



Observational Cosmology Journal Club

Nov 16th, 2020 | Shijie Wang

1. Shibaïke & Alibert. Planetesimal formation at the gas pressure bump following a migrating planet I. Basic characteristics of the new formation model [arxiv:2010.10594v1](https://arxiv.org/abs/2010.10594v1)
2. Ali-Dib & Petrovich **Constraining protoplanetary disks with exoplanetary dynamics: Kepler-419 as an example** [arXiv:2009.06448v1](https://arxiv.org/abs/2009.06448v1)
3. Ronco et al. **How Jupiters Save or Destroy Inner Neptunes around Evolved Stars** [2020 ApJL 898 L23](https://doi.org/10.3847/2020ApJL898L23)

Preview

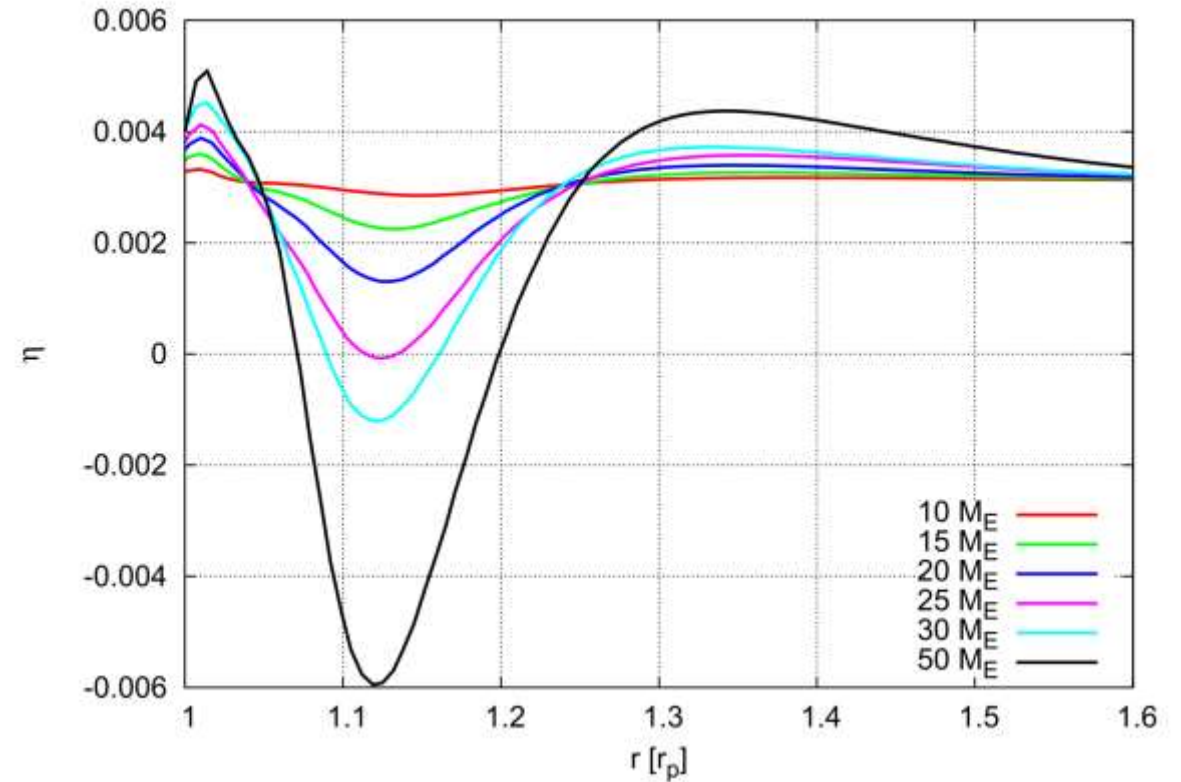
[P1] Planetesimal + planetary migration: a new scenario in which planetesimals can form in broad areas of the discs

[P2] Deducing the properties of the protoplanetary disk from the observed Kepler-419 system

[P3] After the host star turns to become red giant, the final fate of the “inner Neptune” can be very different if there is an “outer Jupiter”.

[P1] Context

- Some planet formation models believe that planets are formed via coalescence of **planetesimals**
- But how planetesimals grows all the way from dust?
 - Difficulty: Drift & fragmentation barriers may stop the growth
 - Previous solution: instabilities, but only occur at certain locations → not compatible with models & observation (arguably)
- This paper: a new scenario
 - Point 1: Planet can create a pressure bump → streaming instability → planetesimals form
 - Point 2: Planet can migrate → planetesimals can form in broad regions



Planet can create a pressure bump that can trap solid particles (Bitsch+18)

Methods: disk and planet

- Gas-disk models

$$\Sigma_{g, \text{unp}} = \Sigma_{g,0} (r/\text{au})^{-p}$$

$$T = T_0 (r/\text{au})^{-q}$$

3 Disk Models →

Disc	$\Sigma_{g,0}$	T_0	p	q
A	500	280	1	0.5
A'	5000	500	1	0.5
B	1700	280	1.5	0.5

- Planet

- Single planet, $20 M_{\oplus}$ @ 30 au (mig only, no mass growth)
- Undergoes Type I migration, given by Tanaka+02

- Gap structure

- $\Sigma_{g, \text{local}} = \Sigma_{g, \text{unp}} \max(s_K, s_{\text{min}})$

$$s_K = \max(s_{\text{Kepler}}, s_{\text{Rayleigh}})$$

$$s_{\text{min}} = (1 + 0.04K)^{-1}$$

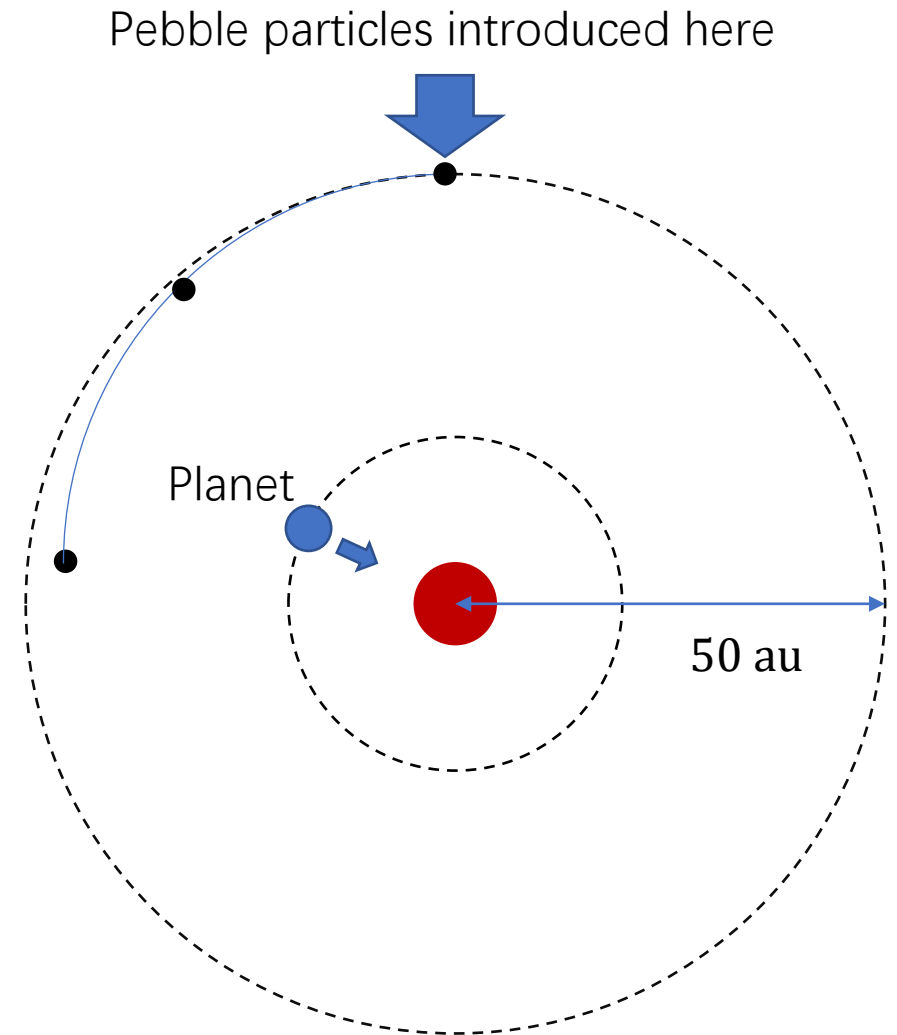
- Pressure gradient / gravity → $\eta = -0.5(H_g/R)^2 \partial \ln P_g / \partial \ln R$

$$P_g = \rho_g c_s^2 = \Sigma_{g, \text{local}} / (\sqrt{2\pi} H_g) c_s^2$$

Methods: pebbles → planetesimals

- Introduce pebble particles
 - Pebble drift radially $v_r = v_{drift} + v_{diff}$
$$v_{drift} = -2 \frac{St}{St^2+1} \eta v_K \text{ (due to head wind),}$$

 $St=0.1$
 v_{diff} is the radial diffusion velocity
 - Pebble particles are introduced at $r_{out} = 50 \text{ au}$
 - At time interval $\Delta t = \Omega_{K,planet}^{-1}$,
 - n particles are introduced to $[r_{out}, r_{out} + v_r \Delta t]$, with total mass $\dot{M}_{peb} \Delta t$. \dot{M}_{peb} surveyed.
 - n is integer and $n \geq 1$
 - Particles pass the planet's orbit or r_{out} will be removed
 - Calculation stops when $r_{planet} = 0.5 \text{ au}$



Methods: pebbles → planetesimals

- Planetesimal formation

- **Condition:** $\rho_{peb,mid} > \rho_{gas,mid}$

$$\rho_{peb,mid} = \Sigma_{peb} / (\sqrt{2\pi} H_{peb})$$

- Calculation of Σ_{peb} using pebble particles

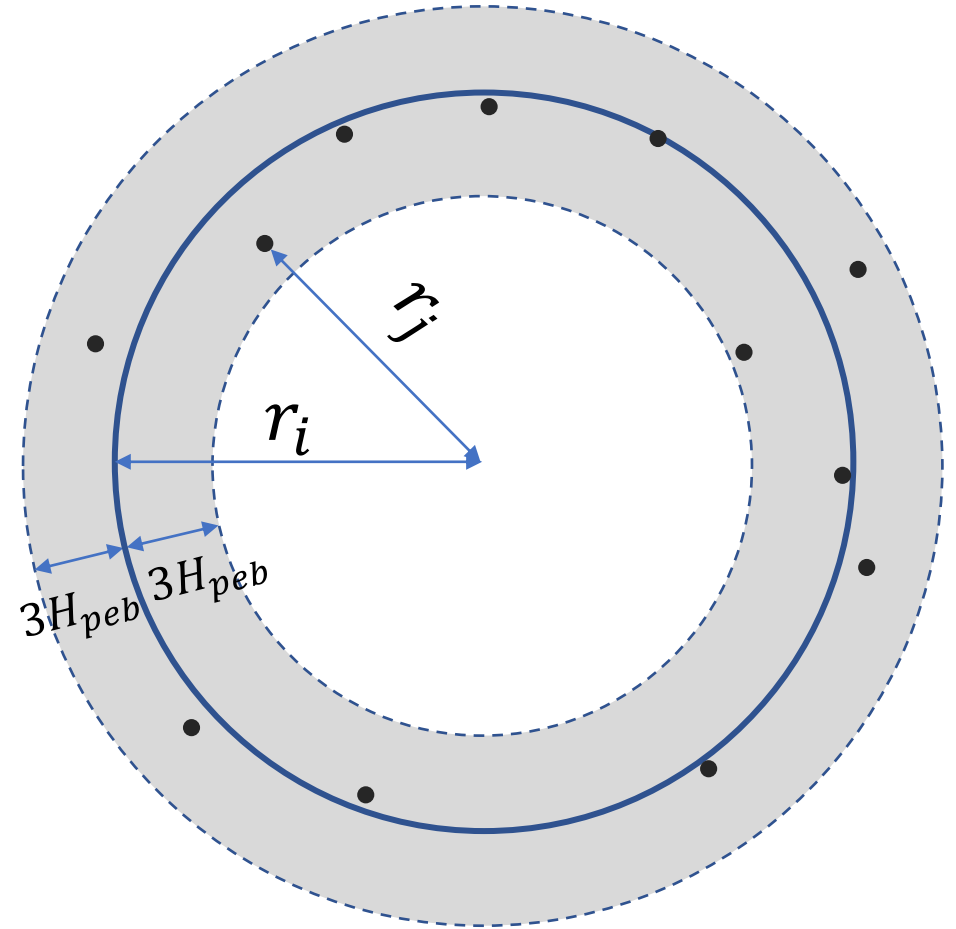
$$\Sigma_{peb}(r_i) \equiv \frac{1}{2\pi r_i} \sum_j m_{peb,j} W(|r_i - r_j|, H_{peb,r_i})$$

$$W(|r_i - r_j|, H_{peb,r_i}) = \frac{1}{\sqrt{\pi} H_{peb,r_i}} \exp \left[- \left(\frac{r_i - r_j}{H_{peb,r_i}} \right)^2 \right]$$

- $j \in$ all particles in grey area
- H_{peb,r_i} given by Youdin & Lithwick +07
- The pebble particle mass is then replaced by a planetesimal particle mass if condition is satisfied

$$m_{pls} = \chi_{SI} m_{peb}, \chi_{SI} = \epsilon_{SI} \Delta t / \tau_{SI}$$

- Planetesimals are merged if they are too close

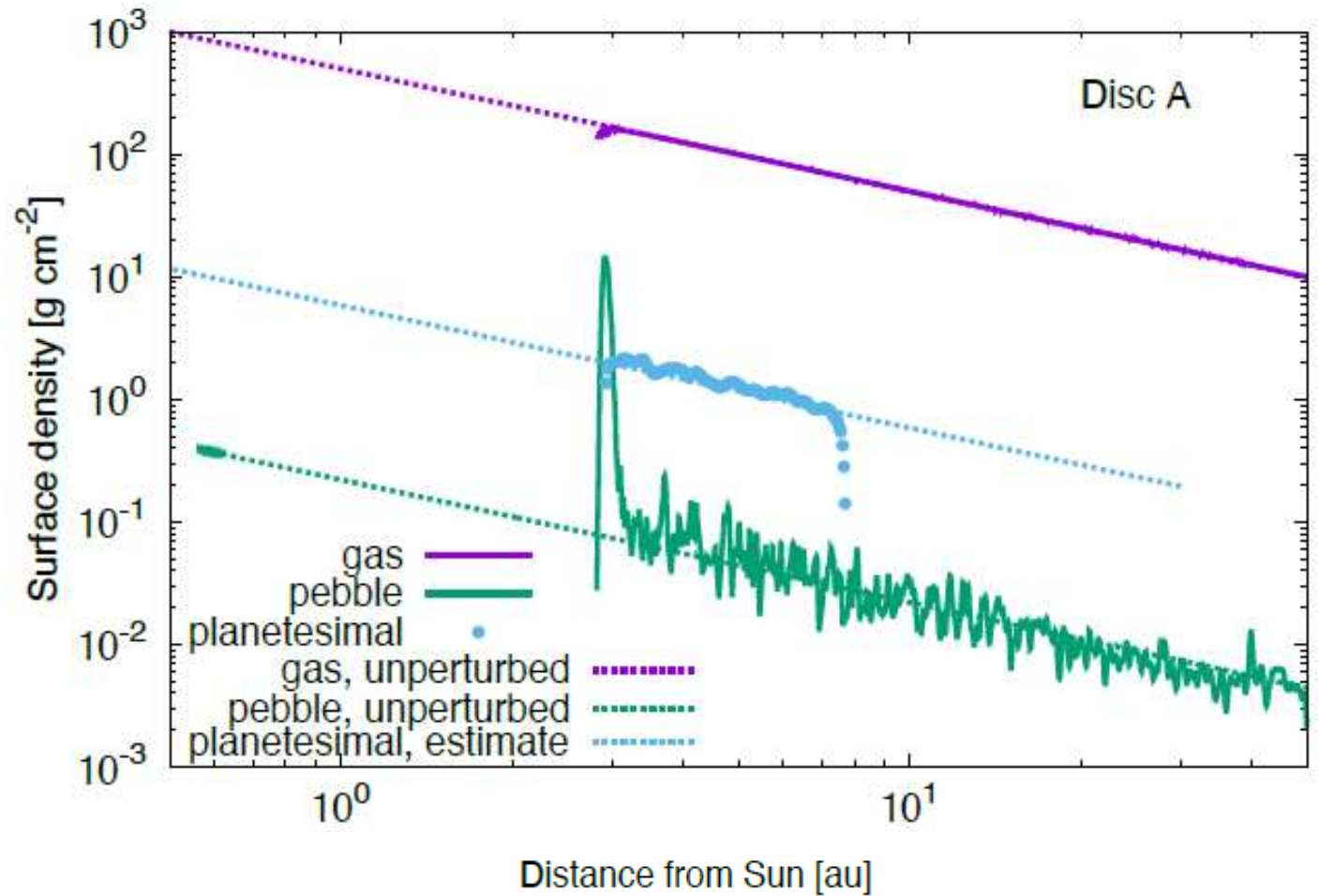


Results

- **A snapshot:** Gas, pebble and planetesimal surface density at 0.38 Myr, $\dot{M}_{peb} = 10^{-4} M_E \text{yr}^{-1}$
- Reference profile

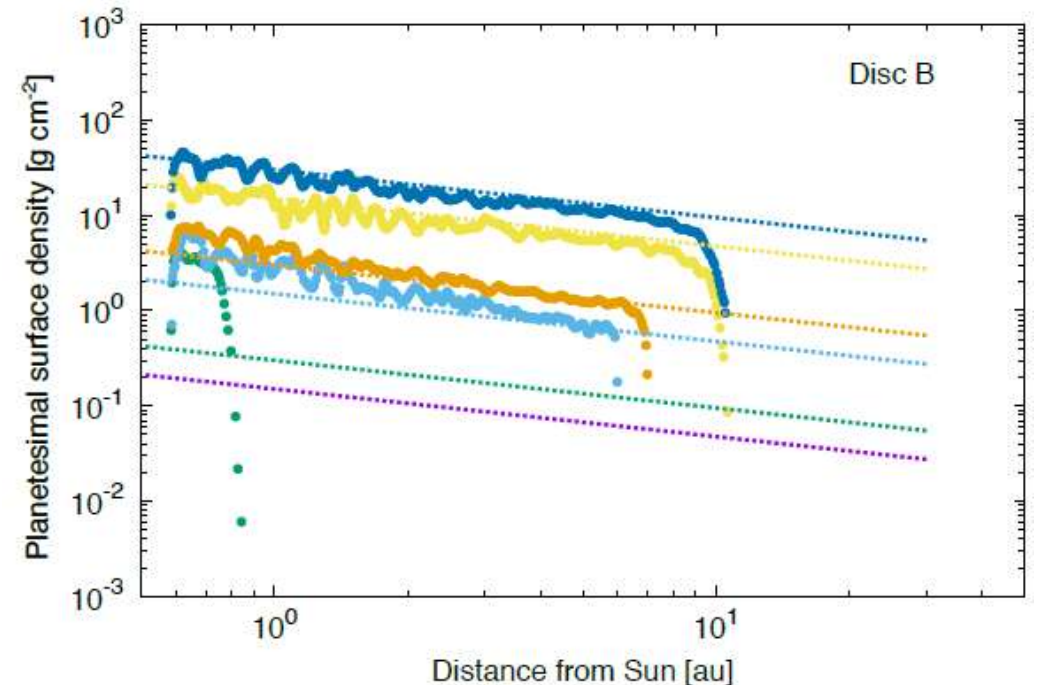
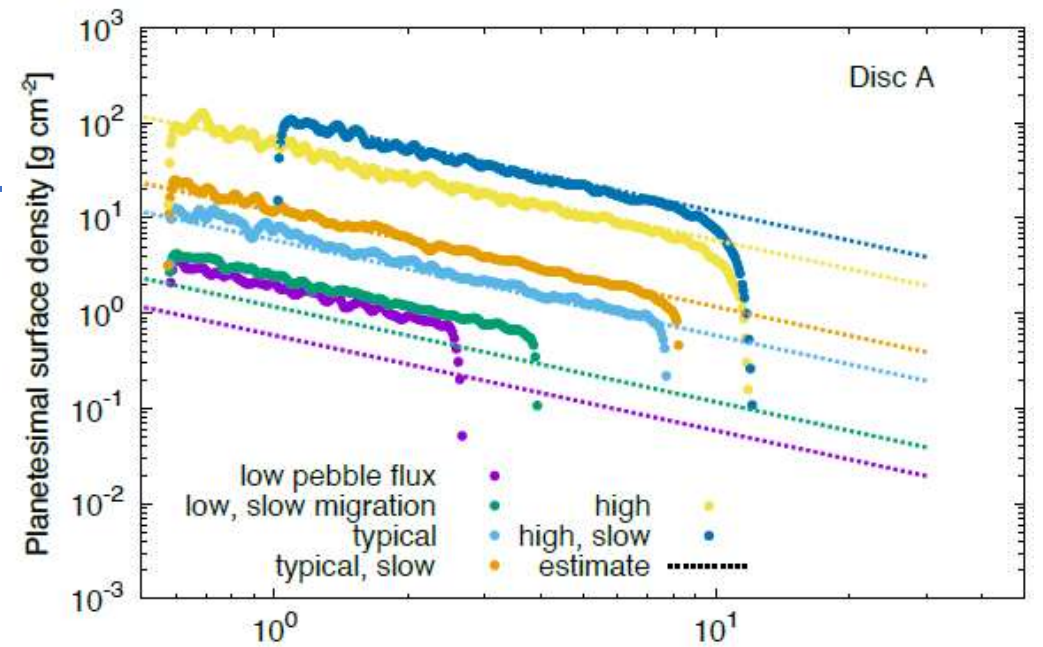
$$\Sigma_{peb,unp} = \frac{\dot{M}_{peb}}{2\pi r v_{drift,unp}}$$

$$\Sigma_{pls,est} \equiv \frac{\dot{M}_{peb}}{2\pi r v_{mig}}$$



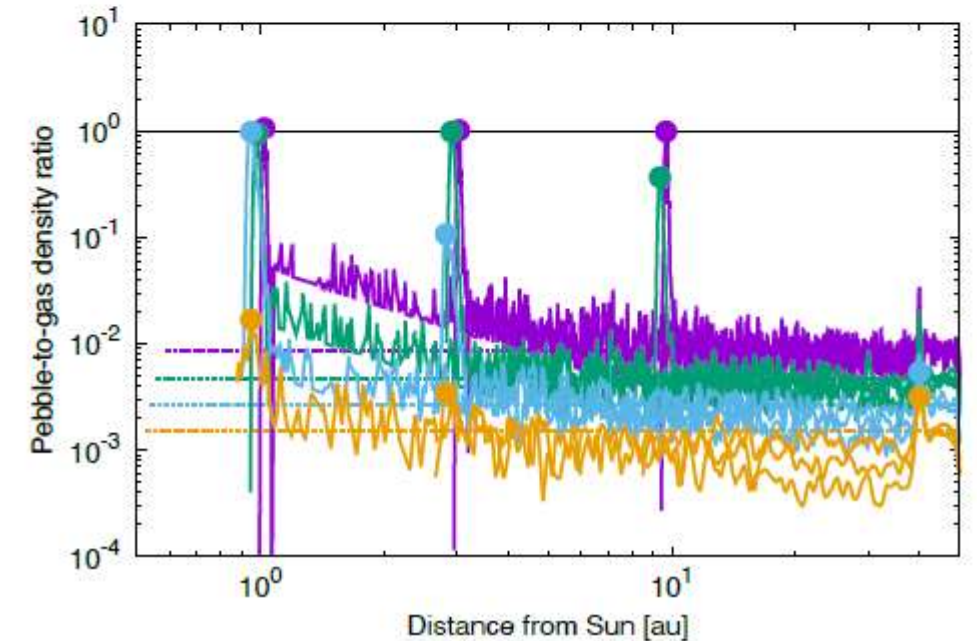
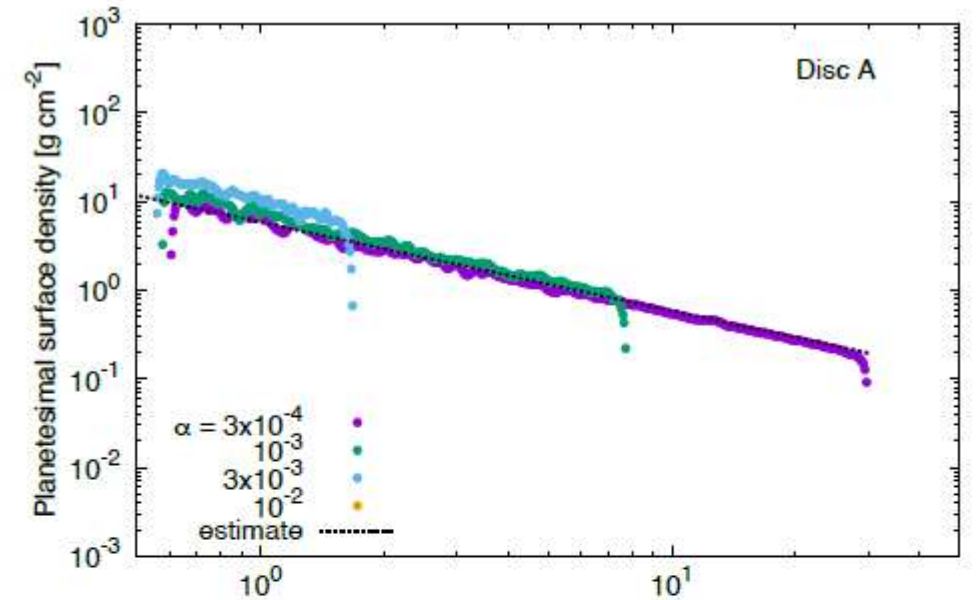
Results

- **Planetesimal surface density**
 - Typical/Low $\dot{M}_{peb} \rightarrow 10^{-4}/10^{-5} M_{\oplus} yr^{-1}$
 - Slow mig \rightarrow half speed
- Planetesimals form in wide regions of the discs, except for one case
- Profile well approximated by $\Sigma_{pls,est}$
 \rightarrow All pebbles near the planet become planetesimal \rightarrow quasi-static



Parameter study

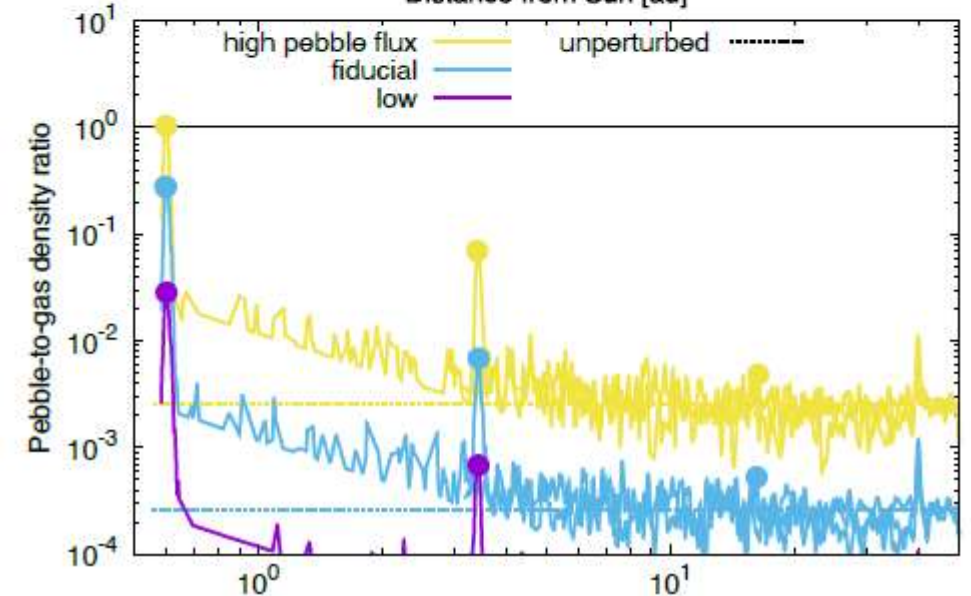
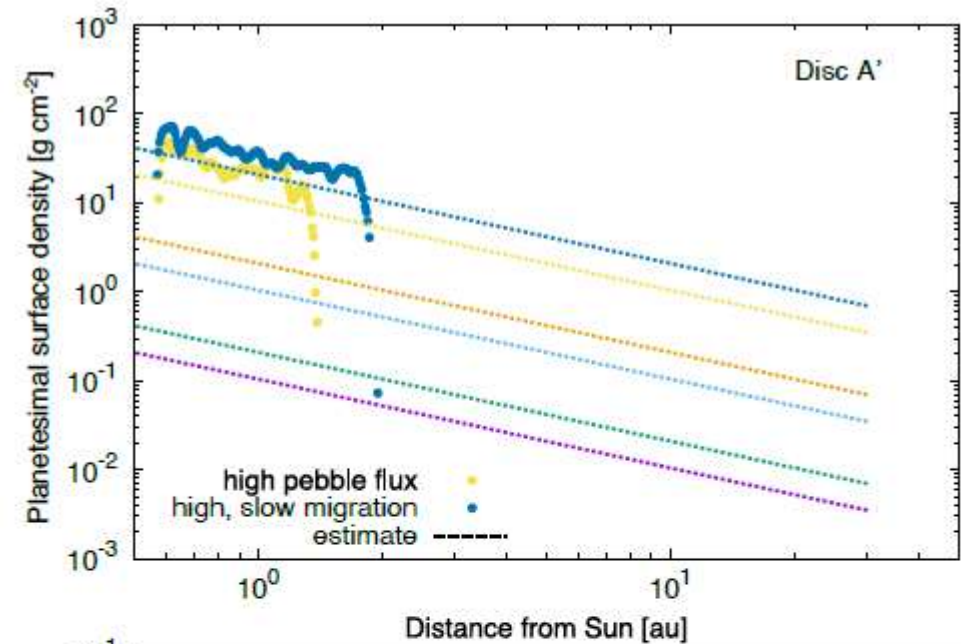
- **Three parameters varied:**
 - Strength of turbulence: α viscosity
 - Stronger turbulence \rightarrow stronger diffusion \rightarrow harder to achieve high pebble-to-gas ratio \rightarrow formation condition harder to meet
 - $\alpha = 10^{-2} \rightarrow$ no planetesimals
 - Mass of protoplanetary disks
 - 10 times heavier gas disk $A' \rightarrow$ higher \dot{M}_{peb} required to produce planetesimals
 - Timescale of streaming instability(not sensitive)



Dependence on turbulence

Parameter study

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10 times heavier disk

Discussions and future work

- **Compare with population synthesis work**
 - Outer boundary of planetesimals depends on thermal structure of the disk
 - planetesimals do not always spread to outermost region of the disk
 - different from what assumed by population synthesis
 - Total mass of the planetesimals are different from population synthesis model
 - need to address detailed pebble growth scheme & planet accretion → Paper II
- **Planetary mass can significantly change the results**
 - Heavier planet can carve a deeper gap → easier to trap planetesimals
 - Type II migration → slower migration speed → higher surface density of planetesimals

[P2] Kepler-419 system

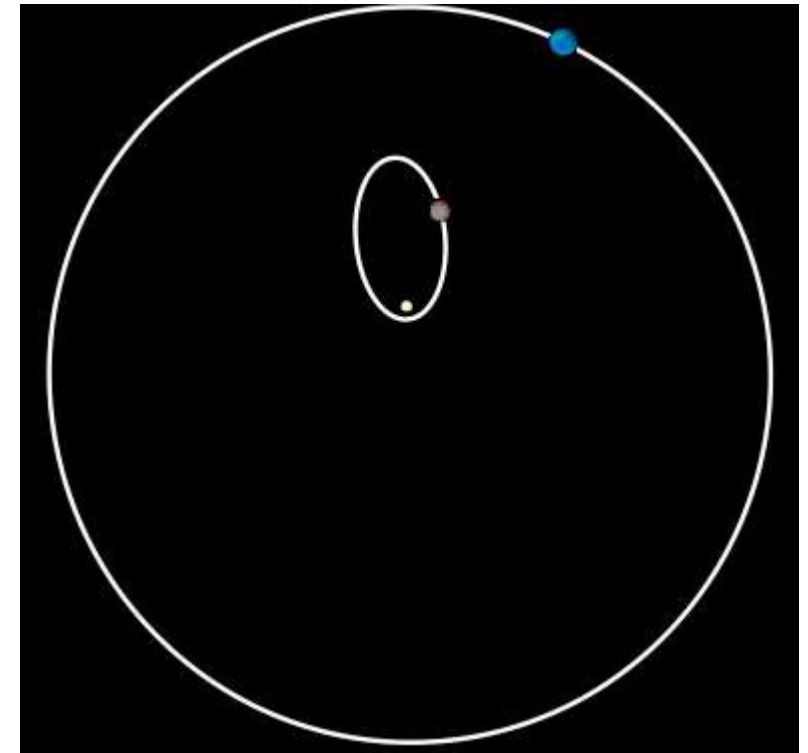
- “A peculiar system hosting two gas giants”

Table 1
Parameters of Kepler-419 Planets

	Planet b	Planet c
Mass m (M_J)	2.77 ± 0.19	7.65 ± 0.27
Semimajor axis a (au)	0.3745 ± 0.0046	1.697 ± 0.02
Eccentricity e	0.817 ± 0.016	0.1793 ± 0.0017
Inclination i (deg)	87.04 ± 0.72	87 ± 2
Arg. of pericenter ω (deg)	94 ± 2.2	275.7 ± 1.8
Long. asc. node Ω (deg)	180 (fixed)	185.4 ± 7.6

Petrovich+19

- $\bar{\omega}_b - \bar{\omega}_c \sim 180^\circ \rightarrow$ apsidally anti-aligned orbits
- Explanation by Petrovich, Wu & Ali-Dib (2019): planets initially inside the inner gap(hole) of a slowly dissipating massive disk \rightarrow force the apses to anti-align
 - Initial angular momentum deficit(AMD) of planet c due to **planet-disk interaction** \rightarrow transfer to planet b
- This paper:
 - Verify the results of PWA+19 as an extension work
 - Constrain & study the disk parameters

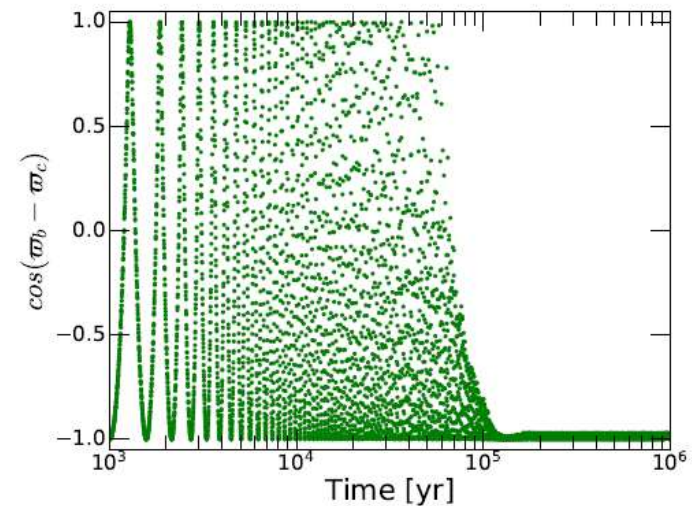
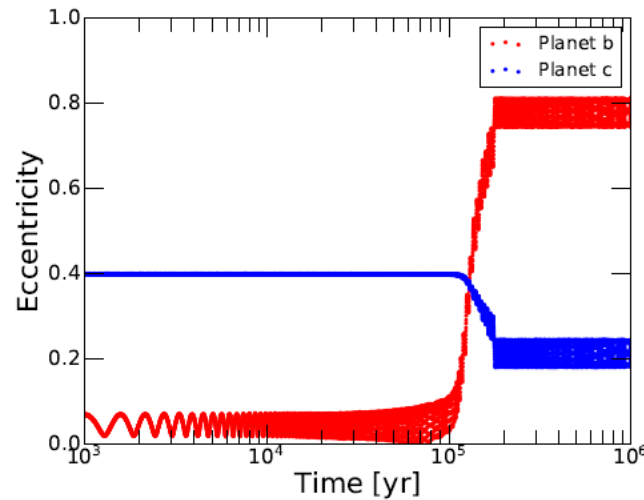
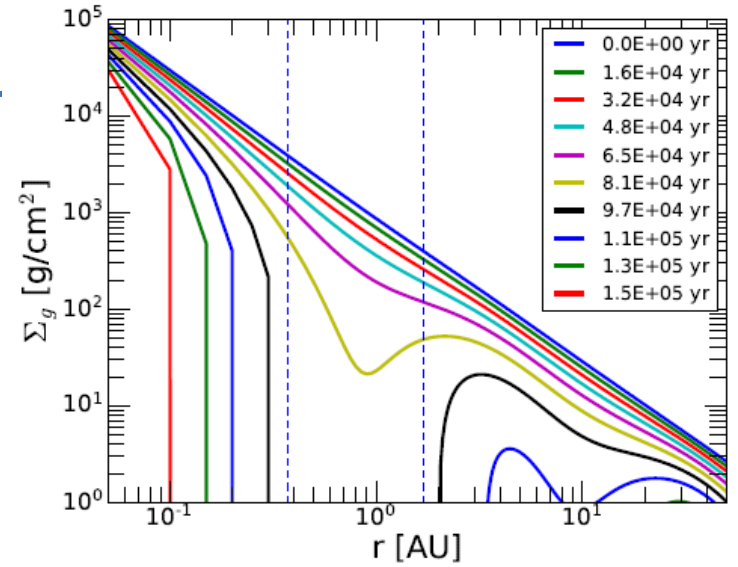


Configuration of Kepler-419 system

Credit: allplanets.ru

Numerical Setup

- Two dimension N-body simulations
 - REBOUND & REBOUNDx
 - Simulation time: 6 Myr
 - Disk potential \rightarrow radial acceleration
- Initial conditions
 - Stellar mass: $1.39M_{\odot}$
 - Two planets: SMA $0.374/1.697 au$, $2.77M_J/7.65M_J$, ini ecc $0.05/0.4$, $\omega_b - \omega_c = 60^{\circ}$
- Disk profile
 - Initial mass $10M_J$
 - $\Sigma(R) = \Sigma_0 \left(\frac{r}{r_{in}}\right)^{-\gamma}$, $r_{in} = 0.05$, $\gamma = -1.5$, outer edge = $50au$
 - Photoevaporation rates adopted from Owen+12; (hydro fitting results)
- Fiducial result



Parameter study

- Now switch to simplified disk decay model:

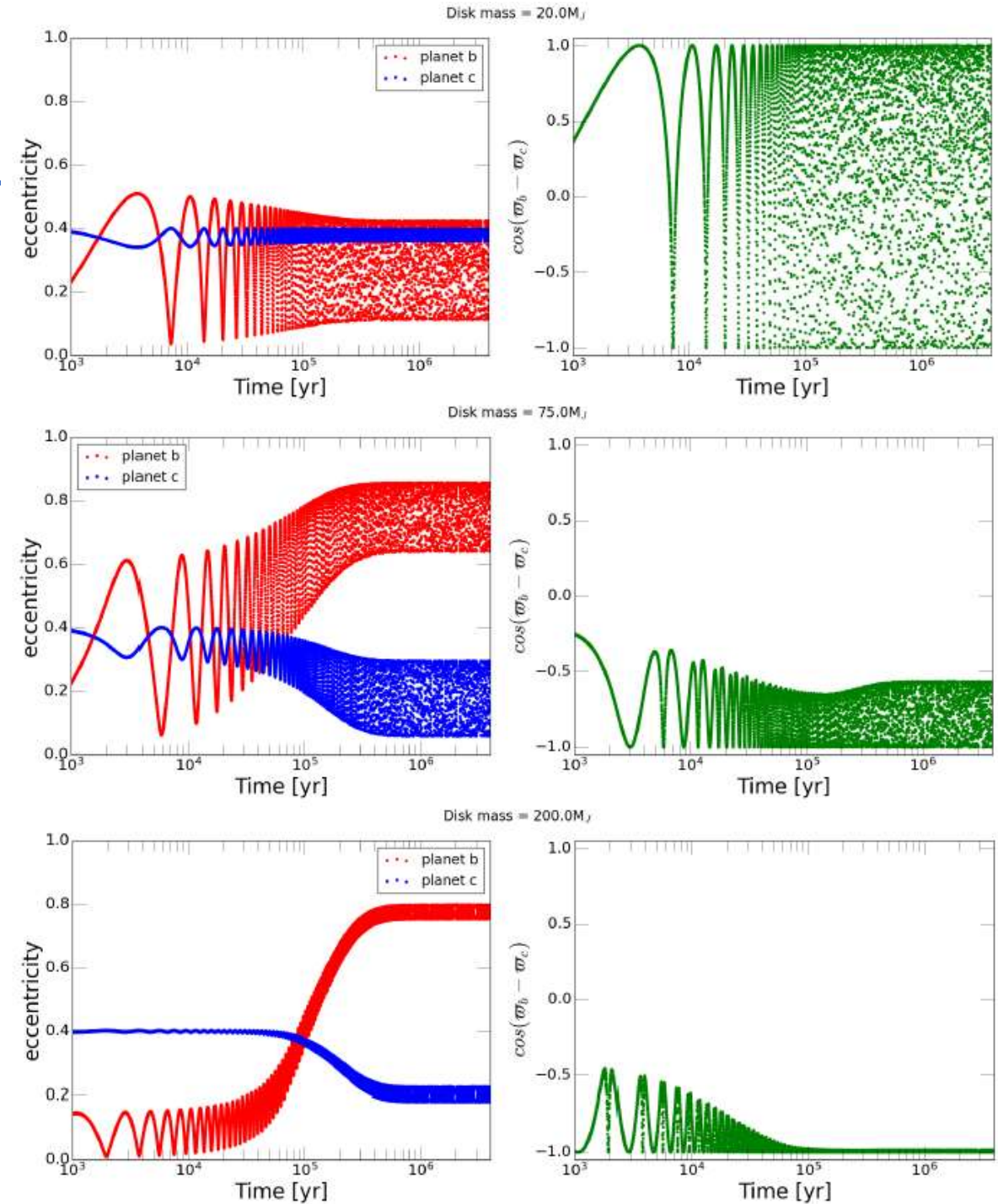
$$M_{disk} = M_{disk}^{t_0} \exp(-t/\tau_d)$$

- Varying two parameters: Disk mass and disk's dispersal time scale

- Mass: 1, 20, 40, 50, 75, 100, 200 M_J
- τ_d : $10^4, 10^5, 10^6$ year

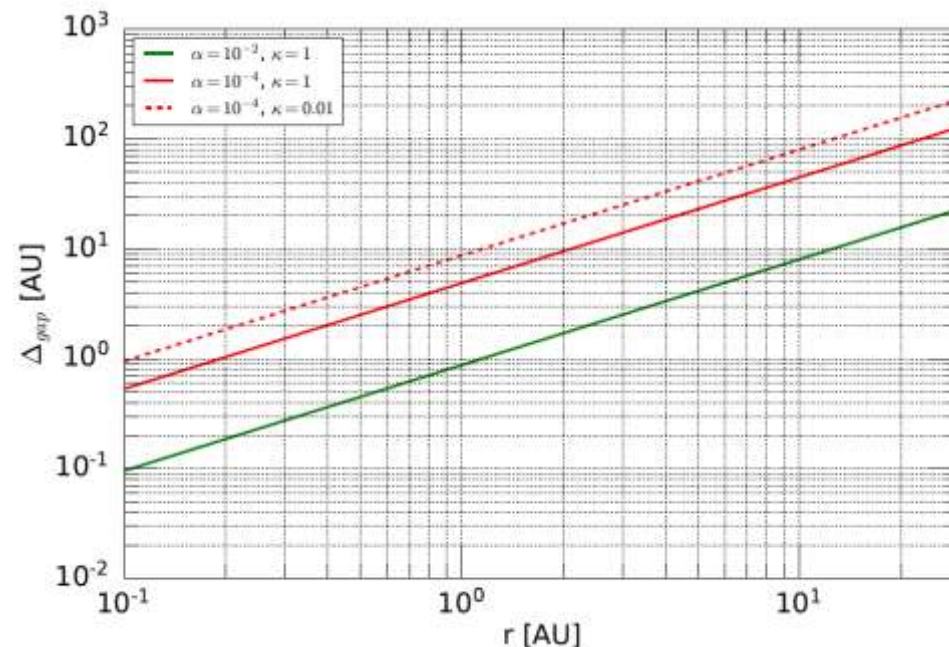
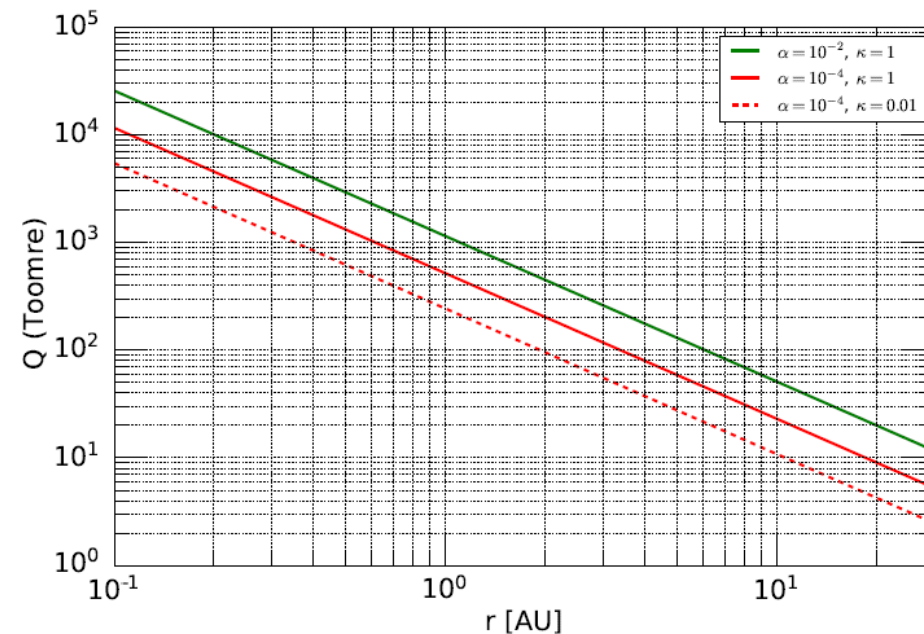
- Results

- $M_{Disk} \leq 20 M_J$ (not recover): disk-planet interaction too weak, nearly three body problem
- $M \sim 40 - 50 M_J$ (not consistent): oscillates with large amplitude
- Larger mass (recover): libration around anti-alignment, AMD transferred from c to b
- All disk dispersal time lead to similar results



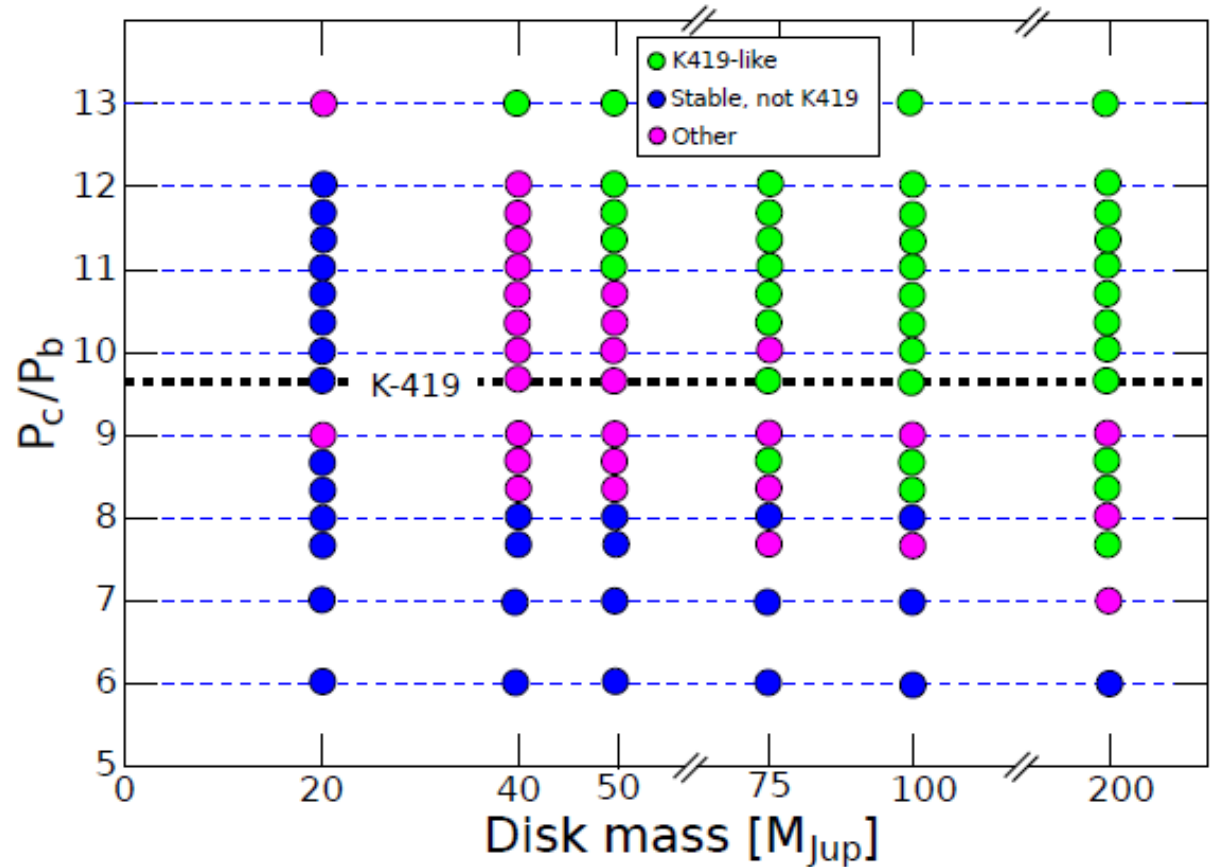
Is the required disk realistic?

- Disk mass $\geq 75 M_J$. **Any observational counterparts?**
 - GM Aur and DM Tau, possibly TW Hya($50M_J$)
 - Transition disks: 7% $\geq 100 M_J$
- **Is the disk gravitationally stable?**
 - Toomre Q value(< 1 means unstable)
 - Everywhere in the planet forming region($< 30\text{au}$) is stable
 - Suggest planets are formed via core acc
- **Can planets open gaps?**
 - Both of the planets can open gaps
 - Gaps will merge to a common gap, even for large α case



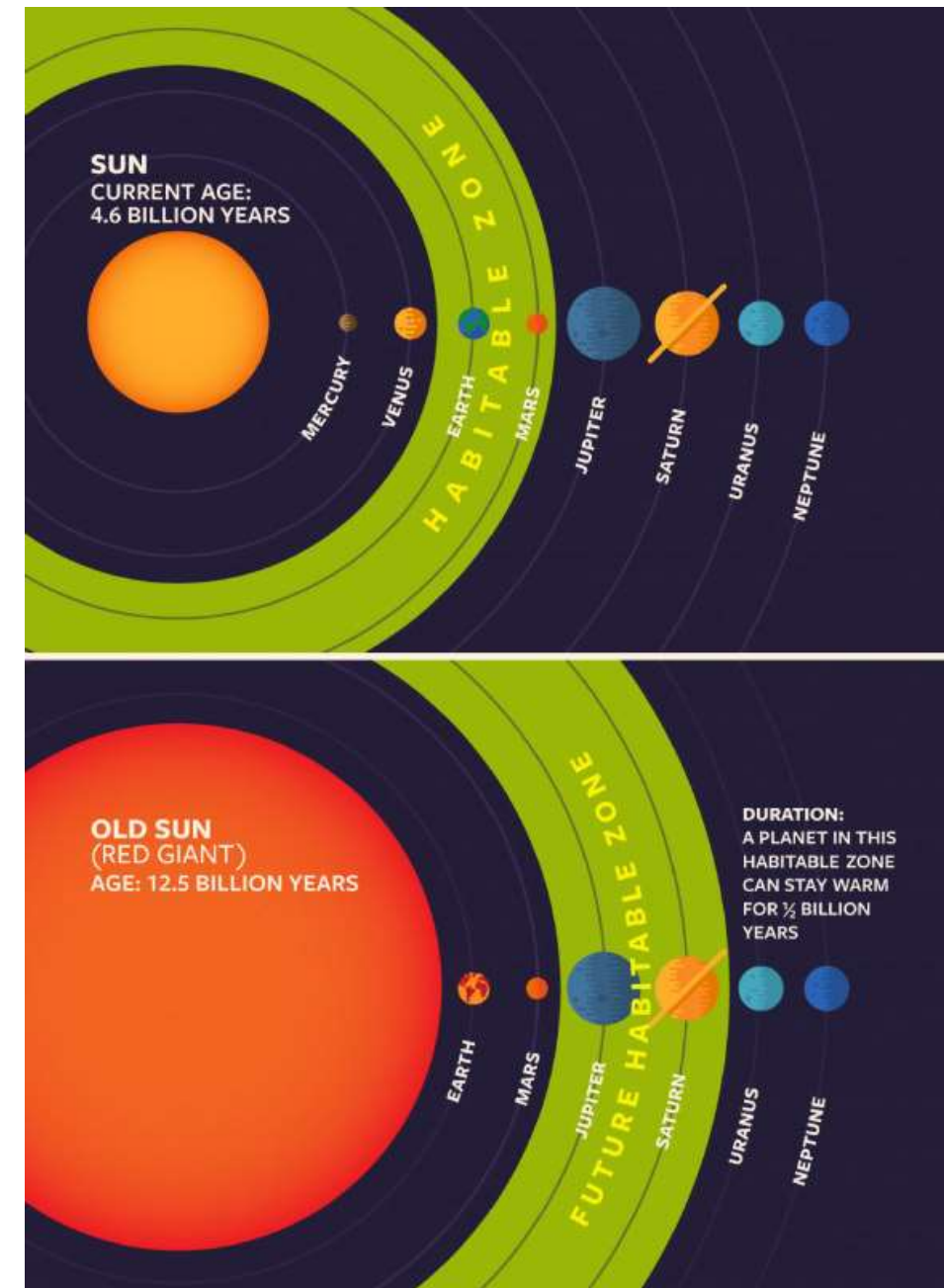
Sensitivity to Planet c

- If Kepler-419 formed by accretion + migration, the assumed architecture is fine-tuned?
 - Need to consider alternative positions of planet c
- Vary the orbits of planet c
 - Fiducial: $P_c = 9.6 P_b$
 - Survey range $6 - 13 P_b$
 - $\tau_d = 10^5 \text{yr}$, and same range of disk mass
- Results
 - **BLUE:** stable, but trapped in other MMR(6:1, 7:1, 8:1)
 - **Pink:** Plethora of behaviours; dynamically noisy
 - **Green:** Kepler-419 like system
- Conclusion:
 - Higher order MMR does not trap planets to become K-419-like systems → such system can be more common than expected



[P3] Apocalyptic fate of planets

- The sun will eventually become a red giant with $R \sim$ earth orbit, and then white dwarf.
 - Inner planets $< 1\text{au}$: engulfed and vaporized.
 - But how about outer planets around 1-10 au?
- Observation
 - > 100 gas giants are discovered around red giants
 - Clues show planets(or debris) exist around white dwarfs: metal absorption lines
- Need to model planetary systems beyond main sequence
 - Previous studies: only concern about the surviving condition of a **single planet**
 - **This work:** two planets, one inner Neptune and one outer Jupiter, with stellar mass loss, stellar tides, and mutual gravitational interactions



Credit: Cornell University

Model

- Change of semi-major axis

$$\left(\frac{\dot{a}}{a}\right) = \left[\left(\frac{\dot{M}_*}{M_* + M_p}\right) - \left(\frac{\dot{a}}{a}\right)_t\right]$$

Typo

- Stellar tides

$$\left(\frac{\dot{a}}{a}\right)_t = -\frac{1}{9\tau_{\text{conv}}} \frac{M_*^{\text{env}}}{M_*} \frac{M_p}{M_*} \left(1 + \frac{M_p}{M_*}\right) \left(\frac{R_*}{a}\right)^8 \times \left[2p_2 + e^2 \left(\frac{7}{8}p_1 - 10p_2 + \frac{441}{8}p_3\right)\right]$$

M_*^{env} : envelope mass

τ_{conv} : eddy turnover timescale

P_i : frequency components

- Eccentricity damping

$$\left(\frac{\dot{e}}{e}\right)_t = -\frac{1}{36\tau_{\text{conv}}} \frac{M_*^{\text{env}}}{M_*} \frac{M_p}{M_*} \left(1 + \frac{M_p}{M_*}\right) \left(\frac{R_*}{a}\right)^8 \times \left[\frac{5}{4}p_1 - 2p_2 + \frac{147}{4}p_3\right]$$

$$p_i \approx \frac{9}{2} \min \left[1, \left(\frac{4\pi^2 a^3}{i^2 G (M_* + M_p) \tau_{\text{conv}}^2} \right) \right], i = 1, 2, 3.$$

- Stellar evolution code SSE

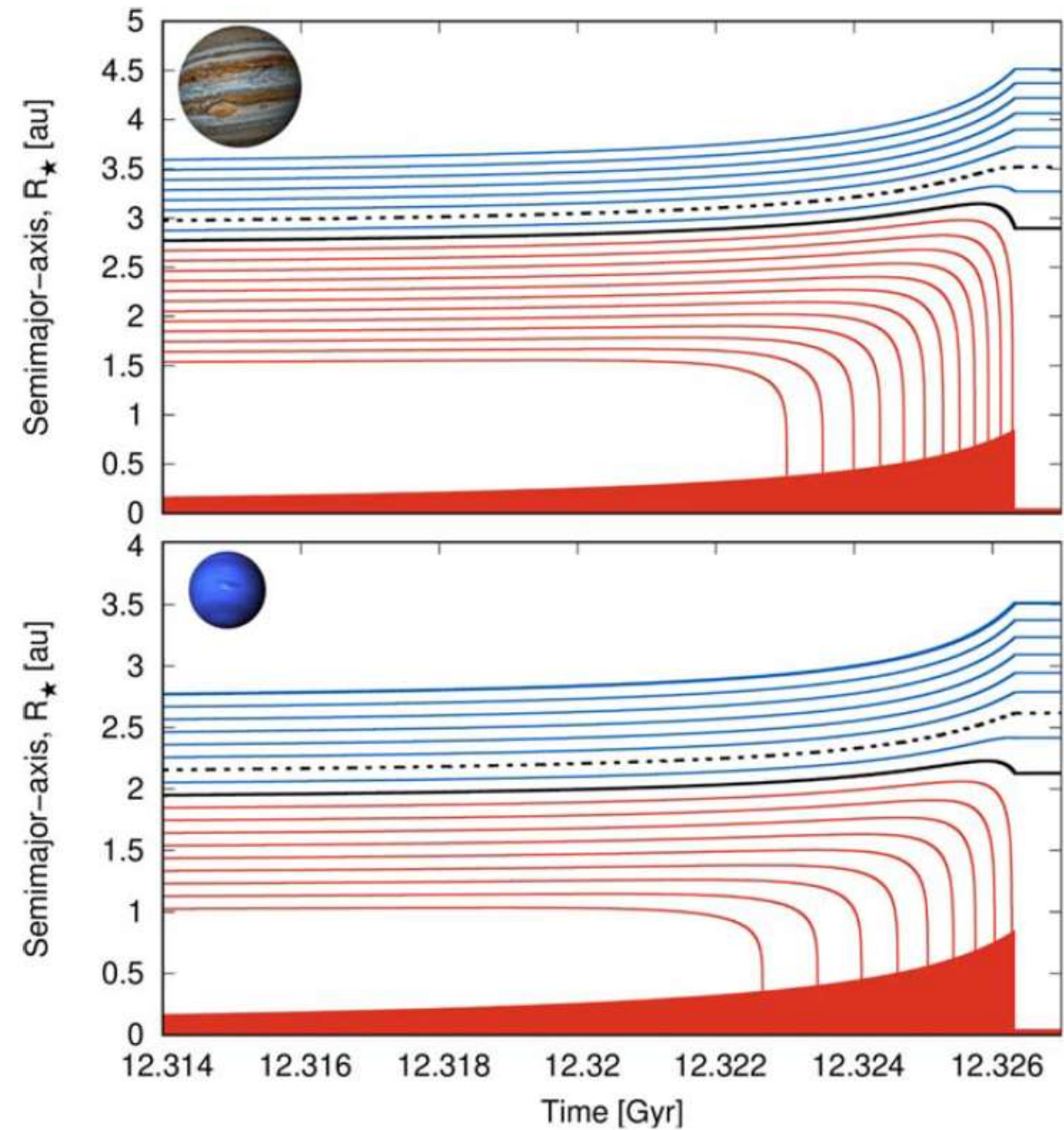
- Stellar mass = $1M_\odot$, $Z = 0.02$
- Evolution track will give out $M_*, R_*, M_*^{\text{env}}, R_*^{\text{env}}, L_*$

Tidal

Mass loss

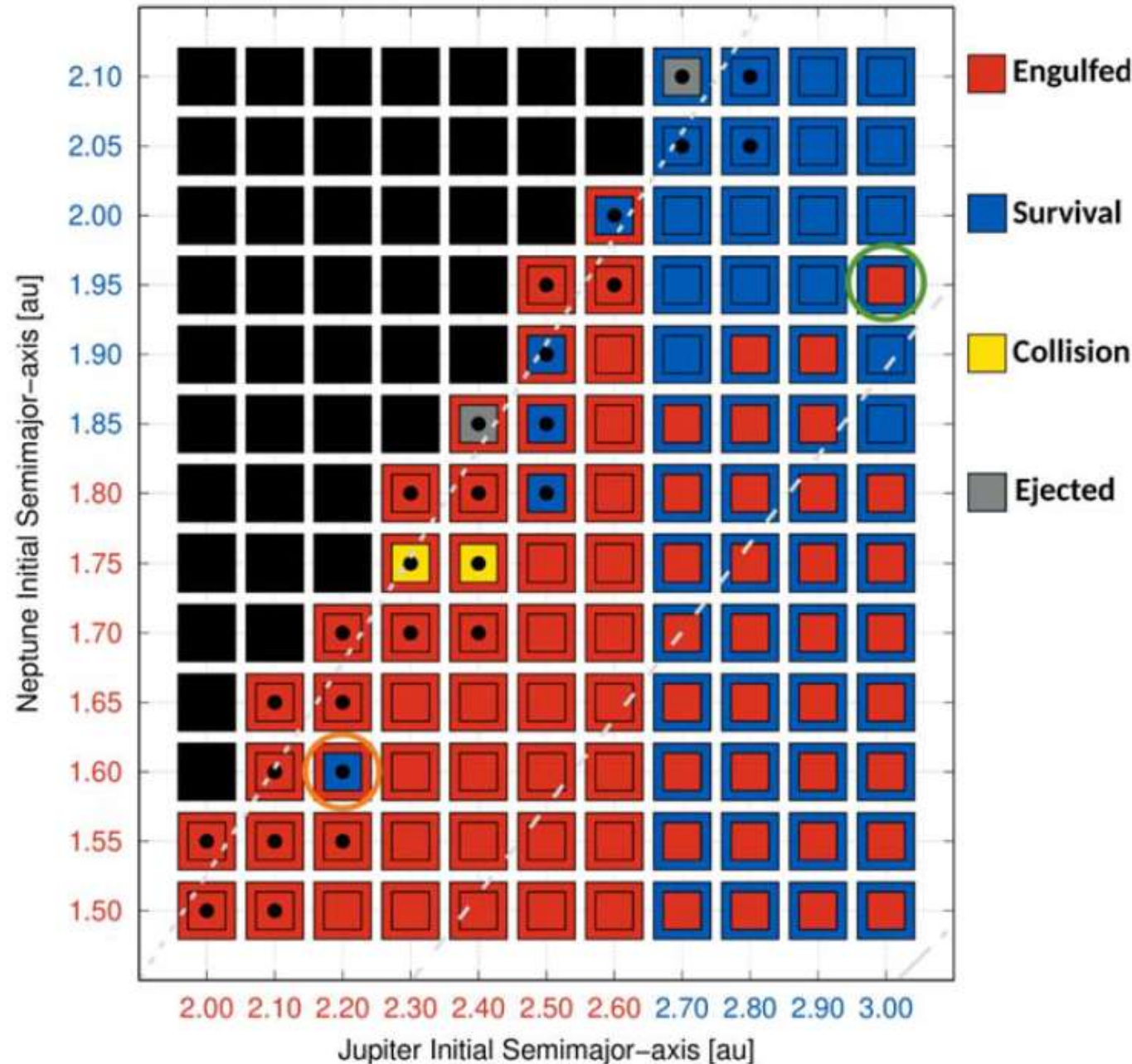
Evolution of single planets

- Initial position
 - Jupiter: 1.5 – 3.5 *au*
 - Neptune: 1.0 – 2.7 *au*
 - Survival conditions
 - Jupiter ≥ 2.7 *au*
 - Neptune ≥ 1.9 *au*
- agree with most of the previous studies



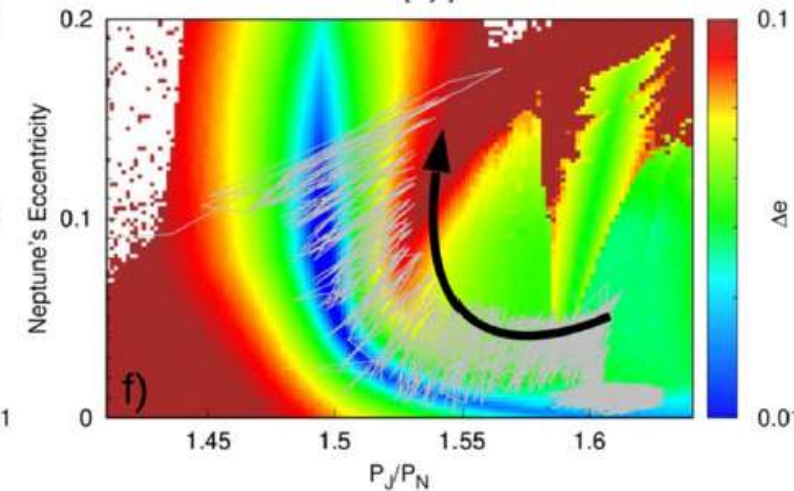
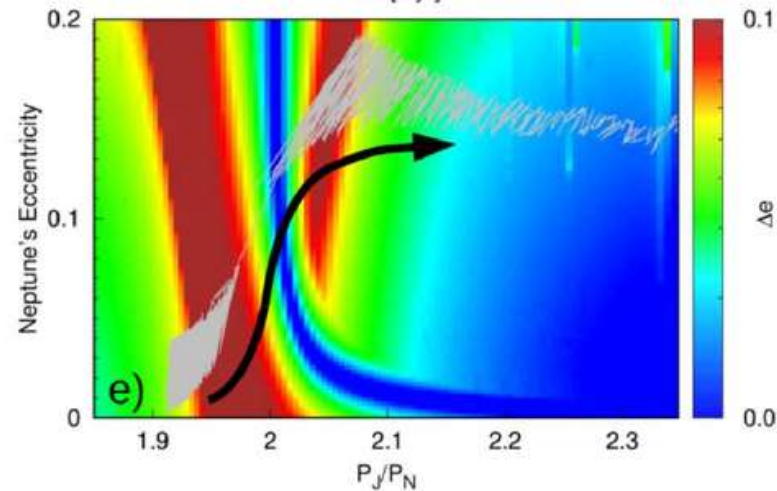
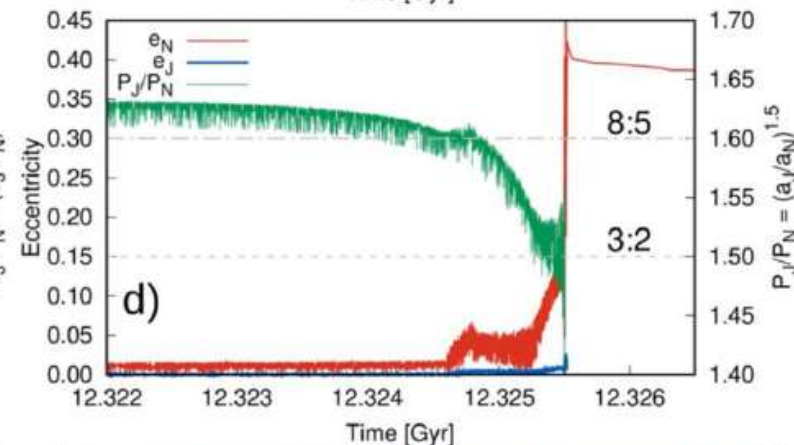
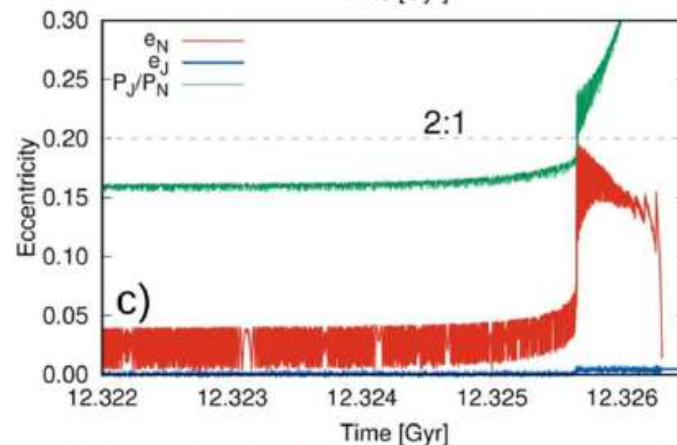
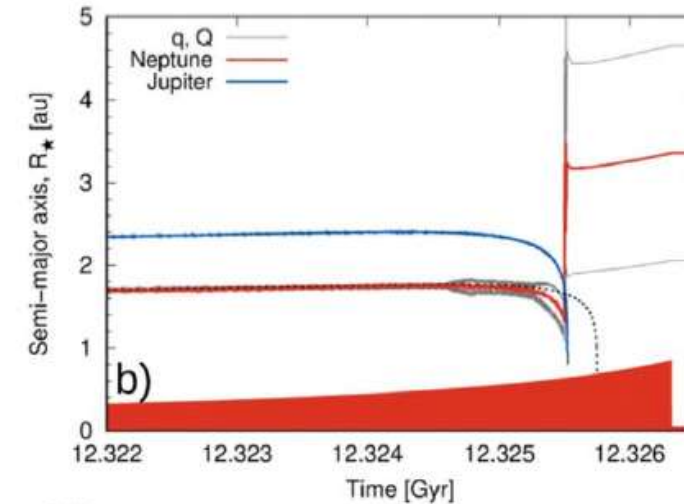
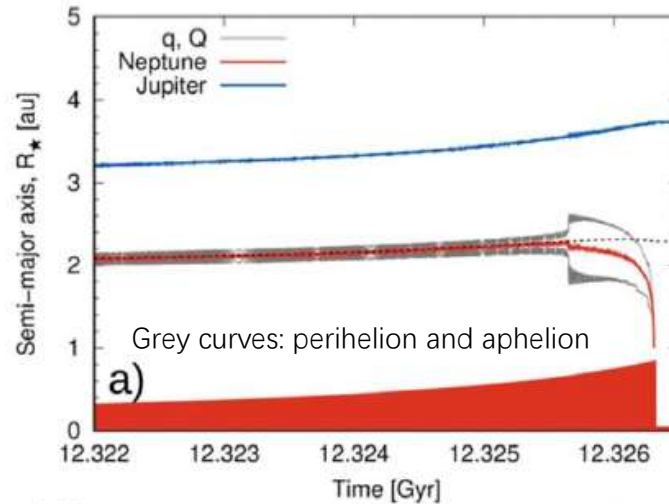
Multi-planetary case

- Integration time: 750 Myr, starting from 11.6 Gyr
- Final fate of the planets
 - Large square: Jupiter
 - Small square: Neptune
 - Black dot: close encounter 3H
 - Yellow: collision
 - Dashed lines: 2:1 & 3:2 MMR
 - Filled black: unstable
- Majority of the Neptunes are engulfed
- Two cases: fates are changed!
 - **Orange**: although $a_{nep} < 1.9$, the Neptune survives
 - **Green**: although $a_{nep} > 1.9$, the Neptune is engulfed



Two cases in details

- Left: “Destroyer” case
 - Jup: 3.0 au, Nep:1.95 au
 - Divergent migration: P ratio increases → instability happens when 2:1 resonance is crossed
 - Sudden increase e_{Nep} → Perihelion distance shrinks → tides more effective
- Right: “Savior” case
 - Jup: 2.2 au, Nep: 1.6 au
 - Convergent: P ratio decreases → Jupiter falls in, with Neptune scattered out
- Bottom are dynamical maps:
 - 100x100 grid
 - Integrated to 10^4 year

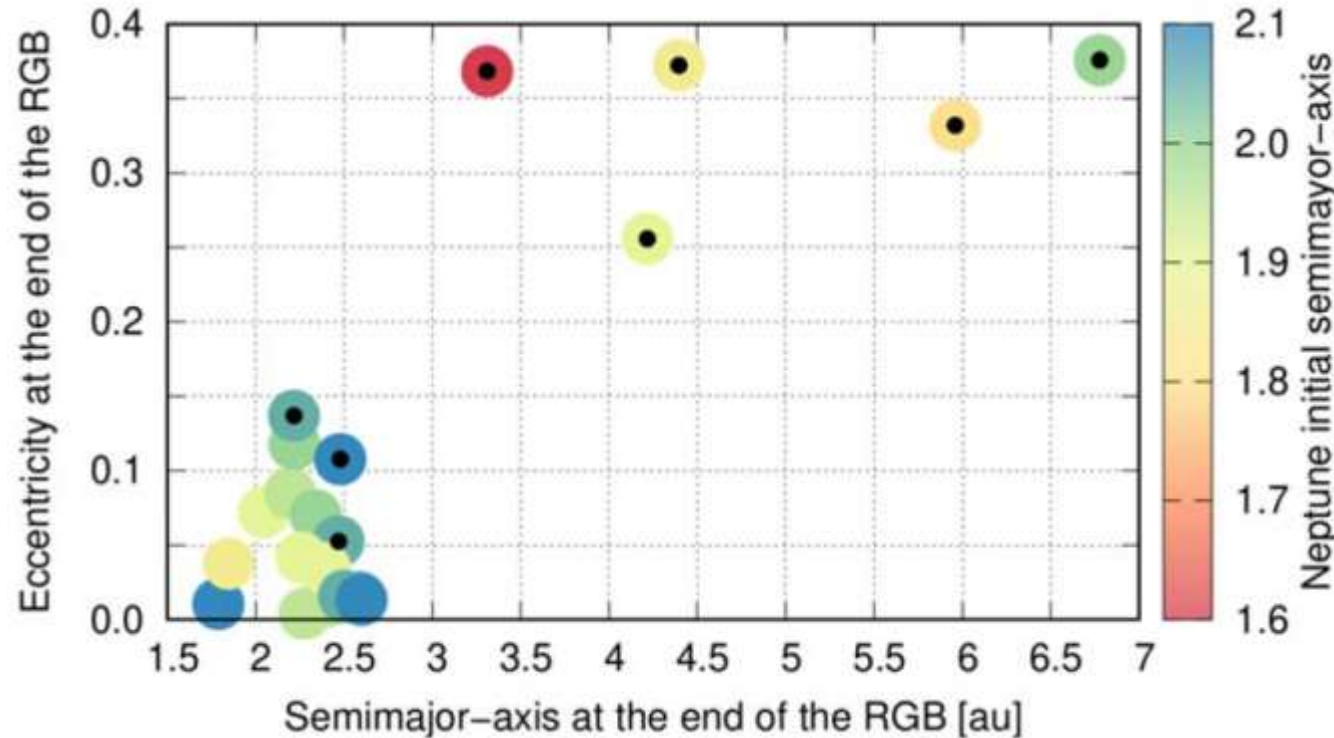


Survivors

- Two groups of the Neptunes can survive:
 - High eccentricity with significant scattering (like the example case)
 - Low eccentricity, relatively large initial SMA

Implications

- A significant fraction of the planetary systems around white dwarfs might be shaped by gravitational interactions, particularly resonance
- Planets in such eccentric orbits can scatter planetesimals/asteroids → metal pollution



*Black dots means the Neptune has undergone significant close encounter with the Jupiter