluxes should be almost equal, and so too must the individual specific and mean intensities.

The local temperature in the upper layers is given, using equation (43), as

$$T/T_0 = \gamma(T). \quad (45)$$

It is clear that if  $\gamma$  exhibits a strongly non-monotonic behavior in the vicinity of  $T_0$ , for instance if it has a pronounced minimum or maximum there, equation (45) may have two or even more solutions.

This is the origin of thermal inversions, when they occur, in the atmospheres of strongly irradiated EGPs (Hubeny, Burrows, & Sudarsky 2003). The essential element is the differential absorption in the optical on the one hand (since this is where most of the irradiating stellar light is found), and in the infrared (since this is where most of the emission at the temperatures achieved in the atmospheres of hot Jupiters occurs). As the above formalism makes plain, an inversion is not possible for gray opacities, whatever the degree of irradiation. For strongly irradiated EGPs, if there is not a strong optical absorber at altitude, then stellar optical light is absorbed rather deeply in the atmosphere, near pressures of  $\sim 1$  bar. This is near and interior to the corresponding emission photospheres in the near-IR. The result is a more-or-less monotonic decrease of temperature with altitude and decreasing pressure. However, if there is a strong

optical absorber at altitude, the large value of  $\gamma$  will allow another solution to eq. (45) for which there is an inversion. The resulting higher temperatures in the upper atmosphere will result in higher fluxes in the mid-IR, e.g. in the IRAC and MIPS bands of *Spitzer* where their photospheres reside. We see signatures of such inversions in the measured spectra of many transiting EGPs, such as HD 209458b, XO-1, TrES-4, and HD 149026b. However, to date we do not know what chemical species is absorbing at altitude in the optical (see §4.3).

### 3. LESSONS FROM JUPITER AND SATURN

Jupiter and Saturn are the largest planets in our solar system and serve as initial paradigms for the atmospheres of EGPs. With the largest exoplanets invariably referred to as “super-Jupiters,” it is instructive to start with an assessment of the properties of “regular Jupiters.” Both Jupiter and Saturn have been studied with a variety of remote-sensing techniques across a wide spectral range, and these approaches have provided sufficient information to determine physical and chemical properties and their variation in both time and space. In the case of Jupiter, these physical and chemical properties have been bolstered by *in situ* observations made by the Galileo mission atmospheric probe which both extended and served as a measure of ground truth for remote-sensing observations. This subsection will concentrate on properties of their atmospheres and the spectra of their upwelling fluxes in order to provide analogies with extrasolar planets which can boast fewer observational constraints.

Observations of Jupiter and Saturn have been made in some detail from the time of Galileo, with serious ground-based observations taking place with the advent of photographic film and spectroscopy. In the second half of the 20th century, NASA spacecraft ventured to both - first with the Pioneers 10 (Jupiter) and 11 (Jupiter and Saturn) flyby spacecraft. Later observations were made with more instrumentation (including an infrared spectrometer, and wide- and narrow-angle cameras) by Voyagers 1 and 2, which visited both planets, and provided an abundance of information on the dynamics, structure, and composition of both Jupiter and Saturn. The Galileo spacecraft orbited Jupiter and determined more about the dynamics of individual regions on the planet and dropped a direct probe into its atmosphere. Most recently, the Cassini spacecraft obtained substantial information on the atmosphere, flying by Jupiter in a gravity assist on its way to Saturn, which it began orbiting in 2005. Most recently the New Horizons spacecraft flew by Jupiter on its way to Pluto, collecting information on Jupiter’s clouds.

These spacecraft observations were complemented by observations from Earth-orbiting platforms beginning with observations of auroral emission from Jupiter by the International Ultraviolet Explorer (IUE). They include ultraviolet through near-infrared imaging and spectroscopy by the instrument complement on board the Hubble Space Telescope (HST), disk-averaged spectroscopy by ESA’s In-

frared Space Observatory (ISO), and even X-ray observations by the Chandra Observatory. Additional spectroscopic and occultation observations were made using instruments on board NASA’s Kuiper Airborne Observatory (KAO).

The ever-improving competence of ground-based observational facilities has substantially increased our knowledge of these atmospheres. In particular, increasing spatial and spectral discrimination became available with larger primary mirrors (minimizing diffraction-limited spatial resolution) and a variety of active optical systems, which have been extremely effective in reducing the blurring due to atmospheric turbulence. These have been accompanied at the smaller-telescope end by a host of amateur Jupiter watchers wielding increasingly sophisticated instrumentation, including multi-filtered CCD cameras.

### 3.1 Spectra

Models for the structure of the atmospheres of Jupiter and Saturn can be understood in terms of the various regions in which energy transfer is by either radiation or convection, similar to stellar atmospheres. To good accuracy, much of the atmospheres of both planets can be approximated as self-gravitating fluids in hydrostatic equilibrium. At depth, the atmospheres of both Jupiter and Saturn are dominated by convective processes, and gases rise and fall at rates faster than they can radiate away energy. Thus, adiabatic conditions hold (eq. 26).

It is important to note the “principal players” in radiative transfer in Jupiter and Saturn. In the visible and near infrared, the spectrum is dominated by  $\text{CH}_4$  (methane) absorption, with some additional opacity from the  $\text{H}_2$ - $\text{H}_2$  collision-induced fundamental and  $\text{H}_2$  quadrupole lines at higher resolution Figure 5 depicts the near-infrared spectrum of Jupiter from 1 to 6 microns. For Jupiter, the  $5\text{-}\mu\text{m}$  spectrum is not dominated by reflected sunlight, as is the case at the shorter wavelengths, but by thermal emission from depth, as the result of a dearth of gaseous absorption in this region. It is this atmospheric “window” which allows glimpses of Jupiter’s composition down to a few bars of pressure, where  $\text{H}_2\text{O}$  vapor was first detected in Jupiter’s atmosphere from observations using NASA’s Kuiper Airborne Observatory, and where high-resolution spectroscopy detected  $\text{PH}_3$  and trace constituents such as  $\text{AsH}_3$  (arsine) and  $\text{CO}$  (carbon monoxide) at depth. For colder Saturn, more of this spectral window is composed of reflected sunlight.

At longer wavelengths, in the middle and far infrared, the spectrum is dominated by thermal emission. Figure 6 shows the brightness temperature spectrum of both Jupiter and Saturn. Rather than flux, these spectra are plotted in brightness temperature, which is defined as the temperature that a blackbody source would need to emit at a particular wavelength in order to match the observed flux.

Plotting a spectrum in brightness temperature rather than directly in flux is a convenient way to display a spectrum over a broad range, such as the ones in Fig. 6, because

the flux varies over several orders of magnitude. In addition, plotting the brightness temperature provides a quick way to estimate the depth in the atmosphere from which most of the radiation emerges. For example, the source of a strong emission feature with a high brightness temperature is likely to be emerging from molecular emission very high in the hot stratospheres of either planet. More details can be found in dePater and Lissauer (2004), Irwin (2003), or Goody and Yung (1989).

We also note that Fig. 6 plots its primary spectral scale in  $\text{cm}^{-1}$  (“wavenumbers”) rather than wavelength. Historically, this is the result of such spectra being derived from Fourier-transform spectrometers, where inverse of the path length difference of a Michelson-like interferometer is the native spectral unit. A wavenumber ( $\text{cm}^{-1}$ ) is equal to the frequency of the radiation in Hertz ( $\text{sec}^{-1}$ ) divided by 29.97. Because the frequency or wavenumber is proportional to quantum energy, such a plot enables molecular lines to be displayed in a manner proportional to the transition energy. The result is often (but not always!) a regular series of line transitions (or groups of line transitions known as manifolds). Some of these are evident in Fig. 6 in the far infrared for  $\text{NH}_3$  (ammonia) or  $\text{PH}_3$  (phosphine) or near  $10\ \mu\text{m}$  for  $\text{NH}_3$ .

Figure 6 shows that the far infrared, where the bulk of Jupiter’s and Saturn’s flux emerges, is controlled by the collision-induced absorption of  $\text{H}_2$  which varies so slowly that it constitutes a virtual continuum opacity source. Two broad rotational lines are evident, and the far-infrared lines of  $\text{NH}_3$  in Jupiter and  $\text{PH}_3$  in Saturn show up as absorption features on the long-wavelength “translational” component of the  $\text{H}_2$  absorption. When helium collides with  $\text{H}_2$ , a slightly different spectrum is created than for pure  $\text{H}_2$ - $\text{H}_2$  absorption, and the translation component is stronger. Fitting this shape accurately provides a means to determine the ratio of He (helium) to  $\text{H}_2$  in these planets. This part of the spectrum also allows one to determine the ratio of ortho- $\text{H}_2$ , where the spins of the hydrogen atoms are parallel, to para- $\text{H}_2$ , where the spins are antiparallel (parallel but pointed in opposite directions), because para- $\text{H}_2$  alone is responsible for all even rotational transitions, such as S(0) and ortho- $\text{H}_2$  alone is responsible for all odd rotational transitions, such as S(1). In a quiescent atmosphere, there is an equilibrium between these two species of  $\text{H}_2$  which is purely a function of temperature and how their energy levels are populated. In reality, however (particularly in Jupiter)  $\text{H}_2$  gas can be transported vertically much faster than this temperature re-equilibration can take place, and the para-ortho  $\text{H}_2$  ratio varies across the face of the planet. This is useful as an indirect means to track upwelling and downwelling winds. For example, a para- $\text{H}_2$  value which is lower than the value expected from local thermal equilibrium, but greater than 0.25, would indicate rapid upwelling from the deep, warm atmosphere where its value is close to the high-temperature asymptotic value of 25%. However, at the high temperatures of hot-Jupiter atmospheres, transiting or otherwise, para- and ortho-hydrogen are in thermal and statistical equi-

librium.

The spectra of Jupiter and Saturn are also filled with discrete transitions, such as the rotational lines of  $\text{NH}_3$  and  $\text{PH}_3$  in the far infrared. Lines arising from a combination of vibrational and rotational quantum transitions can be identified easily in the mid-infrared. Both planets display emission features arising from  $\text{CH}_4$  (methane) and from higher-order hydrocarbons, such as  $\text{C}_2\text{H}_2$  (acetylene) and  $\text{C}_2\text{H}_6$  (ethane) which are by-products of the photolysis of methane by ultraviolet radiation in the upper atmosphere. They appear in emission rather than absorption because the stratospheres of both planets are substantially warmer than the upper troposphere. This is the result of warming by sunlight absorbed in the near infrared by  $\text{CH}_4$  and small atmospheric particulates.  $\text{NH}_3$  and  $\text{PH}_3$  can also be seen as components of the mid-infrared spectrum; their lines are in absorption because they are most abundant in the troposphere. In fact, ammonia is a condensate - much like water vapor in the Earth's atmosphere. It does not appear as strongly in Saturn's spectrum because Saturn is colder than Jupiter, and ammonia condenses out deeper in the atmosphere than in Jupiter and is at the limits of detectability above the  $\text{H}_2$  collision-induced continuum.  $\text{PH}_3$  lines are, in fact, also detectable in Jupiter's spectrum, but are more difficult to discern among the forest of  $\text{NH}_3$  lines in Fig. 6.

The existence of absorption and emission features from  $\text{H}_2$  and  $\text{CH}_4$  in the thermal spectrum is also useful for determining temperatures. Both molecules are well mixed in the atmosphere, so any changes which take place in their emission from point to point can be attributed to changes of temperature rather than abundance. There are techniques for inverting the radiative-transfer equations for the emitted flux, given observations of thermal emission in regions dominated by  $\text{H}_2$  or  $\text{CH}_4$  which allow temperatures to be determined (some authors say "retrieved") as a function of altitude. For the  $\text{H}_2$  absorption features, the relevant range is in the upper troposphere - around  $\sim 100\text{--}400$  mbar ( $\sim 0.1\text{--}0.4$  bars) in atmospheric pressure. For  $\text{CH}_4$  emission, the relevant range is the stratosphere at pressures less than  $\sim 100$  mbar.

Details about molecular transitions in planetary atmospheres can be found in Goody and Yung (1989) and Irwin (2004). Irwin (2004) also discuss in some detail the techniques for retrieving atmospheric temperatures in the giant planets.

### 3.2 Clouds

The visual appearances of Jupiter and Saturn are strongly affected by clouds. Jupiter's visible atmosphere is famously heterogeneous, and cloud motions and colors have been studied for decades. An extensive review of historical and amateur images is given by Rogers (1995). Because light reflected from a generally homogeneous upper-atmospheric haze layer Voyager and Cassini imaging observations of Jupiter's and Saturn's cloud fields to determine wind velocities confirmed and greatly refined ground-based stud-

ies which showed variable zonal (east-west) winds that are variable with latitude, but generally constant in time. Jupiter's wind vectors are both prograde and retrograde with respect to the rotation of the deep interior, ranging from a maximum near 140 m/sec and a minimum near -50 m/sec. Doppler tracking of the Galileo probe suggests that these zonal winds persist into the atmosphere at least as deep as the 20-bar pressure level. Saturn's winds display a strong jet of higher speeds, reaching 500 m/sec near the equator. A drop of Saturn's maximum jet speed has been detected in comparing HST-derived winds with those derived by Voyager imaging, but it is not clear whether this is due to a real change in the wind speed itself or a change of the altitude of the cloud particles being tracked. Meridional (north-south) winds are much smaller and only notable around large, discrete features such as Jupiter's Great Red Spot or smaller vortices. Jupiter's largest and longest-lived vortices are all anticyclonic (rotating counterclockwise in the southern hemisphere, clockwise in the northern hemisphere). Cyclonic storms are also evident and Galileo observations noted that they are often the source locations for observable lightning; however, their lifetimes are generally measured in weeks rather than months to years.

At near-infrared wavelengths, the dominance of gaseous absorption by  $\text{CH}_4$  and some  $\text{H}_2$  allows tracking of higher-altitude clouds and hazes. Imaging through wavelengths that sample particulates at various levels provides a means of shaping a 3-dimensional picture of cloud systems. Stratospheric hazes can be seen at high latitudes which are thought to be products of charged-neutral interactions in Jupiter's polar auroral regions. Images of near-infrared reflectivity in Saturn have an overall banded structure which is similar to Jupiter's, but Saturn seldom shows individual discrete features at these wavelengths that are large enough to be detected from the Earth.

The  $5\text{-}\mu\text{m}$  "spectral windows" for Jupiter and Saturn provide insight into their cloud systems at several bars of atmospheric pressure. The lack of substantial gaseous absorption allows cloud tops to be sensed, and thermal emission begins to dominate most of the  $4.8\text{--}5.3\ \mu\text{m}$  region for Jupiter and the  $5.0\text{--}5.3\ \mu\text{m}$  region for Saturn. Analogous to the visible region, Jupiter's  $5\text{-}\mu\text{m}$  appearance is spectacularly heterogeneous (Fig. 7), with some regions of the atmosphere nicknamed " $5\text{-}\mu\text{m}$  hot spots" ostensibly cloudless down to deep (5 bars atmospheric pressure) and warm (275 K) cloud-top levels. These are mixed with regions of both intermediate and cold clouds across the face of the disk. The warmer regions are highly correlated with areas of darker color in the visible, and the hot spots are correlated with gray areas. This implies that the lighter colored clouds represent an upper layer of tropospheric clouds with particles thick enough to be optically thick at wavelengths near  $5\ \mu\text{m}$ . Such clouds could be related to an ammonia ice condensate ("cirrus") cloud near 1 bar to 500 mbar in pressure, but spectral signatures of ammonia ice have only been seen in particulates undergoing rapid upwelling or regions of turbulent flow to the northwest of the Great Red

Spot. This requires that ammonia condensate to be (i) riming nucleation sites made of other materials or (ii) particles covered by a coating of other material. The morphology of these clouds can also be used to diagnose upwelling and downwelling motions, just as the para- $\text{H}_2$  distribution discussed earlier. Upwelling gas is wet and capable of forming clouds, but - after reaching dryer and colder altitudes - the condensate has precipitated out and downwelling regions will generally be cloudless because of the dry nature of the gas. Thus the relatively cold  $5\text{-}\mu\text{m}$  interior of the Great Red Spot (near the center of Fig. 7) diagnoses a region of upwelling, and its ostensibly warm (actually less cloudy) periphery indicates regions of downwelling.

Saturn's thermal emission at  $\sim 5\ \mu\text{m}$  reveals a cloud structure in the several-bar pressure region every bit as heterogeneous as Jupiter's, although one might say it is a negative version. A series of warm zonal bands are interlaced with a cold bands, and discrete regions are dominated not by clear, warm areas as in Jupiter's atmosphere but by cloudy, cold ones. Cassini VIMS observations of this region are similar, but take advantage of the entire spectral window by observing only thermal emission on Saturn's night side. The persistence of some cloud features that are detectable in the visible can also be found in this spectral region, an indicator that the dynamics creating them persists over a wide vertical range. For example an irregular band near high northern latitudes known as the "polar hexagon" attests to the presence of meridional waves which perturb the normally uniform zonal flow, and the combination of visible, near-infrared,  $5\text{-}\mu\text{m}$ , and mid-infrared observations shows that this feature persists in both the cloud and thermal fields from atmospheric pressures less than  $\sim 100$  mbar down to levels with pressures of several bars.

### 3.3 Temperatures

Temperatures in the atmospheres of Jupiter and Saturn can be determined using several different techniques. For individual locations, occultations of optical light from stars by the atmosphere has been used to determine atmospheric density as a function of altitude and then transformed into temperatures and pressures using the ideal gas law, together with the equation of hydrostatic equilibrium and an estimate of the mean molecular weight. A similar approach has been successful using occultations by the atmosphere of coherent spacecraft signals in the radio.

One such result for a Voyager spacecraft radio occultation is shown in Fig. 8 for Saturn, but the Galileo probe at Jupiter provided the most direct measurement of temperatures available for the giant planets (Fig. 8), with direct measurements consistent with a "dry" adiabat (i.e., one without perturbations to the lapse rate from exchanges of latent heat from condensing molecules) from  $\sim 400$  mbar to  $\sim 20$  bars (thick, asterisked curve in Fig. 8). At higher levels, before the entry velocity of the probe became subsonic, the deceleration of the probe was Doppler tracked, the density of impeding gas determined, and knowledge of

the mean molecular weight was used to determine the temperature profile of Jupiter at that location in the stratosphere (regular asterisked curve in Fig. 8). This profile showed the presence of substantial vertical thermal waves in the stratosphere, which should provide an substantial additional source of mechanical energy for the upper stratosphere.

The most successful approach for mapping temperatures across the disk is to invert observations of thermal emission in spectral regions dominated by well-mixed constituents. As described earlier, spectral regions dominated by collision-induced absorption by well-mixed  $\text{H}_2$  and the  $7\text{-}\mu\text{m}$  band of  $\text{CH}_4$  (Fig. 6) are used in both planets to map temperatures. Fig. 8 contains temperatures derived using this technique by the Cassini Composite Infrared Spectrometer (CIRS) instrument for Jupiter and Saturn near the equator and for latitudes of  $\pm 30^\circ$ . This approach has a vertical resolution no better than a scale height, and so it acts as a low-pass filter for temperature variability with altitude. Nonetheless, it provides a good means to derive a range of temperatures over time and space, similar to instrumentation in weather satellites orbiting the Earth. The technique has been expanded from spacecraft spectroscopy to a series of middle-infrared filtered images of Jupiter and Saturn, which provide similar temperature information over a wide horizontal range without as much vertical information overlap. This has provided a means for ground-based observations to supplement the close-up coverage provided by spacecraft, with spatial resolutions that have often been as good as those available from spacecraft instruments with the deployment of mid-infrared imaging instruments on 8-meter or larger-class telescopes which minimize the effects of blurring by diffraction. The entire host of temperature information verifies that the atmosphere is indeed separable into largely convective versus largely radiative regions, with the convective regions over a variety of different latitudes and bands converging at depth in both planets (Fig. 8).

### 3.4 Compositions

Over 99.9% of the composition of both planets by volume consists of hydrogen, helium and methane. A summary of our current knowledge of the compositions of Jupiter and Saturn in the detectable part of the atmosphere is given in Table 1. Their relative abundances, particularly the  $\text{He}/\text{H}_2$  ratio, are important constraints on models of their formation, evolution and interiors. For Jupiter, the value shown in Table 1 is the one derived independently by the Galileo Probe Mass Spectrometer (GPMS) and a purpose-built Helium Abundance Detector (HAD). The measured value for the He abundance may be influenced by its ability to form droplets at high pressure and "rain out" of the deep atmosphere toward the center of the planet. Neon (Ne) is soluble in the He drops and appears to be severely depleted in Jupiter with respect to solar abundances. The abundances of Ar (argon), Kr (krypton) and Xe (xenon) determined by the GPMS are all enhanced by  $\sim 2.6$  with respect to solar

values.

CH<sub>4</sub> is present throughout the atmosphere because it represents the simplest stable form of carbon, originally delivered to the planet as methane or other carbon-bearing ices in planetestimals. This is also true of NH<sub>3</sub> for N, H<sub>2</sub>O for O, and possibly PH<sub>3</sub> for P, and H<sub>2</sub>S for S. Ammonia and water both condense out in the detectable parts of Jupiter's and Saturn's atmospheres; both are responsible for at least part of the atmospheric opacity in the submillimeter through microwave part of the spectrum and, with phosphine, in the 5- $\mu$  spectral window. The measurement of O/H via the Galileo GPMS value is considered to be too low because the Galileo probe descended in a 5- $\mu$ m "hot spot," that also proved to be a region of unusual dessication. Chemical equilibrium models predict that H<sub>2</sub>S should react with NH<sub>3</sub> to form NH<sub>4</sub>SH (ammonium hydrosulfate) clouds around  $\sim 1-3$  bars pressure (between the upper NH<sub>3</sub> cloud and the deeper H<sub>2</sub>O cloud layers. Molecules in chemical disequilibrium at the cold upper tropospheric temperatures such as PH<sub>3</sub> and GeH<sub>4</sub> (germane) are present because upwelling from warmer depths takes place more rapidly than molecular decomposition.

Methane is present in the stratosphere and is destroyed by solar ultraviolet radiation, with higher-order hydrocarbons resulting from the chemical recombination process. The most abundant of these are C<sub>2</sub>H<sub>2</sub> (acetylene), C<sub>2</sub>H<sub>4</sub> (ethylene), and C<sub>2</sub>H<sub>6</sub> (ethane), which act as the principal means for stratospheric radiative cooling. Enhanced abundances of hydrocarbons have been reported in polar stratospheric "hot spot" regions, the result of additional auroral-related chemistry. Reports of H<sub>2</sub>O line emission attest to the presence of H<sub>2</sub>O in the stratosphere, in abundances suggesting infall from the exterior, either from ring particles or from interplanetary ice.

The isotopic <sup>13</sup>C/<sup>12</sup>C ratio, determined by the Galileo probe for Jupiter and by the Cassini CIRS experiment for Saturn are close to the terrestrial value, suggesting a protosolar value with almost no chemical fractionation of carbon isotopes in either atmosphere. The observed D/H ratios, determined from the same set of experiments, also suggests protosolar values. In the case of Saturn, this is inconsistent with interior models which predict an enhancement of deuterium because of the larger mass of its core.

In addition to the reviews already mentioned, detailed summaries on several topics concerning Jovian and Saturnian atmospheres, interiors, icy satellites, rings and magnetospheres are given in Bagenal et al. (2004) for Jupiter and Brown et al. (2009) for Saturn.

#### 4. SUMMARY OF EGP FEATURES AND HIGHLIGHTS

Using the formalisms sketched in §2, and the current knowledge of Jovian planet atmospheres summarized in §3, one can establish a theoretical framework in which to study EGPs for any age, orbit, mass, and elemental composition. This theoretical edifice is also understood using the simple models provided in §2.4 and §2.6, with which one can

understand most of their measured and anticipated properties. In this section, we highlight a few of the interesting ideas and features that have emerged in the last few years concerning EGP evolution, generic planet/star flux ratios, and the distinctive character of the family of hot Jupiters. This summary is in no way comprehensive, but provides the reader with a snapshot of some of the salient facts and issues in this rapidly evolving field.

#### 4.1 Evolution of EGP Atmospheres and Chemistry

Unlike in a star, EGP atmospheric temperatures are sufficiently low that chemistry is of overriding importance. The atmosphere of a gaseous giant planet is the thin outer layer of molecules that controls its absorption and emission spectra and its cooling rate. Molecular hydrogen (H<sub>2</sub>) is the dominant constituent, followed by helium. An EGP's effective temperature ( $T_{\text{eff}}$ ) can vary from  $\sim 2500$  K at birth for the more massive EGPs or in a steady state for the most severely irradiated to  $\sim 50$  K for the least massive EGPs in wide orbits after evolving for billions of years. This wide range translates into a wide variety of atmospheric constituents that for a given mass and elemental composition can evolve significantly.

Without any significant internal sources of energy, after formation an EGP gradually cools and shrinks. Its rate of cooling can be altered by stellar irradiation, or when old and light by hydrogen/helium phase separation (Fortney & Hubbard 2004). Jupiter itself is still cooling and its total infrared plus optical luminosity is about twice the power absorbed from the Sun. Hence, the temperatures and luminosities achieved are not just functions of mass and composition, but of mass, age, composition, orbital distance, and stellar type.

Since EGPs evolve through atmospheres of various compositions and temperatures, age is a key parameter in their study. A theoretical evolutionary scenario for Jupiter itself can serve to exemplify these transformations. The evolution of other EGPs with different masses and orbits will be different in detail, but for the wide-separation variety not in kind. The description below is based in part on the review by Burrows (2005), to which the reader is referred. Another useful review can be found in Marley et al. (2007).

At birth, Jupiter had a  $T_{\text{eff}}$  near 600-1000 K and the appearance of a T dwarf (Burgasser et al. 2002). It had no ammonia or water clouds and, due to the presence of atomic sodium in its hot atmosphere, had a magenta color in the optical (Burrows et al. 2001). Due to the formation and settling to depth of the refractory silicates that condense in the temperature range  $\sim 1700-2500$  K, its atmosphere was depleted of calcium, aluminum, silicon, iron, and magnesium<sup>2</sup>. Water vapor (steam) was the major molecule containing oxygen, gaseous methane was the major reservoir of carbon, gaseous ammonia and molecular nitrogen were the contexts for nitrogen, and sulfur was found in H<sub>2</sub>S. At

<sup>2</sup>Note that such silicate clouds should exist at depth in the current Jupiter.

lower temperatures ( $< \sim 700\text{K}$ ), FeS would be the equilibrium reservoir of sulfur. However, as noted above, earlier in the planet’s history when refractory species condensed out and settled gravitationally, the atmosphere was left depleted of most metals, including iron. The result of this “rainout” was that the chemistry simplified and sulfur was in the form of  $\text{H}_2\text{S}$ , as is observed in the current Jupiter. The rainout phenomenon of condensates in the gravitational field of EGPs and solar system giants is a universal feature of their atmospheres (Fegley & Lodders 1994; Burrows & Sharp 1999).

As Jupiter cooled, the layer of alkali metals was buried below the photosphere to higher pressures, but gaseous  $\text{H}_2$ ,  $\text{H}_2\text{O}$ ,  $\text{NH}_3$ , and  $\text{CH}_4$  persisted. At a  $T_{\text{eff}}$  of  $\sim 400\text{K}$ , water condensed in the upper atmosphere and water clouds appeared. This occurred within its first 100 million years. Within less than a billion years, when  $T_{\text{eff}}$  reached  $\sim 160\text{K}$ , ammonia clouds emerged on top of the water clouds, and this layering persists to this day (see section 3).

Stellar irradiation retards cloud formation, as does a large EGP mass, which keeps the EGP hotter longer. Proximity to a star also keeps the planet hotter longer, introducing a significant dependence of its chemistry upon orbital distance. Around a G2V star such as the Sun, at 5 Gyr and for an EGP mass of  $1.0 M_J$ , water clouds form at 1.5 AU, and ammonia clouds form beyond 4.5 AU (Burrows, Sudarsky, & Hubeny 2004). Jupiter’s and Saturn’s current effective temperatures are 124.4 K and 95 K, respectively. Jupiter’s orbital distance and age are 5.2 AU and 4.6 Gyr. The orbital distance, mass, and radius of a coeval Saturn are 9.5 AU,  $0.3 M_J$ , and  $0.85 R_J$ . However, as an EGP of whatever mass cools, its atmospheric composition evolves through a similar chemical and condensation sequence. Figure 9 depicts the atmospheric temperature/pressure (T/P) profile for a sequence of  $1-M_J$ , 5-Gyr models as a function of orbital distance (0.2 to 15 AU) from a G2V star. As the EGP’s orbital distance increases, its atmospheric temperature at a given age and pressure decreases. Superposed on the plot are the  $\text{H}_2\text{O}$  and  $\text{NH}_3$  condensation lines. Clearly, a given atmospheric composition and temperature can result from many combinations of orbital distance, planet mass, stellar type, and age. This lends added complexity to the study of EGPs.

The atmospheres of hot Jupiters at orbital distances of  $\sim 0.02\text{-}0.07\text{ AU}$  from a G, F, or K star are heated and maintained at temperatures of  $\sim 1000\text{-}2000\text{ K}$ , roughly independent of planet mass and composition. The transiting EGPs discovered to date are examples of such hot objects. At high temperatures, carbon is generally in the form of carbon monoxide, not methane. As a result of this and the rainout of most metals, EGP atmospheric compositions are predominantly  $\text{H}_2$ , He,  $\text{H}_2\text{O}$ , Na, K, and CO. There are, however, significant day/night differences in composition, temperature, and spectrum that distinguish a hot Jupiter from a lone and isolated planet or star. For instance, on the night side, carbon might be found in methane, whereas on the day side it might be in CO. This suggests that non-equilibrium

chemistry, where the chemical rates and the dynamical motions compete in determining the composition, might be at play. Exotic general circulation models (GCMs) with credible dynamics, radiative transfer, chemistry, and frictional effects will soon be necessary to understand the equatorial currents, jet streams, day/night differences, terminator chemistry, and global wind dynamics of irradiated EGPs, in particular, and of orbiting, rotating EGPs, in general.

There is another interesting aspect to the orbital-distance dependence of EGP properties and behavior. At the distance of Jupiter, the infrared photosphere is close to the radiative-convective boundary, near 0.5 bars. This means that a good fraction of the stellar radiation impinging upon Jupiter from the Sun is absorbed directly in the convective zone, which thereby redistributes this heat more or less uniformly to all latitudes and longitudes of the planet. The upshot of this, and that the luminosity from the core due to the remaining residual heat of formation is comparable to the stellar irradiation, is that Jupiter (and Saturn) emit isotropically in the infrared, the effects of cloud banding and structure notwithstanding. However, as a gas giant planet moves inward towards its primary star, the pressure level of the photosphere and the pressure level of the day-side radiative-convective zone separate. When the EGP is at  $\sim 0.05\text{ AU}$ , and after a Gyr, the photospheres have moved little, but the radiative-convective boundary is now near a kilobar. Moreover, the internal flux is miniscule compared with the magnitude of the irradiation. The result is that heat is not efficiently redistributed by internal convective motions, but by zonal winds in the radiative atmosphere *around* the planet to the night side. This day side/night side dichotomy is a central feature of hot Jupiters and can lead to severe thermal contrasts as a function of longitude.

Curiously, a star with solar composition at the edge of the light-hydrogen-burning main sequence ( $M_* \sim 75 M_J$ ) has a  $T_{\text{eff}}$  of  $\sim 1700\text{ K}$ . Therefore, an irradiated EGP, with a radius comparable to that of such a star, can be as luminous.

## 4.2 Planet/Star Flux ratios of Wide-Separation EGPs

The planet/star flux ratio versus wavelength is the key quantity in the study of orbiting planets. Figure 10, taken from Burrows, Sudarsky, & Hubeny (2004), depicts orbit-averaged (Sudarsky et al. 2000) such flux ratios from  $0.5\ \mu\text{m}$  to  $30\ \mu\text{m}$  for a  $1-M_J/5\text{-Gyr}$  EGP in a circular orbit at distances of 0.2 to 15 AU from a G2V star. These models are the same as those depicted in Fig. 9. The water absorption troughs are in evidence throughout. For the closer EGPs at higher atmospheric temperatures, carbon resides in CO and methane features are weak. For those hot Jupiters, the Na-D line at  $0.589\ \mu\text{m}$  and the corresponding resonance line of K I at  $0.77\ \mu\text{m}$  are important absorbers, suppressing flux in the visible bands. Otherwise, the optical flux is increased by Rayleigh scattering of stellar light. As  $a$  increases, methane forms and the methane absorption features appear in the optical (most of the waviness seen in Fig. 10 for  $a \gtrsim 0.5\text{ AU}$  shortward of  $1\ \mu\text{m}$ ), at  $\sim 3.3$

$\mu\text{m}$ , and at  $\sim 7.8 \mu\text{m}$ . At the same time, Na and K disappear from the atmosphere and the fluxes from  $\sim 1.5 \mu\text{m}$  to  $\sim 4 \mu\text{m}$  drop. For all models, the mid-infrared fluxes longward of  $\sim 4 \mu\text{m}$  are due to self-emission, not reflection. As Fig. 10 makes clear, for larger orbital distances a separation between a reflection component in the optical and an emission component in the mid-infrared appears. This separation into components is not so straightforward for the closer, more massive, or younger family members. For these EGPs, either the large residual heat coming from the core or the severe irradiation buoys the fluxes from 1 to 4  $\mu\text{m}$ . The more massive EGPs, or, for a given mass, the younger EGPs, have larger  $J$ ,  $H$ , and  $K$  band fluxes. As a result, these bands are diagnostic of mass and age. For EGPs with large orbital distances, the wavelength range from 1.5  $\mu\text{m}$  to 4  $\mu\text{m}$  between the reflection and emission components may be the least favorable search space, unless the planet is massive or young.

When water or ammonia clouds form, scattering off them enhances the optical fluxes, while absorption by them suppresses fluxes at longer wavelengths in, for example, the 4–5  $\mu\text{m}$  window. Because water and ammonia clouds form in the middle of this distance sequence, the geometric albedo ( $A_g$ ) is not a monotonic function of  $a$ . This effect is demonstrated in Figure 11, taken from Sudarsky et al. (2005), which plots the planet/star flux ratio for a Jovian-mass planet orbiting a G2V central star as a function of orbital distance at 0.55  $\mu\text{m}$ , 0.75  $\mu\text{m}$ , 1  $\mu\text{m}$ , and 1.25  $\mu\text{m}$ . Clearly, the planet/star flux ratio does not follow an inverse-square law. Clouds can form, evaporate, or be buried as the degree of stellar heating varies with varying distance. This behavior is included in the models of Fig. 10, but its precise manifestations depend upon unknown cloud particle size, composition, and patchiness. As a consequence, direct spectral measurements might constrain cloud properties. As Fig. 10 suggests, the planet/star contrast ratio is better in the mid- to far-infrared, particularly at wide separations. For such separations, the contrast ratio in the optical can sink to  $10^{-10}$ .

For the closest-in EGPs (not shown on Fig. 10), such as HD 189733b, HD209458b, OGLE-TR56b, 51 Peg b, and  $\tau$  Boo b, the contrast ratio in the optical should be between  $10^{-5}$  and  $10^{-6}$  and is more favorable, though still challenging. However, for these hottest EGPs, alkali metal (sodium and potassium) absorption is expected to dominate in the optical and very near-IR. Sodium has already been detected in the transit spectrum of HD 209458b. As a result, the expectation is that the optical albedos of hot Jupiters should be quite low, perhaps less than  $\sim 5\%$ .

Importantly, the transiting EGPs are so hot and their orbits are so favorably inclined that the planet/star flux ratios in the mid-IR, in particular in the *Spitzer* bands, can range between  $\sim 10^{-3}$  and  $\sim 10^{-2}$ . For these objects, the gap between the reflection and emission components is completely closed. Moreover, the variation in the summed light of planet and star during eclipses and the execution of the orbit can be used to derive the planetary spectrum itself.

### 4.3 Hot Jupiter Highlights

The discovery of  $\sim 60$  (and counting) transiting giant planets allows one to address their physical structures by providing simultaneous radius and mass measurements. However, the proximity of transiting EGPs to their primaries boosts the planet/star flux contrast ratios in the near- and mid-IR to values accessible by *Spitzer* during secondary eclipse. Such measurements in the IRAC ( $\sim 3.6$ ,  $\sim 4.5$ ,  $\sim 5.8$ ,  $\sim 8 \mu\text{m}$ ) and MIPS ( $\sim 24 \mu\text{m}$ ) bands, as well as IRS spectral measurements from  $\sim 5$  to  $\sim 14 \mu\text{m}$ , are the first *direct* detections of planets outside the solar system. In addition, *Spitzer* has yielded photometric light curves as a function of orbital phase, and revealed or constrained brightness distributions across planet surfaces. This has been done (dramatically so) for HD 189733b at 8 and 24 microns, for HD 149026b and GJ 436b at 8 microns, and, though non-transiting, for both  $v$  And b at 24 microns and HD 179949b at 8 microns. It will soon be done for many more hot Jupiters. Excitingly, *Spitzer* measurements alone have yielded exoplanet compositions, temperatures, and longitudinal temperature variations that have galvanized the astronomical and planetary communities.

Furthermore, using NICMOS, STIS, and ACS on HST, precision measurements of transit depths as a function of wavelength have enabled astronomers to identify atmospheric compositions at planet terminators. In this way, sodium, water, methane, hydrogen, and carbon monoxide have been inferred. Moreover, the MOST micro-satellite has obtained a stringent upper limit of  $\sim 8\%$  to the optical albedo of HD 209458b (Rowe et al. 2008). Hence, in ways unanticipated just a few years ago, these space telescopes are constraining the degree of heat redistribution from the day to the night sides by zonal winds (providing a glimpse of global climate), are signaling the presence of thermal inversions, and are revealing exoplanet chemistry. The new data from *Spitzer*, HST, and MOST have collectively inaugurated the era of remote sensing of exoplanets and the techniques articulated in this chapter were developed to interpret such data.

As described above, there are many recent highlights in the study of giant exoplanet atmospheres, but we will focus here on only a few examples. They are the spectral and photometric measurements of HD 189733b by Grillmair et al. (2008) and Charbonneau et al. (2008) and the photometric measurements of HD 209458b by Knutson et al. (2008) and Deming et al. (2005), along with their interpretations (see also Barman 2008). These objects exemplify the two basic classes of EGP atmospheres which have emerged, those without and with significant thermal inversions at altitude, and are the two best studied transiting EGPs.

The top panel of Fig. 12 shows a comparison of the HD 189733b data with three theoretical models for the planet/star flux ratio. The best fit model (black) is consistent with most of the data and assumes solar elemental abundances and only modest heat redistribution to the night side ( $P_n = 0.15$ ). One of the salient features is the fact that

the IRAC 1 ( $\sim 3.6 \mu\text{m}$ ) to IRAC 2 ( $\sim 4.5 \mu\text{m}$ ) ratio is greater than one. This has been interpreted to mean that the temperature profile monotonically decreases outward and that there is no significant inversion. The left panel of Fig. 13 shows such temperature profiles (but for TrES-1), as well as the locations of the effective photospheres in the *Spitzer* bands. An appreciable inversion would reverse the IRAC 1/IRAC 2 ratio, since the effective photosphere in IRAC 2 is further out and at much lower pressures than that for IRAC 1. In addition, the depression of the IRAC 2 flux is consistent with the presence of carbon monoxide, which has a strong absorption feature there. More important is the comparison between theory and the IRS spectrum of Grillmair et al. (2008) between  $\sim 5$  and  $\sim 14$  microns. Not only is the slope of the spectrum roughly matched, but there is a  $\sim 3\text{-}\sigma$  detection of a feature just longward of  $\sim 6$  microns. This is best interpreted as the flux peak due to the opacity window between the P and R branches of the  $\nu_2$  vibrational bending mode of water vapor (see Fig. 2). Water would explain both the general slope of the IRS spectrum and this peak and together they are now taken to be the best indications of the presence of water (steam) in an EGP atmosphere.

The bottom panel of Fig. 12 compares theoretical models for the planet/star flux ratio of HD 209458b at secondary eclipse with the corresponding *Spitzer* photometric data of Knutson et al. (2008) (IRAC) and Deming et al. (2005) (MIPS). The differences with HD 189733b are illuminating. Here, the IRAC 1/IRAC 2 ratio is less than one and the IRAC 3 ( $\sim 5.8 \mu\text{m}$ ) flux is higher than the IRAC 4 ( $\sim 8 \mu\text{m}$ ) flux. These features are best interpreted as signatures of a thermal inversion at altitude. There must be an absorber of optical (and/or near UV) stellar light to create the thermal inversion and a hot outer atmosphere (see right panel of Fig. 13), with the result that the planet/star ratio is much higher in the IRAC 1, 2, and 3 channels than predictions without inversions (e.g., the black curve without an absorber). In fact, centered near IRAC 3, the IRAC data look like an *emission* feature, centered in the broad water band from  $\sim 4.5$  to  $\sim 8 \mu\text{m}$ , as opposed to the absorption trough expected for an atmosphere with a negative temperature gradient. Emission features are expected in atmospheres with thermal inversions.

HD 189733b and HD 209458b together represent the two classes of hot-Jupiter atmospheres that are emerging to be explained. As Fig. 12 indicates, we can reproduce their basic spectral features, but there remain many anomalies. The fits at  $\sim 24 \mu\text{m}$  are problematic and the detailed shapes of the spectra are not well reproduced. Moreover, the models depend upon the degree of heat redistribution to the night side (modeled as  $P_n$ ; Burrows, Budaj, & Hubeny 2008), which crucially depends upon the unknown zonal flows and global climate. More important, though we know that there are inversions in the atmospheres of HD 209458b, TrES-4, XO-1b, and (likely) HD 149026b, we don't know why. What is the nature of this "extra absorber" in the optical (§2.6)? With what other planetary properties is the presence or absence of an inversion correlated? Metallic-

ity? Gravity? The substellar flux on the planets TrES-1 and XO-1b are similar, but only the latter shows an inversion. In the bottom panel of Fig. 12, we have introduced an ad hoc optical absorber at altitude merely to determine the opacity ( $\kappa_e$ ) needed to reproduce the measurements. Its physical origin is not addressed. Some have suggested it is TiO or VO (Fortney et al. 2008). However, these species can easily condense out and should not persist for long in the upper atmosphere. The so-called cold-trap, which operates in the Earth's upper atmosphere to render it dry, should also operate for these metal oxides here (Spiegel, Silverio, & Burrows 2009). Hence, the nature of the extra optical absorber at altitude is currently unknown. One might well ask whether the slight thermal inversion introduced due to zonal heat redistribution at depth can be the culprit (Hansen 2008), but the magnitude of the resulting temperature excursion is slight ( $\leq 100$  K) and does not approach the  $\sim 1000$  K needed to explain the data. A recent suggestion by Zahnle et al. (2009) involves the photolytic production of allotropes of sulfur and HS. However, whether a sulfur allotrope or any sulfur compound achieves the necessary abundance at the requisite upper pressure levels and what its production systematics are with the properties of the planet and star (metallicity and/or stellar spectrum) remains to be seen. The theoretical task is emerging to be complex and challenging.

## 5. FUTURE PROSPECTS

The theoretical study of exoplanet atmospheres in general, and of EGP atmospheres in particular, has been energized by continuing discoveries and surprises which show no sign of abating. In the short term, the last cold cycle and the upcoming warm cycle(s) of *Spitzer* will provide more light curves and secondary eclipse measurements. HST will continue to yield high-sensitivity transit data. Ground-based extreme adaptive optics systems that will enable high-contrast imaging of exoplanets from under the glare of their parent stars will be developed and perfected. In the next decade, JWST will constitute a quantum leap in sensitivity and broader wavelength coverage, which together may lay to rest many of the outstanding questions which have emerged during the early heroic phase of EGP atmospheric characterization. These include, but are not limited to:

- How do zonal flows in EGP atmospheres affect their spectra and phase curves?
- What is the magnitude of heat redistribution to the planet's night side? What is " $P_n$ "?
- How bright is the night side?
- Upon what do the longitudinal positions of the hot and cold spots of strongly irradiated planets depend?
- What is the depth of heat redistribution?



- What causes the strong thermal inversions in a subset of the hot Jupiters?
- Is there a central role for photolysis and non-equilibrium chemistry in EGP atmospheres, particularly in hot Jupiter atmospheres?
- Can the chemistry and irradiation be out of phase? Is there chemical and thermal hysteresis?
- How different are the compositions on a planet's day side and night side?
- How different are the temperatures and chemical compositions at the terminators of hot Jupiters during ingress and egress?
- Could there be significant gaps in our understanding of the dominant chemical constituents of EGP atmospheres?
- What is the origin of dissipation in planetary atmospheres that stabilizes their zonal flows?
- What are the signatures of non-zero obliquity and asynchronous spin in the measured light curves and spectra?
- What are the unique features of the light curves of EGPs in highly elliptical orbits and can tidal heating contribute to their thermal emissions?
- What are the thermal and chemical relaxation time constants of EGP atmospheres under the variety of conditions in which they are found?
- At what orbital distances are the day-side and night-side IR fluxes the same due to efficient heat redistribution?
- What is the role of metallicity and planet mass in EGP compositions, light curves, and spectra?
- What are the spectral and evolutionary effects of atmospheric clouds and hazes?
- Do the convective cores of hot Jupiters cool differently on their night and day sides?

Our theories are poised to improve significantly, with credible multi-dimensional simulations undertaken and non-equilibrium chemistry and cloud formation addressed. Methods are being designed to understand day-night coupling, the degree of heat redistribution, and the pattern of zonal flow. Moreover, with the discovery of more transiting planets such as GJ 436b in the ice giant mass and radius regime, the variety of signatures will multiply. Finally, more wide-separation EGPs will be separately imaged and probed. Given the brilliant nature of its past, whatever the manifold uncertainties, this field is on a trajectory of future growth and excitement that is establishing it as a core discipline of 21st-century astronomy.

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TABLE 1  
COMPOSITIONS OF JUPITER AND SATURN IN VOLUME MIXING RATIOS

| Gas                           | Jupiter                       | Saturn                     |
|-------------------------------|-------------------------------|----------------------------|
| H <sub>2</sub>                | 0.862±0.003                   | 0.882±0.024                |
| He                            | 0.136±0.003                   | 0.113±0.024                |
| CH <sub>4</sub>               | 2.4±0.5 x 10 <sup>-3</sup>    | 4.7±0.2 x 10 <sup>-3</sup> |
| NH <sub>3</sub>               | ≤ 7 x 10 <sup>-4</sup>        | ≤ 1 x 10 <sup>-4</sup>     |
| H <sub>2</sub> O              | ≤ 6.5±2.9 x 10 <sup>-5</sup>  | 0.2–2 x 10 <sup>-7</sup>   |
| CO <sub>2</sub>               |                               | ≤ 3 x 10 <sup>-10</sup>    |
| CO                            | 1 x 10 <sup>-9</sup>          | (1–3) x 10 <sup>-9</sup>   |
| PH <sub>3</sub>               | ≤ 6 x 10 <sup>-6</sup>        | ≤ 4.5 x 10 <sup>-6</sup>   |
| GeH <sub>4</sub>              | ~2 x 10 <sup>-8</sup>         | 3.4 x 10 <sup>-7</sup>     |
| H <sub>2</sub> S              | 1–8 x 10 <sup>-5</sup>        | <10 <sup>-6</sup>          |
| C <sub>2</sub> H <sub>2</sub> | ≤ 3 x 10 <sup>-8</sup>        | ≤ 1 x 10 <sup>-7</sup>     |
| C <sub>2</sub> H <sub>6</sub> | ≤ 3 x 10 <sup>-6</sup>        | ≤ 5 x 10 <sup>-6</sup>     |
| HCN                           | < 1 x 10 <sup>-10</sup>       | < 10 <sup>-9</sup>         |
| CH <sub>3</sub> D             | ~2 x 10 <sup>-8</sup>         | 3.2±0.2 x 10 <sup>-7</sup> |
| HD                            | ~1.1 x 10 <sup>-5</sup>       | 0.7–1.7 x 10 <sup>-8</sup> |
| Ar                            | 1.0 ± 0.4 x 10 <sup>-5</sup>  |                            |
| Ne                            | 2.3 ± 0.25 x 10 <sup>-5</sup> |                            |

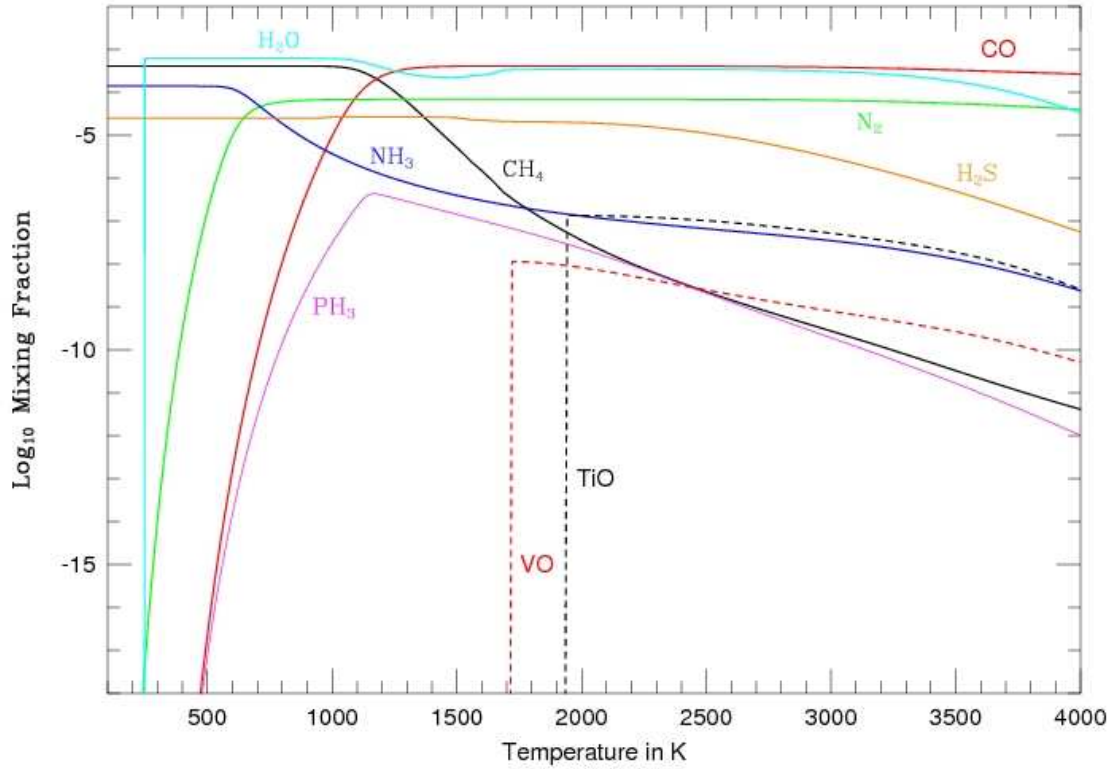


Fig. 1.— The log (base 10) of the mixing fraction as a function of temperature at a total gas pressure of 1 atmosphere for the seven molecules shown with solid curves  $CH_4$  (black),  $CO$  (red),  $N_2$ ,  $NH_3$ ,  $H_2O$ ,  $H_2S$ , and  $PH_3$ , and the two molecules shown with dashed curves  $TiO$  and  $VO$ . At 4000 K,  $CO$  and  $N_2$  are the most stable species, containing nearly all the carbon and nitrogen, respectively. With decreasing temperature,  $CO$  reacts with  $H_2$ , forming  $CH_4$ , which becomes the dominant carbon-bearing species at low temperatures, and  $N_2$  reacts with  $H_2$ , forming  $NH_3$ , which likewise becomes the dominant nitrogen-bearing species at low temperatures. Except above about 3000 K,  $H_2O$  is fully associated containing nearly all the available oxygen that is not bound in  $CO$ . Below about 1600 K, its abundance temporarily falls slightly due to the condensation of silicates which reduce the available oxygen; however, the mixing fraction of  $H_2O$  then rises again when  $CO$  is converted to  $CH_4$ , which releases the oxygen tied up in  $CO$ . Finally, at 273 K  $H_2O$  drops effectively to zero due to the condensation of ice. With decreasing temperature, both  $TiO$  and  $VO$  rise as they associate, then sharply drop to effectively zero when condensates involving  $Ti$  and  $V$  form. [Taken from Sharp & Burrows (2007)]

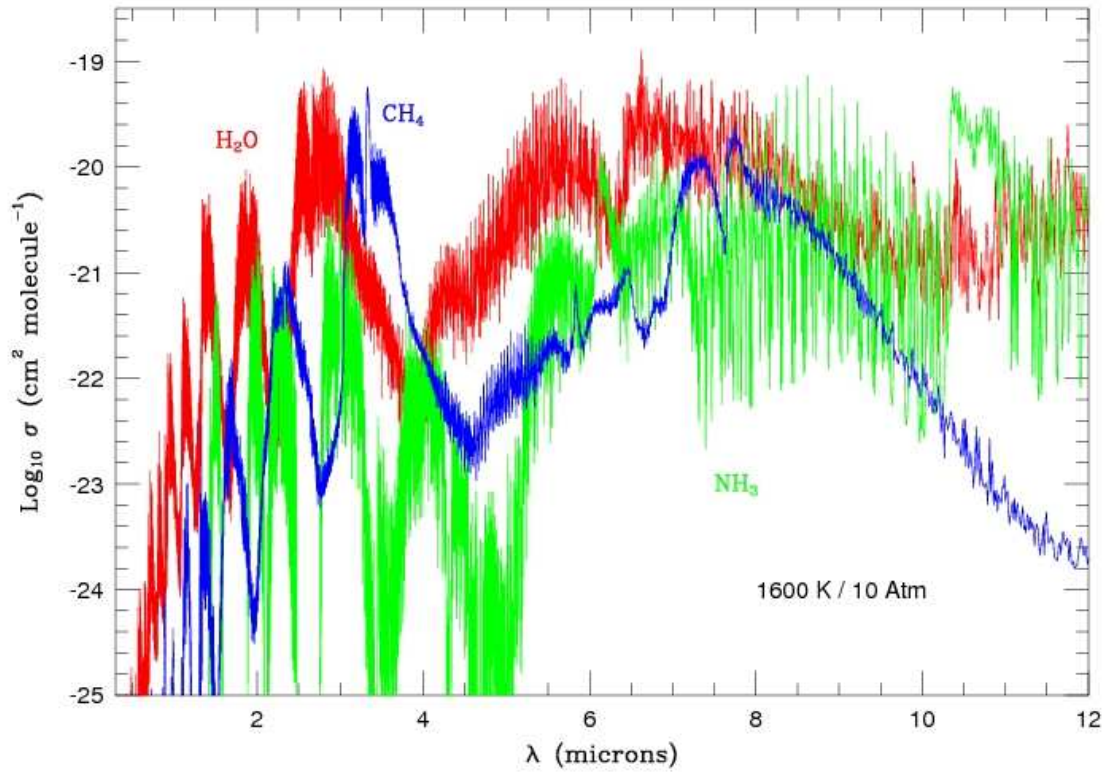


Fig. 2.— The log (base 10) of the monochromatic absorption  $\sigma$  in  $\text{cm}^2 \text{molecule}^{-1}$  as a function wavelength  $\lambda$  in  $\mu\text{m}$  in the infrared at a temperature of 1600 K and a pressure of 10 atmospheres for the vibration-rotation transitions of  $\text{H}_2\text{O}$ ,  $\text{NH}_3$ , and  $\text{CH}_4$ . The contribution due to different isotopes is included. For this plot we chose a high enough temperature and pressure to ensure that the lines were sufficiently broadened to suppress very rapid and large-amplitude fluctuations in the absorption cross section that can otherwise be in evidence over short wavelength intervals. In this way, the main band features (which are nevertheless generic for each species) are more easily seen. At significantly lower pressures the broadening of the lines is much smaller and the absorption can change so rapidly in short wavelength intervals that the main features do not show up so clearly. As can be seen here,  $\text{H}_2\text{O}$  has a strong absorption feature just shortward of  $3 \mu\text{m}$ , and  $\text{CH}_4$  has a strong peak near of  $3.3 \mu\text{m}$ . In the region of  $8 \mu\text{m}$  to  $9 \mu\text{m}$  all three molecules absorb strongly; however, between about  $10.5 \mu\text{m}$  and  $11 \mu\text{m}$   $\text{NH}_3$  has absorption which is distinctly higher than that of the other two molecules. When the combined opacity is calculated, the individual absorptions must be weighted by the abundances. [Taken from Sharp & Burrows (2007)]

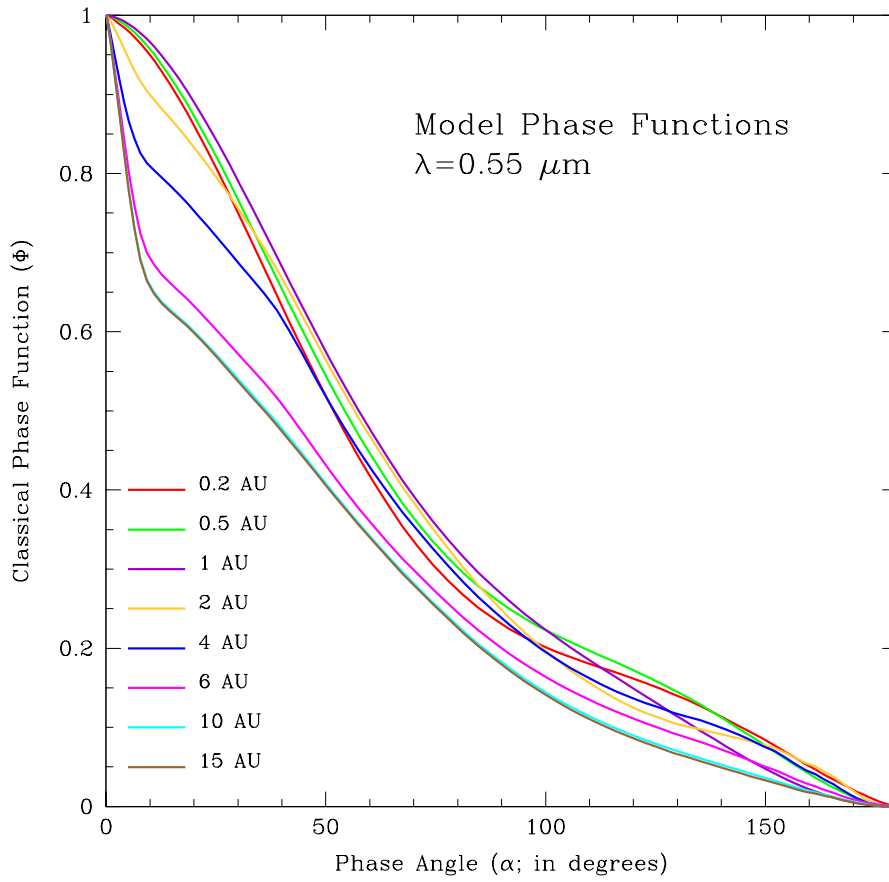


Fig. 3.— Theoretical optical phase functions of  $1-M_J$ , 5-Gyr EGPs ranging in orbital distance from 0.2 AU to 15 AU from a G2V star. Near full phase, the phase functions for our baseline models at larger orbital distances peak most strongly. For the cloud-free EGPs at smaller orbital distances (0.2 AU, 0.5 AU, and 1 AU), the phase functions are more rounded near full phase. [Taken from Sudarsky et al. (2005)]

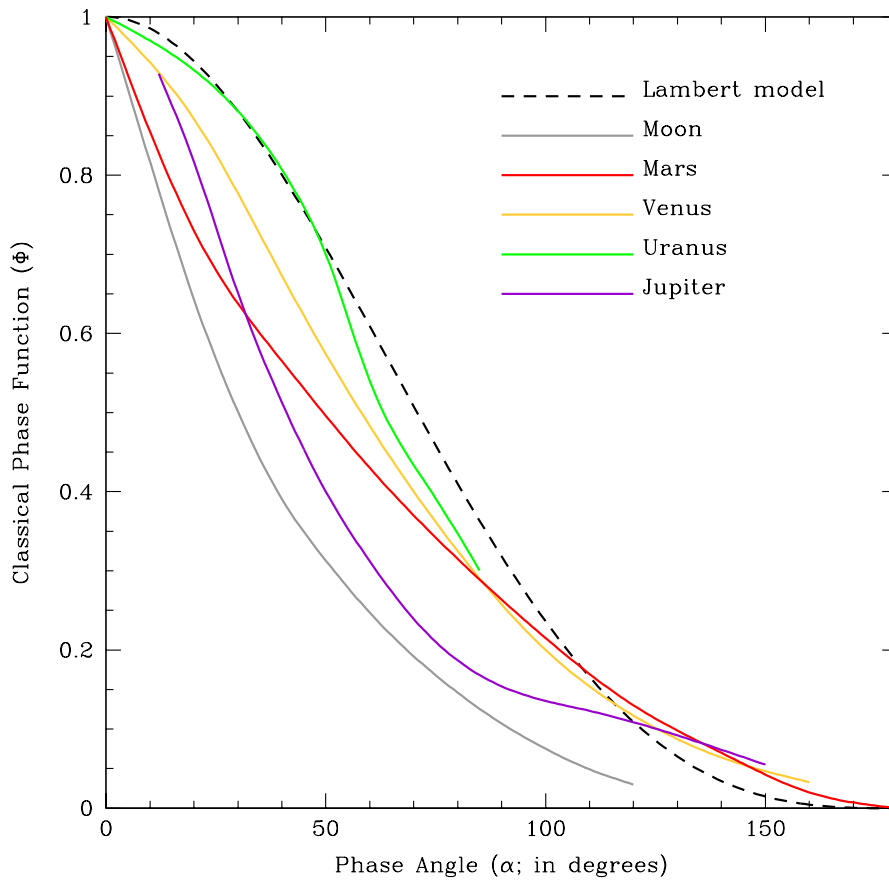


Fig. 4.— The measured visual phase functions for a selection of Solar System objects. A Lambert scattering phase curve, for which radiation is scattered isotropically off the surface regardless of its angle of incidence, is shown for comparison. The phase functions of the Moon and Mars peak near full phase (the so-called “opposition effect”). A red bandpass Jupiter phase function, taken from Dyudina et al. (2004), is also plotted. [Taken from Sudarsky et al. (2005)]

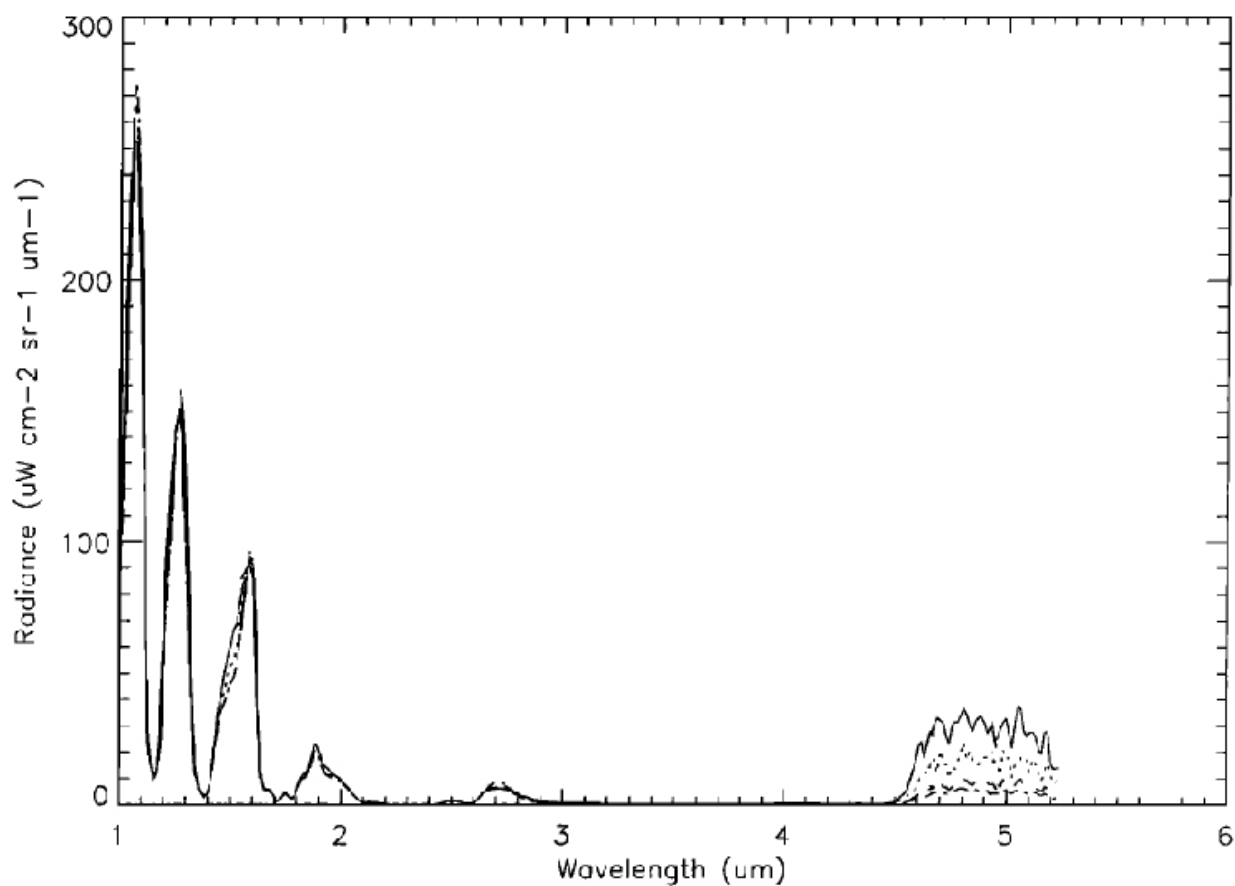


Fig. 5.— Near-infrared spectrum of Jupiter taken in a relatively “cold” but reflective region of the atmosphere by the Galileo Near-Infrared Mapping Spectrometer (NIMS) in 1996. All radiances except those near  $5 \mu\text{m}$  are sunlight reflected from clouds. Absorption is primarily due to  $\text{CH}_4$  gas with some contributions from a  $\text{H}_2$  collision-induced fundamental band near  $2.2 \mu\text{m}$ . From Irwin *et al.* (1998).



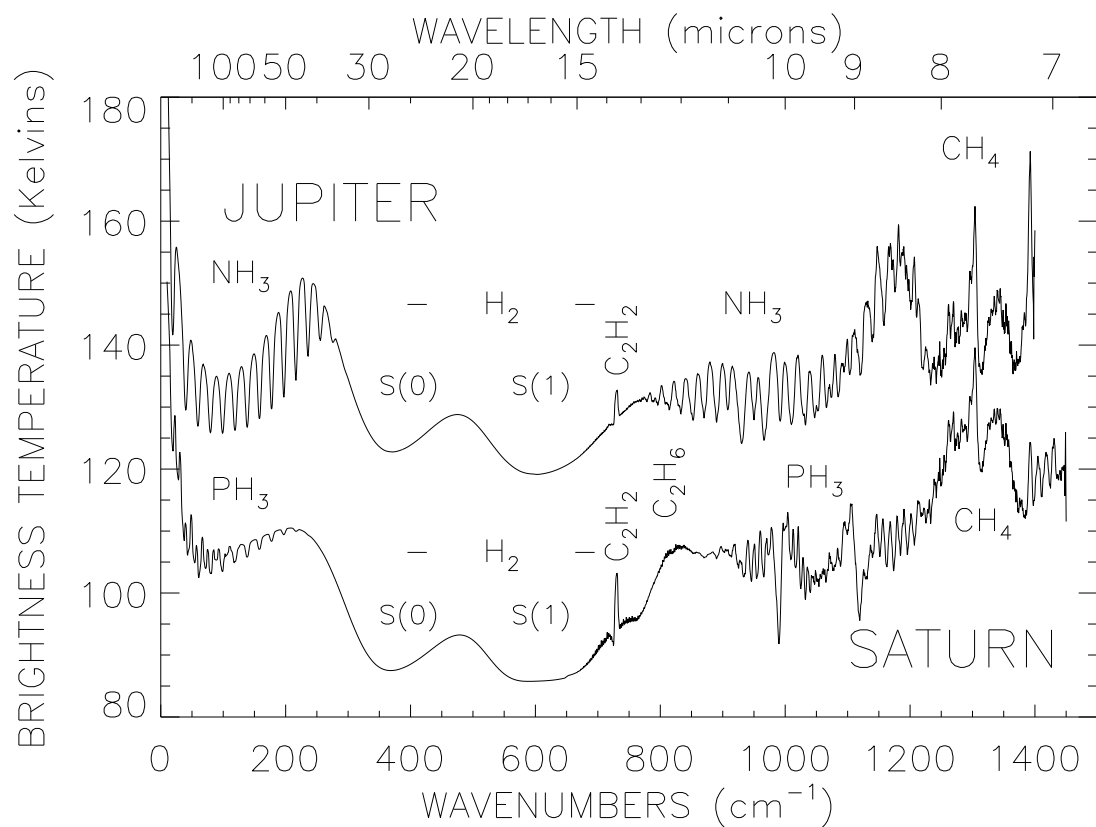


Fig. 6.— Middle-infrared brightness temperature spectra of Jupiter and Saturn, derived from Voyager and Cassini infrared spectrometers. Prominent spectral features are identified. Note that the  $H_2$  collision-induced absorption is a smooth continuum in the spectrum, with the broad rotational transitions S(0) and S(1) identified.

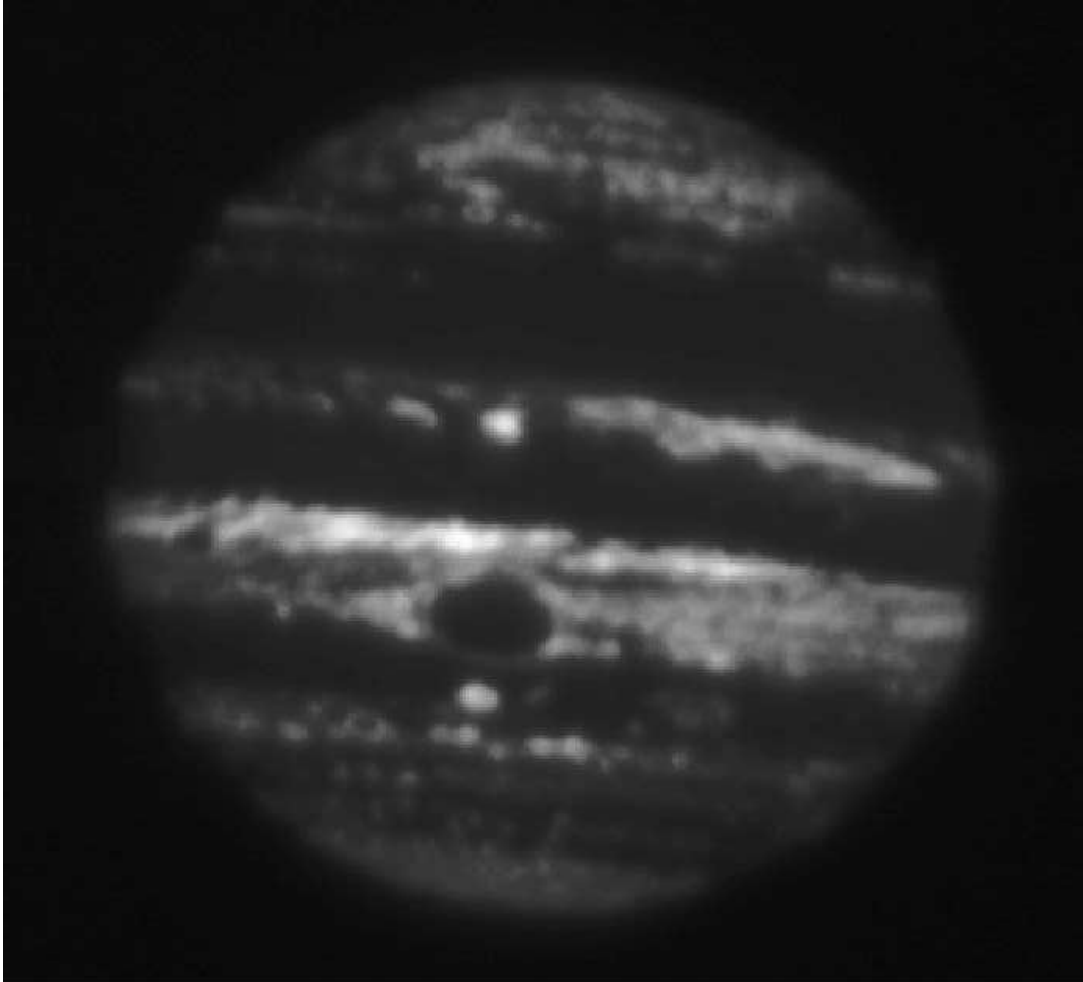


Fig. 7.— 4.85- $\mu\text{m}$  image of Jupiter taken at the NASA Infrared Telescope Facility using the facility NSFCam2 instrument on 2008 Sept 24. The filter used is 0.24  $\mu\text{m}$  wide and illustrates the primarily thermal radiance emerging from Jupiter's multi-layered cloud systems, with more radiance emerging from cloud tops in the deepest atmosphere. Jupiter's Great Red Spot can be seen in the lower center of the figure as a region whose periphery is defined by dry, downwelling gas which creates a region relatively clear of clouds.

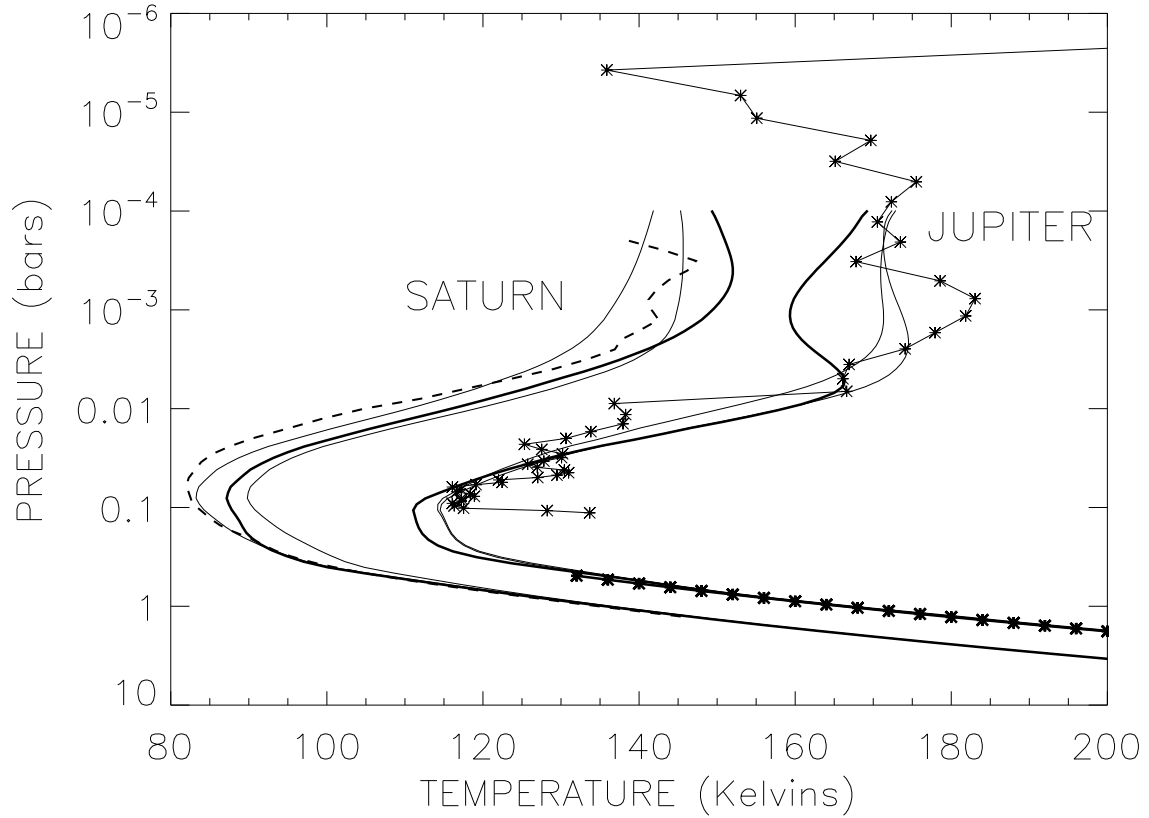


Fig. 8.— Temperature profiles for Jupiter and Saturn. Curves in solid lines are derived from Cassini CIRS (infrared) experiment observations, representative of near-equatorial (thick solid) and  $\pm 30^\circ$  latitude (regular solid) curves. Galileo probe Atmospheric Structure Instrument (ASI) results are shown by the regular solid curve and asterisks for the accelerometer data in the “inverted” stratosphere and by the thick solid curve and asterisks for the direct measurements in the troposphere. A Voyager radio occultation curve is shown for Saturn by the dashed curve. Note the warmer temperatures in Jupiter than in Saturn, the “inverted” temperatures in the radiatively controlled atmosphere at pressures lower than  $\sim 100$  mbars, vertical waves measured by the Galileo ASI accelerometer experiment, and the convergence of the several temperature profiles at different latitudes with depth.

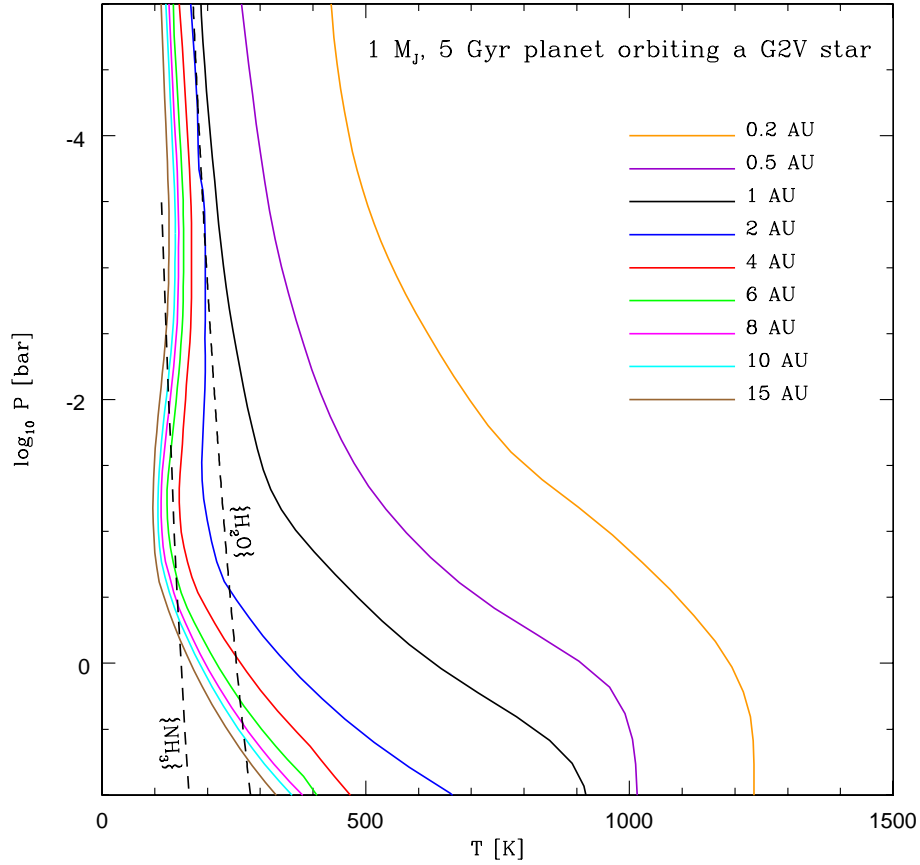


Fig. 9.— Profiles of atmospheric temperature (in Kelvin) versus the logarithm base ten of the pressure (in bars) for a family of irradiated  $1-M_J$  EGPs around a G2V star as a function of orbital distance. Note that the pressure is decreasing along the ordinate, which thereby resembles altitude. The orbits are assumed to be circular, the planets are assumed to have a radius of  $1 R_J$ , the effective temperature of the inner boundary flux is set equal to 100 K, and the orbital separations vary from 0.2 AU to 15 AU. The intercepts with the dashed lines identified with either  $\{NH_3\}$  or  $\{H_2O\}$  denote the positions where the corresponding clouds form. [Taken from Burrows et al. (2004)]

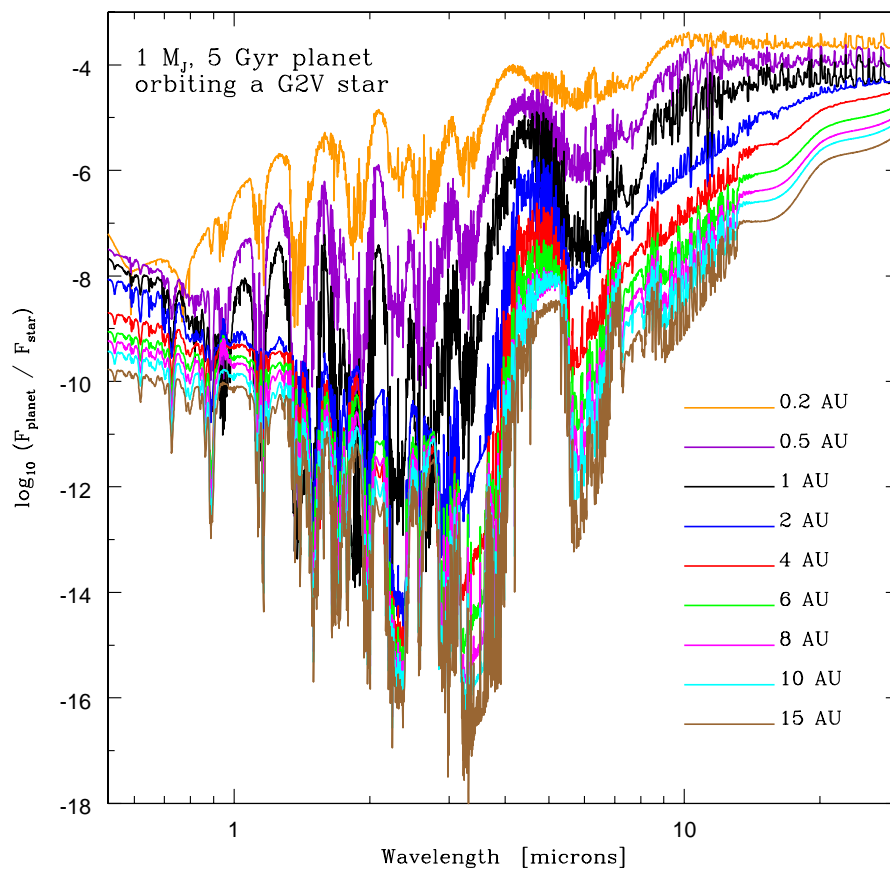


Fig. 10.— Theoretical planet to star flux ratios versus wavelength (in microns) from  $0.5 \mu\text{m}$  to  $30 \mu\text{m}$  for a  $1-M_J$  EGP with an age of 5 Gyr orbiting a G2V main sequence star similar to the Sun. This figure portrays ratio spectra as a function of orbital distance from 0.2 AU to 15 AU. Zero eccentricity is assumed and the planet spectra have been phase-averaged as described in Sudarsky, Burrows, & Hubeny (2003). The associated  $T/P$  profiles are given in Fig. 9. Table 1 in Burrows, Sudarsky, & Hubeny (2004) lists the modal radii for the particles in the water and ammonia clouds. Note that the planet/star flux ratio is most favorable in the mid-infrared. [Taken from Burrows et al. (2004)]

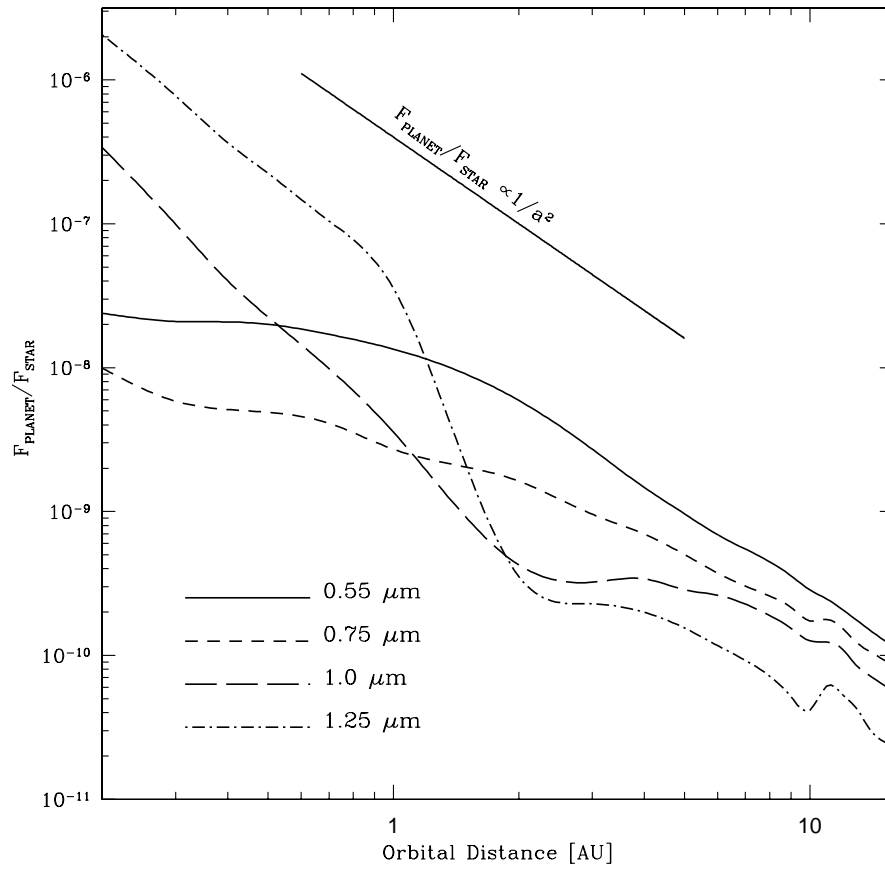


Fig. 11.— Planet/star flux ratio as a function of orbital distance at 0.55  $\mu\text{m}$ , 0.75  $\mu\text{m}$ , 1  $\mu\text{m}$ , and 1.25  $\mu\text{m}$  assuming a G2V central star. In each case, the plotted value corresponds to a planet at greatest elongation with an orbital inclination of  $80^\circ$ . Note that the planet/star flux ratios do not follow a simple  $1/a^2$  law. [Taken from Sudarsky et al. (2005)]

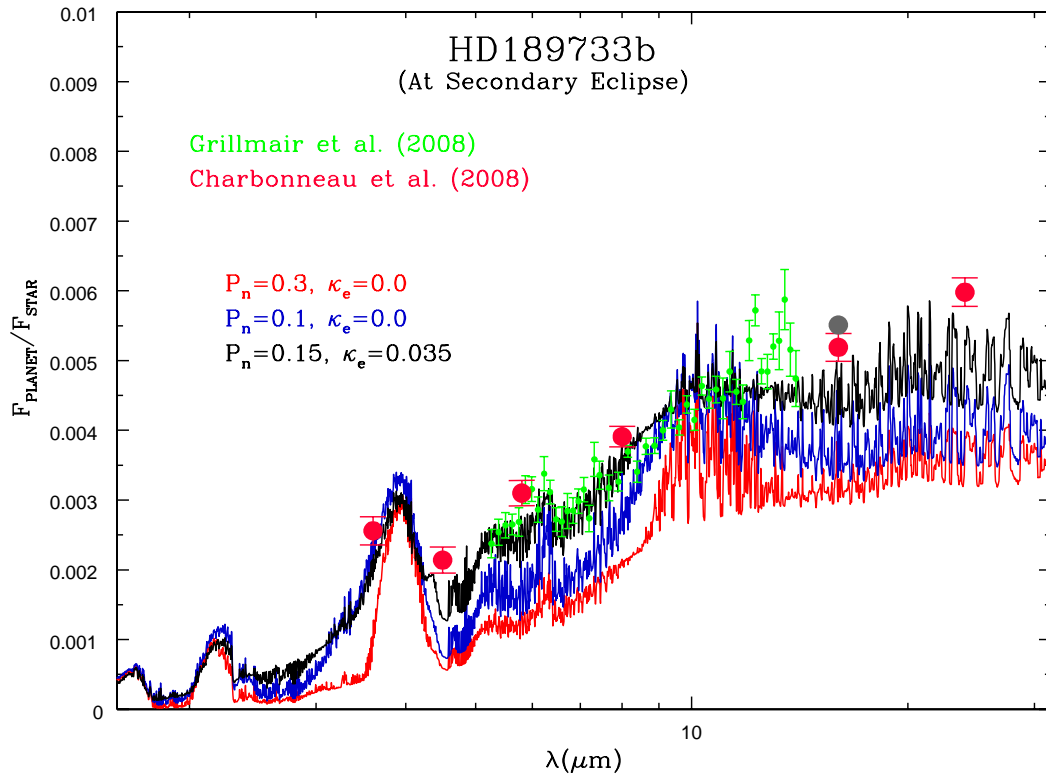
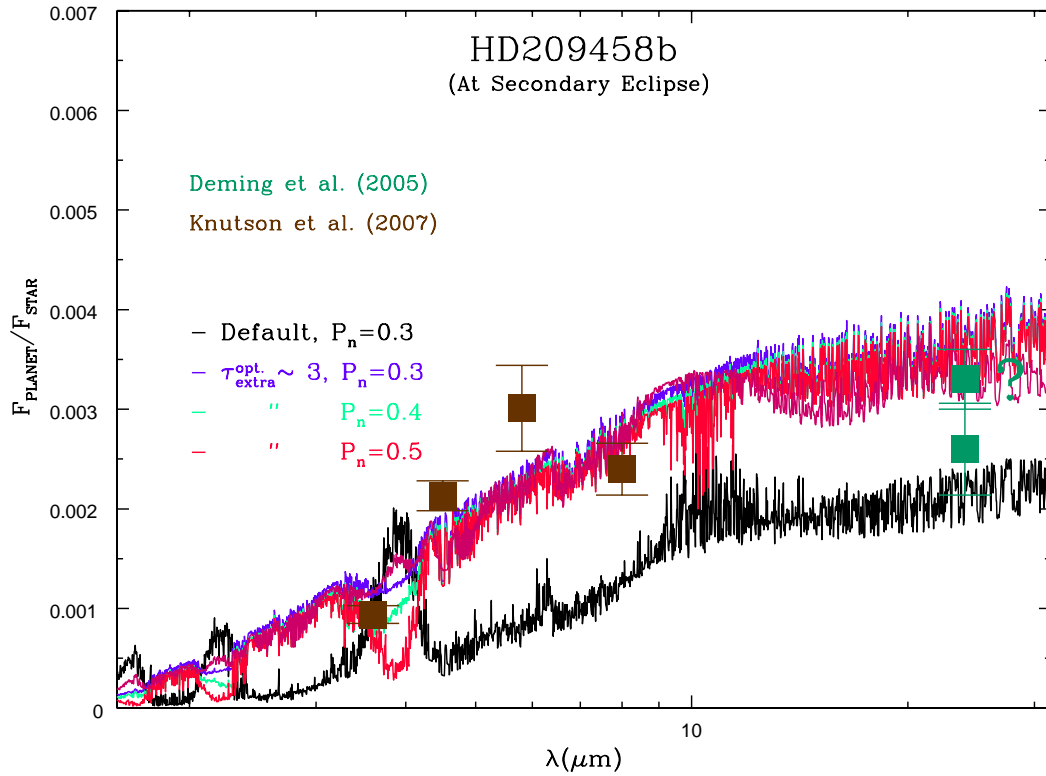


Fig. 12.— **Top:** The planet-star flux ratios at secondary eclipse versus wavelength for three models of the atmosphere of HD 209458b with inversions and for one model without an extra upper-atmosphere absorber of any kind (lowest curve). The three models with stratospheres have different values of  $P_n$  ( $= 0.3, 0.4,$  and  $0.5$ ), but are otherwise the same. The old, default model has a  $P_n$  of  $0.3$ . This figure demonstrates that models with an extra upper-atmosphere absorber in the optical and with  $P_n \gtrsim 0.35$  fit the data; the old model does not fit. Superposed are the four IRAC points and the MIPS data at  $24 \mu\text{m}$  from Deming et al. (2005) (square block on right). Also included, with a question mark beside it, is a tentative update to this  $24 \mu\text{m}$  flux point, provided by Drake Deming (private communication). **Bottom:** Comparison of spectral observations with broadband photometry and theoretical models of the dayside atmosphere of HD 189733b. The black points show the mean (unweighted) flux ratios spectra from  $\sim 5$  to  $\sim 14 \mu\text{m}$ , taken by IRS on *Spitzer* and published in Grillmair et al. (2008). The plotted uncertainties reflect the standard error in the mean in each wavelength bin. The filled red circles show broadband measurements at  $3.6, 4.5, 5.8, 8.0, 16,$  and  $24 \mu\text{m}$  from Charbonneau et al. (2008). Shown in color are atmospheric model predictions for three values of a dayside-nightside heat redistribution parameter,  $P_n$ , and two values for the extra upper-atmosphere opacity,  $\kappa_e$  (see Burrows, Budaj, & Hubeny 2008 for an explanation). See the text for discussion.

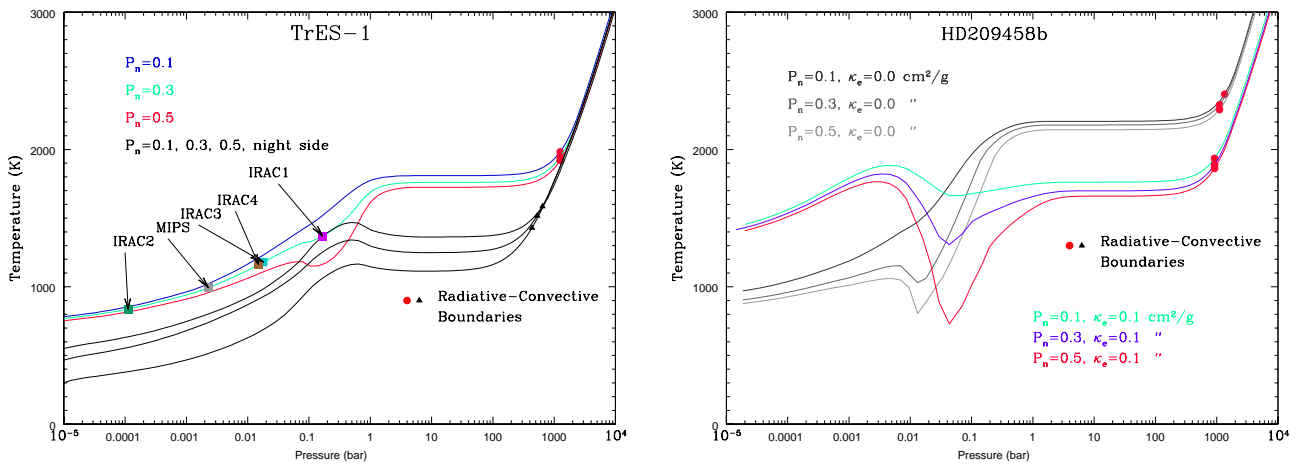


Fig. 13.— Dayside (set of higher curves around 10 bars) and nightside (lower set of curves) temperature-pressure profiles for TrES-1 (left), as a representative of a transiting EGP without a thermal inversion at altitude and for HD 209458b (right), as a representative of a transiting EGP with such a thermal inversion. These profiles incorporate the external substellar irradiation/flux and an internal flux for the planet corresponding to the temperature of 75 K at are included for HD 209458b. See text in for a discussion. Figures taken from Burrows, Budaj, and Hubeny (2008), to which the reader is referred for further details.