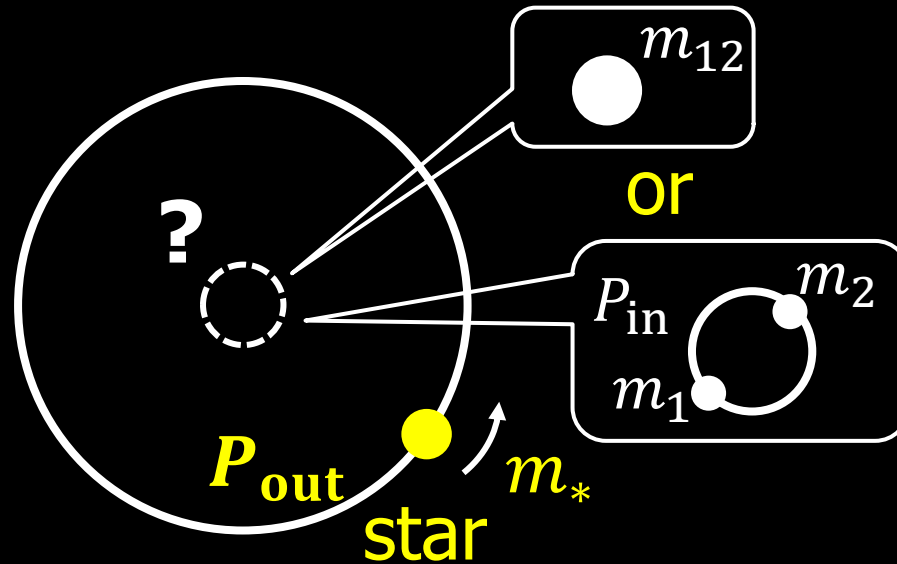


Dynamics of a triple system comprising an inner binary black hole in a mutually inclined orbit



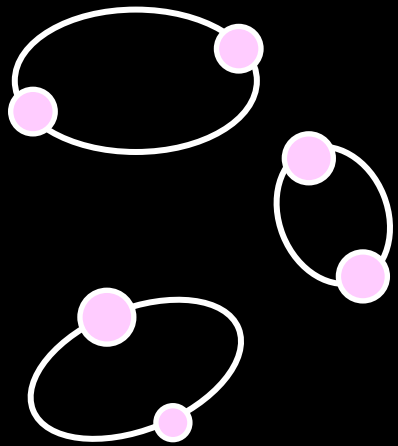
Yasushi Suto

Department of Physics & Research Center for the Early Universe, The University of Tokyo

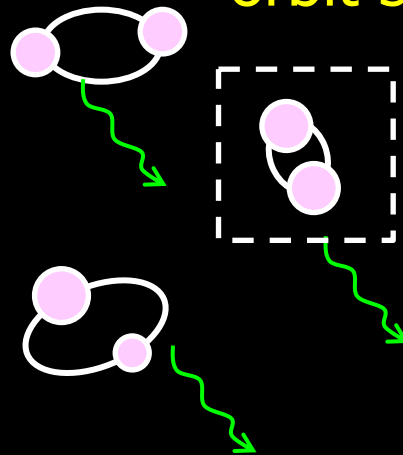
12:00 July 6, 2023. Kavli-IAU Symposium 382 "Complex Planetary Systems II"
@ University of Namur, Belgium

Generic picture of binary BH evolution

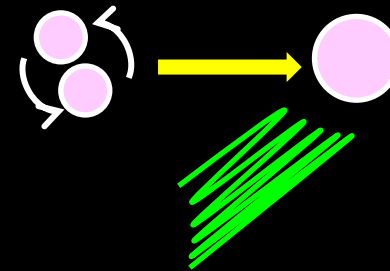
binary blackholes form in wide orbits



orbit shrinking

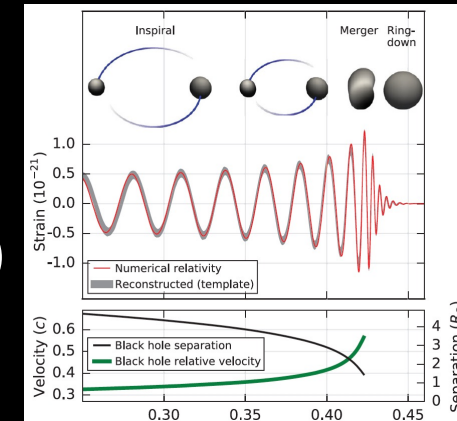


merger



strong GW

weak GW (low-frequency)



LIGO/Virgo

BBHs would spend longer time in wide orbits before merging

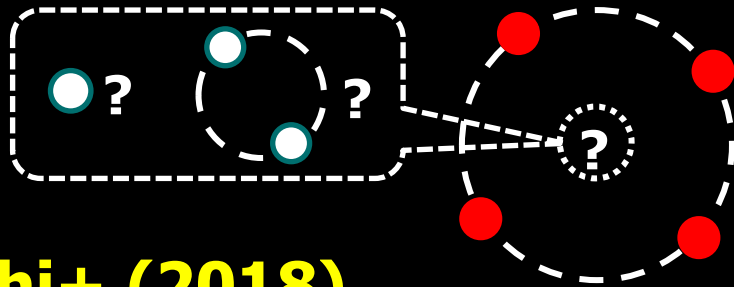
Abundant longer orbital-period BBHs may remain undetected (e.g. ~ 10 day orbital period $\sim 10^{-6}$ Hz).

Other detection strategies complementary to GW ?

Proposals to search for star-BH binaries

Gaia mission (2013-)

Astrometry of stars in Galaxy
~ 10^9 stars eventually
RV with 200-350m/s precision
for brightest stars (Katz 2018)



Yamaguchi+ (2018)

5-year mission may detect
200-1000 star-BH binaries

Tanikawa+(2023)

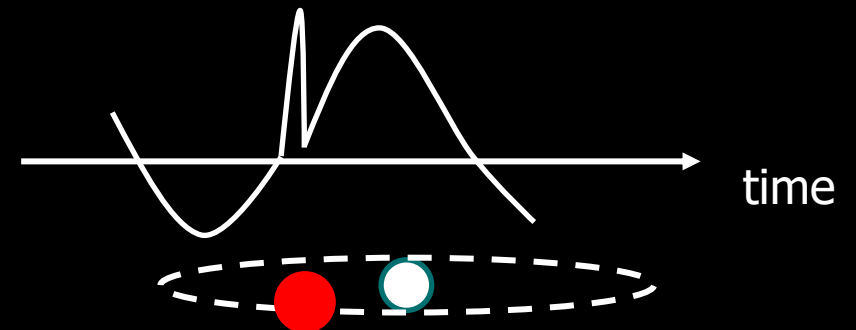
**Some of them may be indeed a star-binary BH triple!
Can precise radial velocity follow-ups unveil the inner BBH?**

TESS mission (2018-)

photometry of nearby stars (~ 12mag)
transit planets

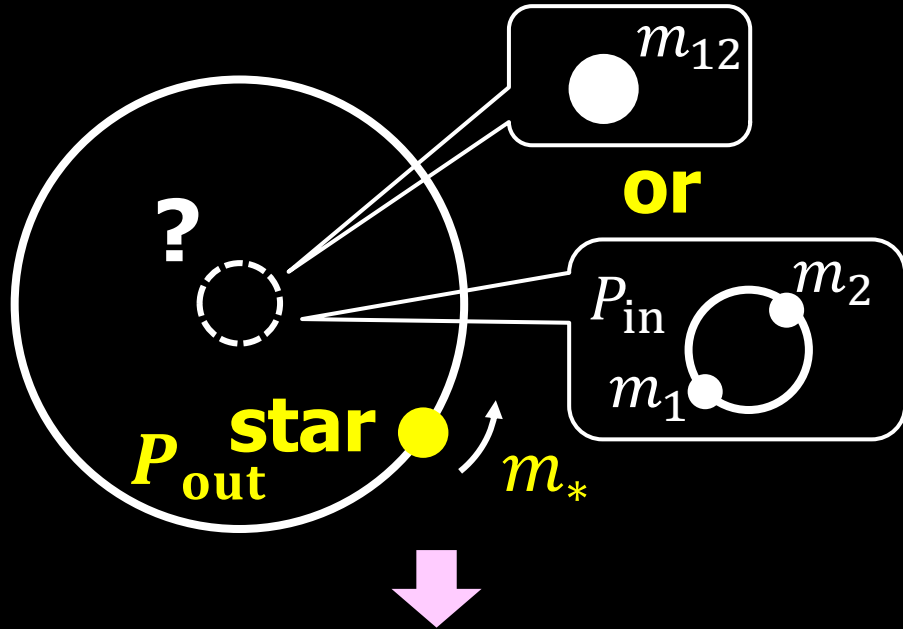
Masuda & Hotokezaka (2019)

Light curve modulation
(relativistic effects, tidal deformation)
⇒ (10 – 100) star-BH binaries may be
identified

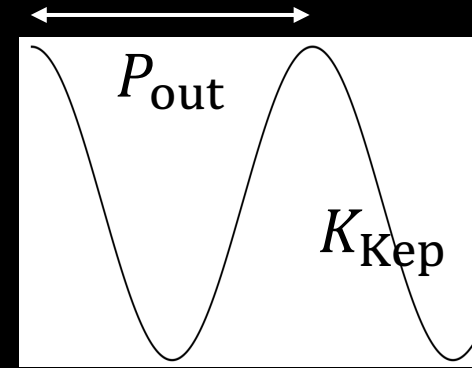


RV (radial velocity) modulations of a tertiary star

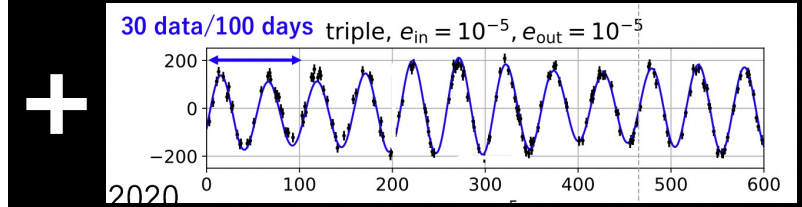
Morais & Correia (2008, 2012) ⁷



(i) short-term



$$\text{Amp} \sim K_{Kep} \left(\frac{P_{in}}{P_{out}} \right)^{\frac{7}{3}}$$



period $\sim P_{in}/2$

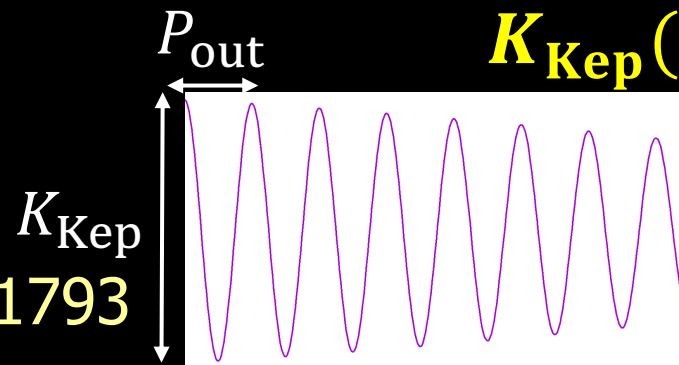
Kepler motion + Short-term RV variations (inner-binary perturbation)

Keplerian motion RV + RV modulations of a tertiary star due to a hidden inner binary

(ii) long-term for non-coplanar triples

Inclination $I_{out}(t)$ modulated in the ZKL timescale

$$K_{Kep}(t) = K_0 \sin I_{out}(t)$$



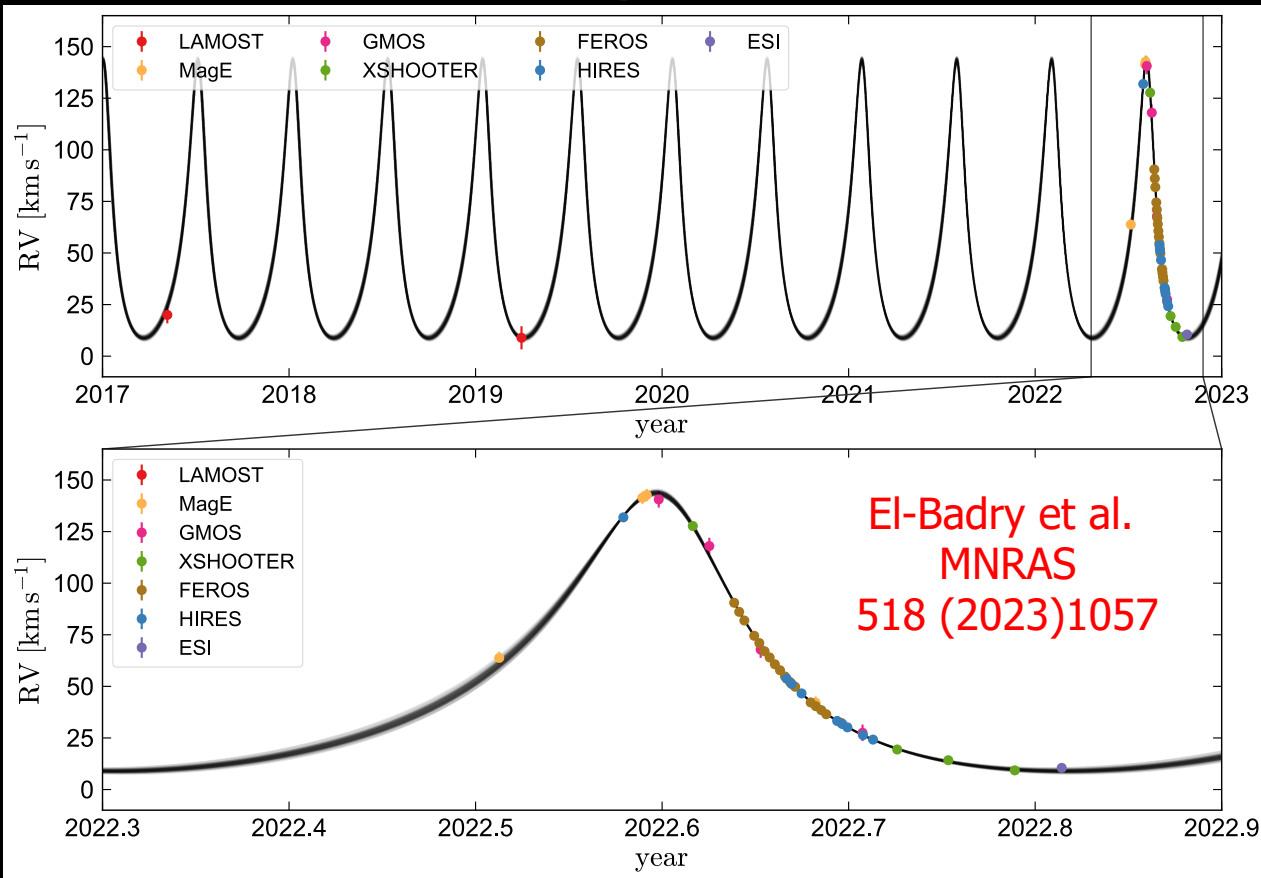
semi-amplitude of Kepler RV varies over longer timescales

Hayashi, Wang + YS: ApJ 890(2020)112
 Hayashi + YS: ApJ 897(2020)29
 Hayashi, YS + Trani (2023): arXiv:2307.01793

A proof-of-concept study with Gaia star-BH candidates

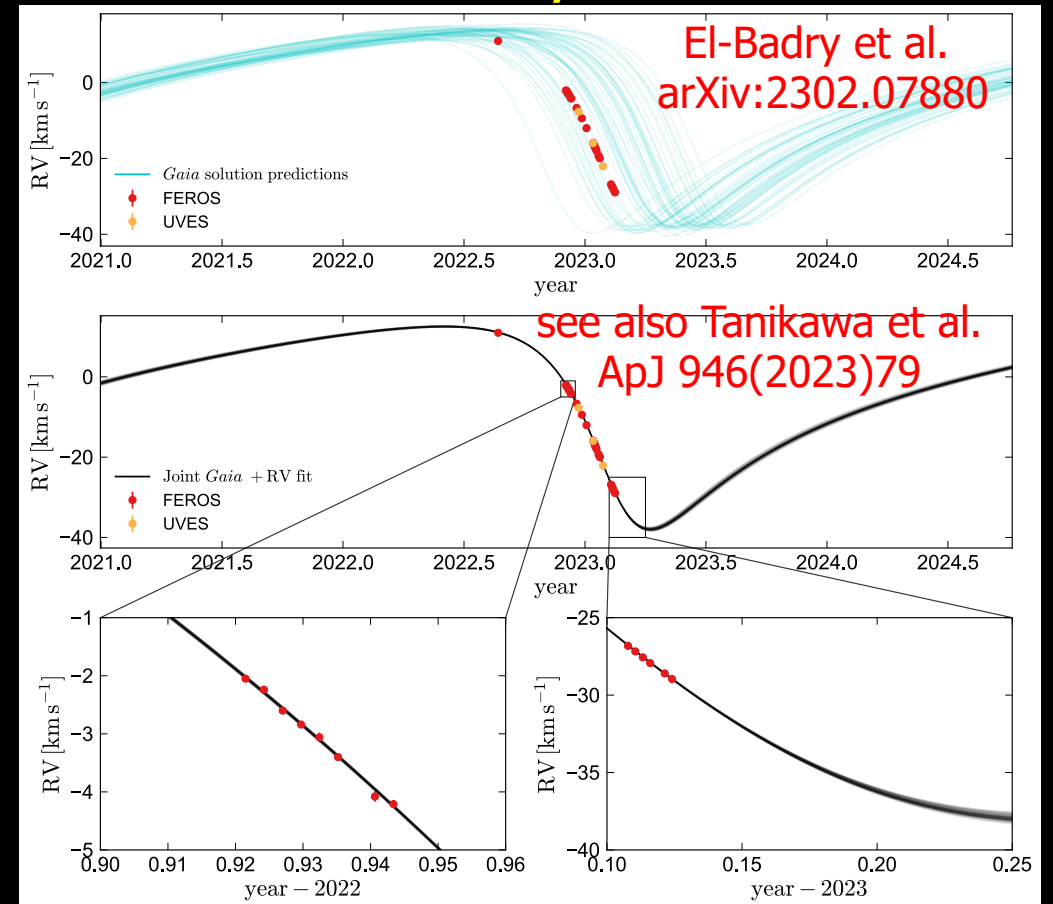
Gaia BH-1

$0.93M_{\odot}$ G star + $9.6M_{\odot}$ BH
($P_{\text{orb}}=186$ days) at $d=477$ pc
eccentricity ~ 0.45



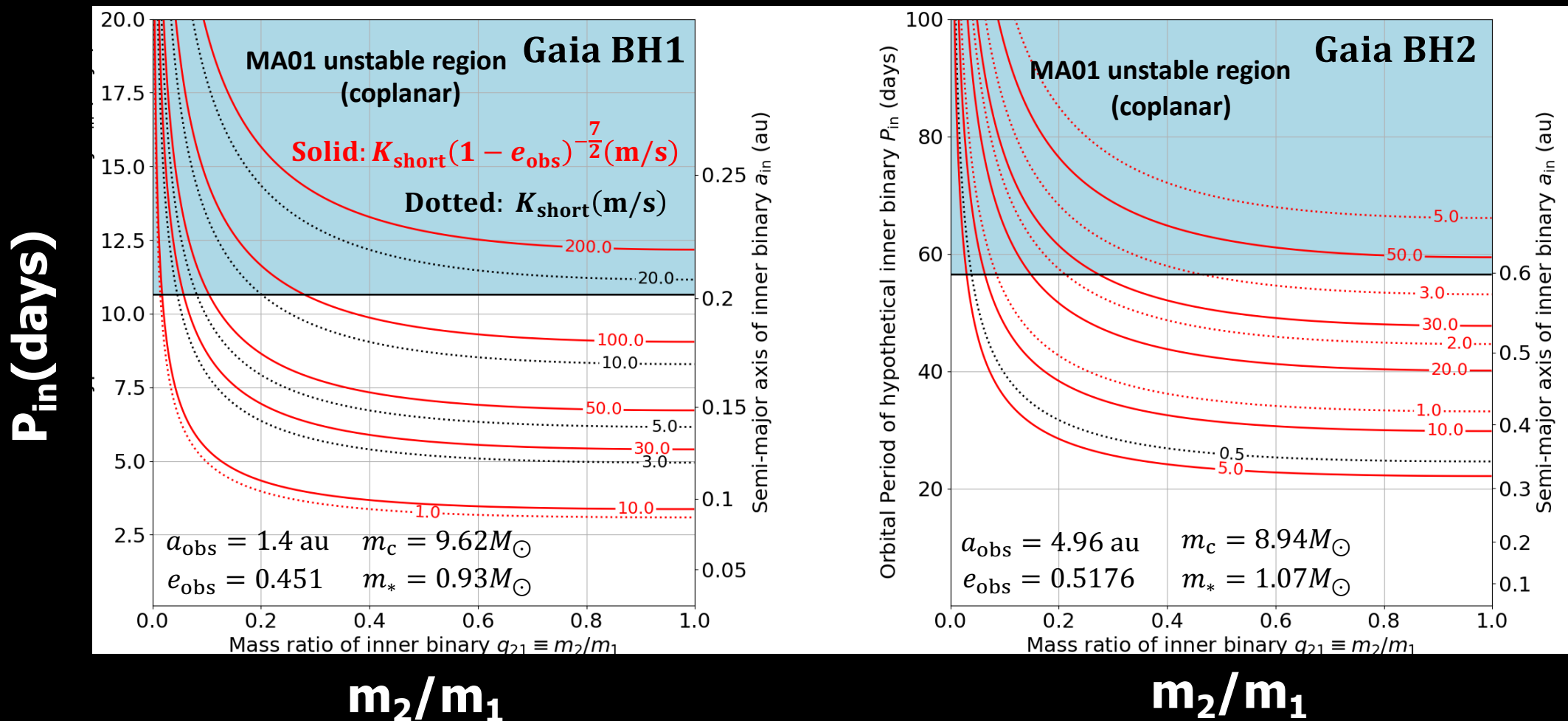
Gaia BH-2

$1M_{\odot}$ red giant + $9M_{\odot}$ BH
($P_{\text{orb}}=1277$ days) at $d=1.16$ kpc
eccentricity ~ 0.52

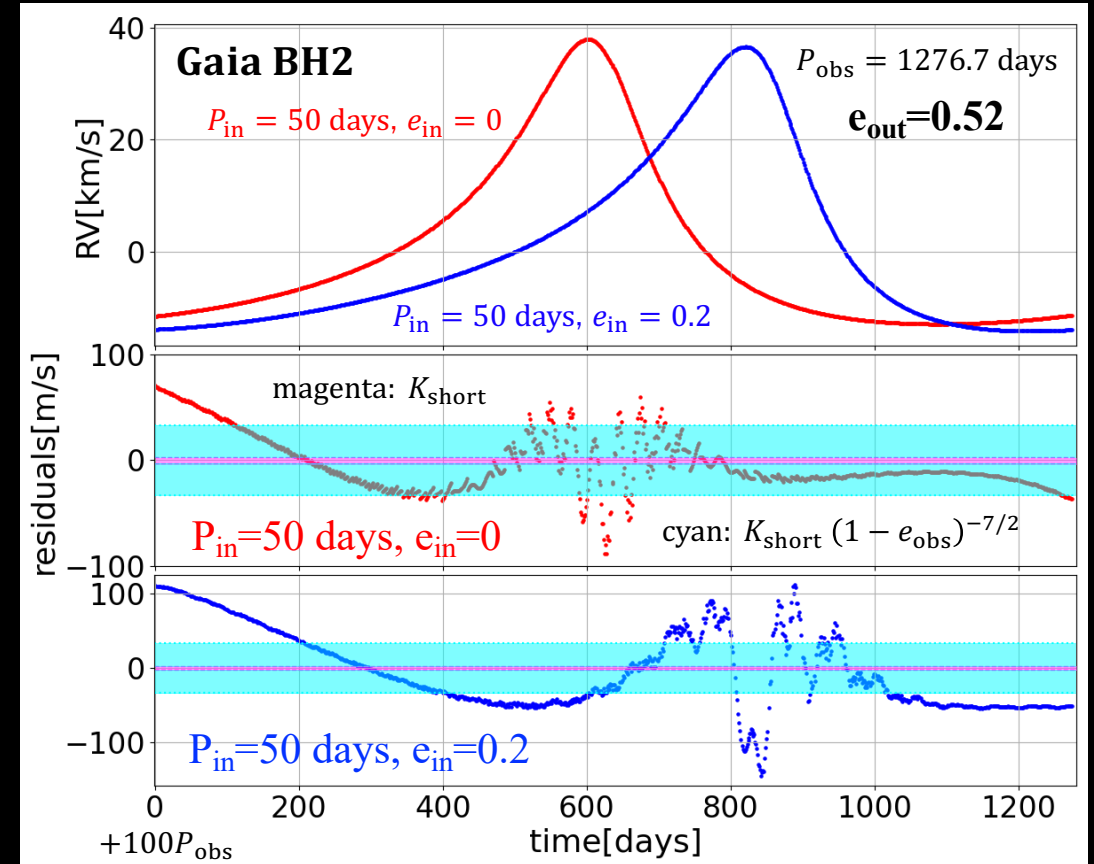
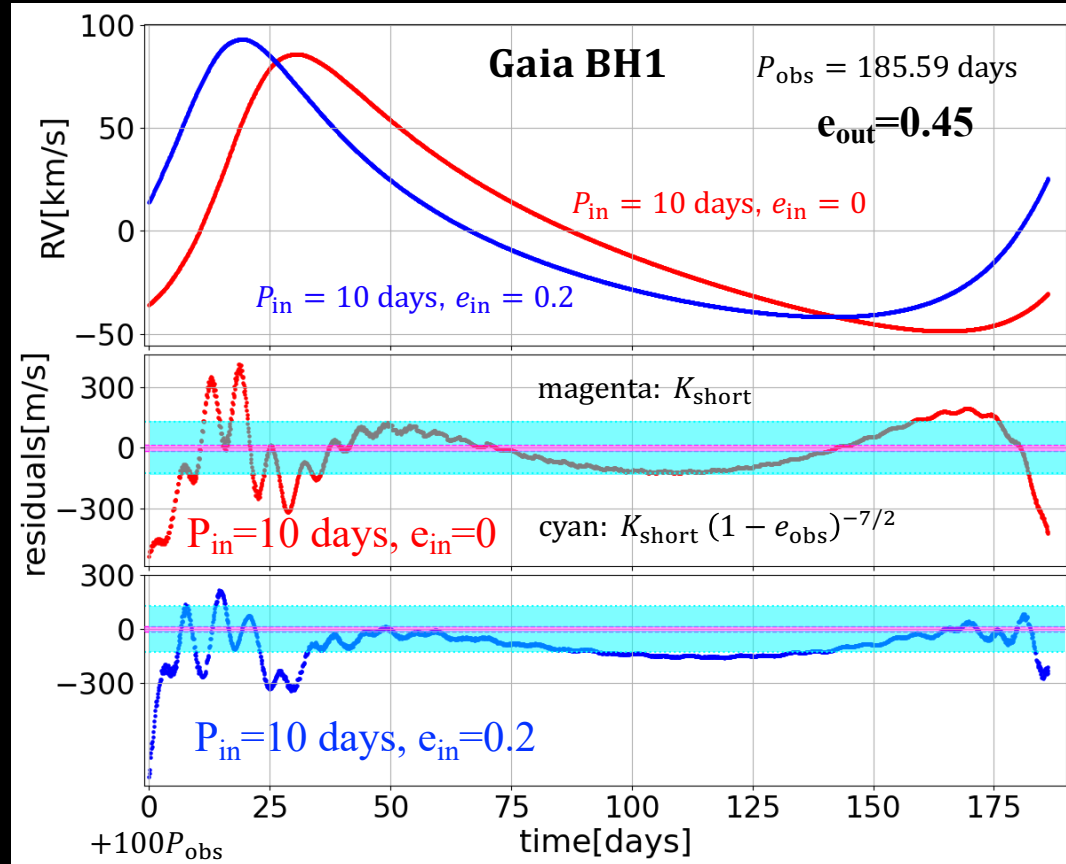


Short-term RV modulations expected from analytic approximation (coplanar + circular tertiary)

Contours of expected semi-amplitudes of short-term RV modulations:
~ (1-100) m/s for coplanar outer orbits (Hayashi, YS + Trani 2023)

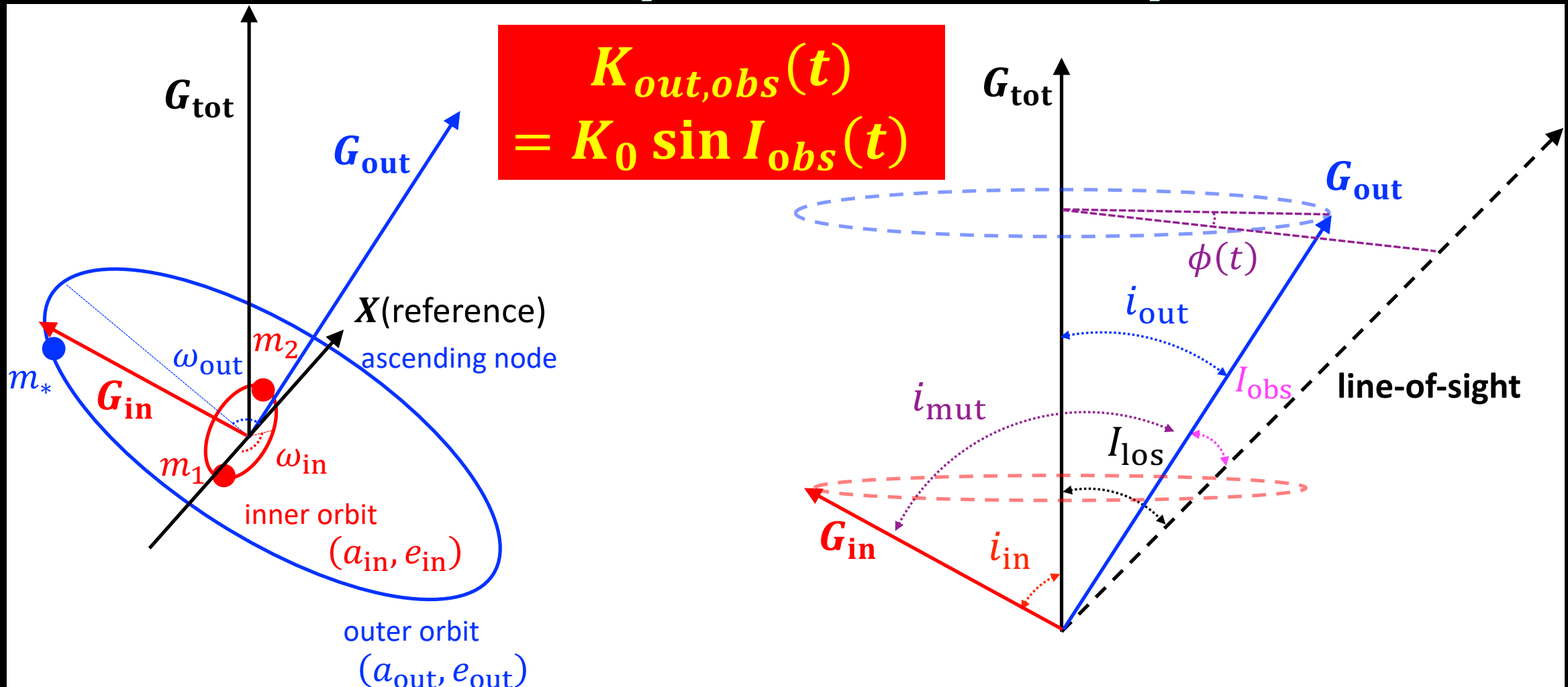


Short-term RV modulations from direct three-body simulation (coplanar + tertiary with observed eccentricity)



- Due to the outer eccentricity, the amplitude of the short-term RV modulations becomes (10-100) times larger at the pericenter passage than the analytic estimate for circular outer orbits

Long-term RV modulations due to nodal precession and ZKL (von Zeipel-Kozai-Lidov) oscillations for non-coplanar inclined triples



Evolution of inclination for non-coplanar triples

$t = 0P_{\text{out}}^{(0)}$

$t = 0P_{\text{out}}^{(0)}$

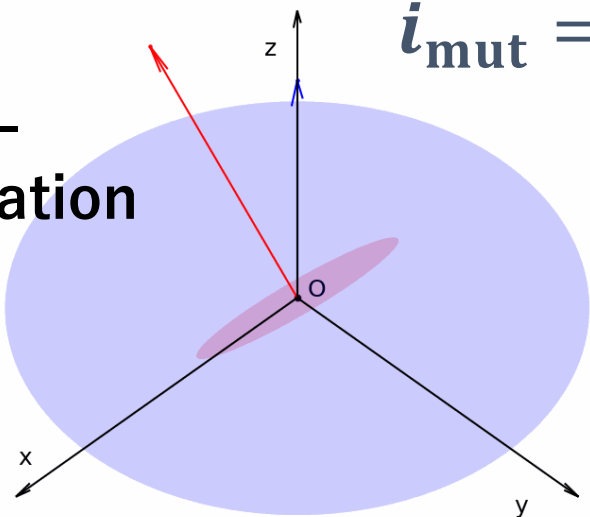
$i_{\text{mut}} = 45^\circ$

$i_{\text{mut}} = 90^\circ$

strong Kozai-Lidov oscillation

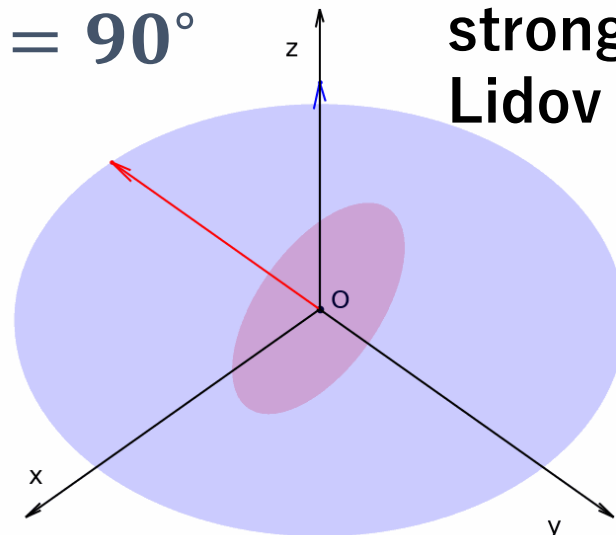
weak Kozai-Lidov oscillation

⇒ small-amplitude nodal precession



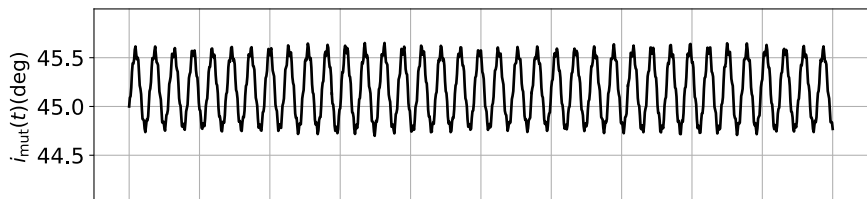
Hayashi + YS: ApJ 897(2020)29

$$K_{\text{Kep}} = K_0 \sin I_{\text{out}}(t)$$

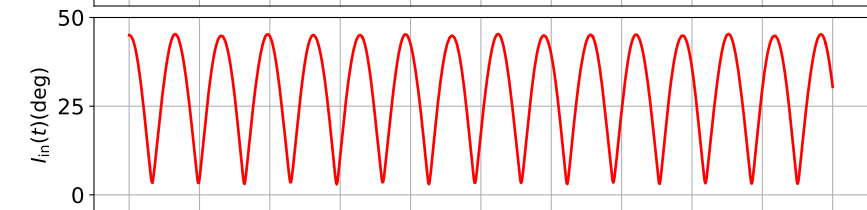


⇒ large-amplitude sporadic precession

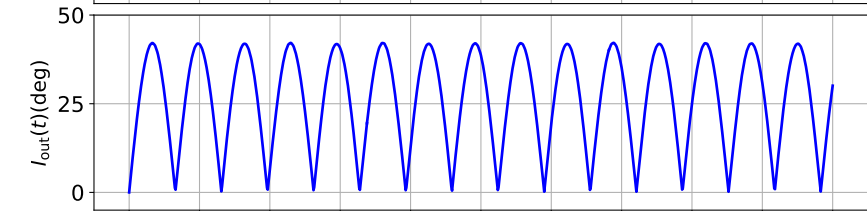
$i_{\text{mut}}(t)$



$I_{\text{in}}(t)$

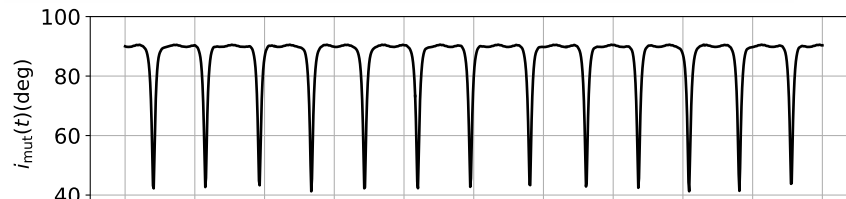


$I_{\text{out}}(t)$

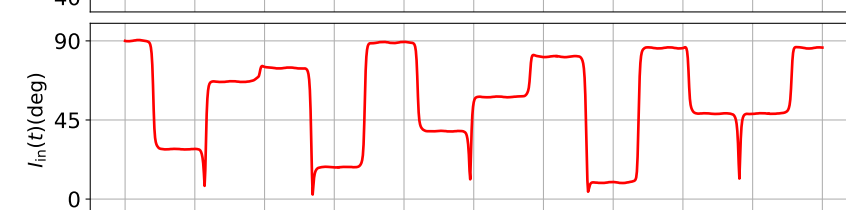


$t/P_{\text{out}}^{(0)}$

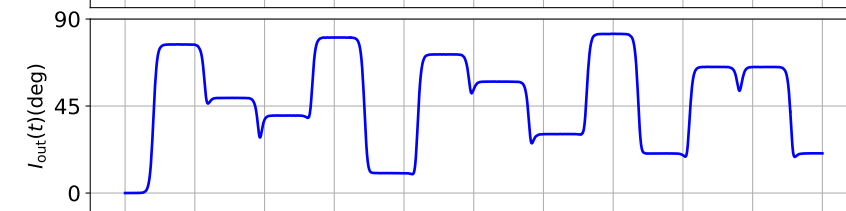
$i_{\text{mut}}(t)$



$I_{\text{in}}(t)$

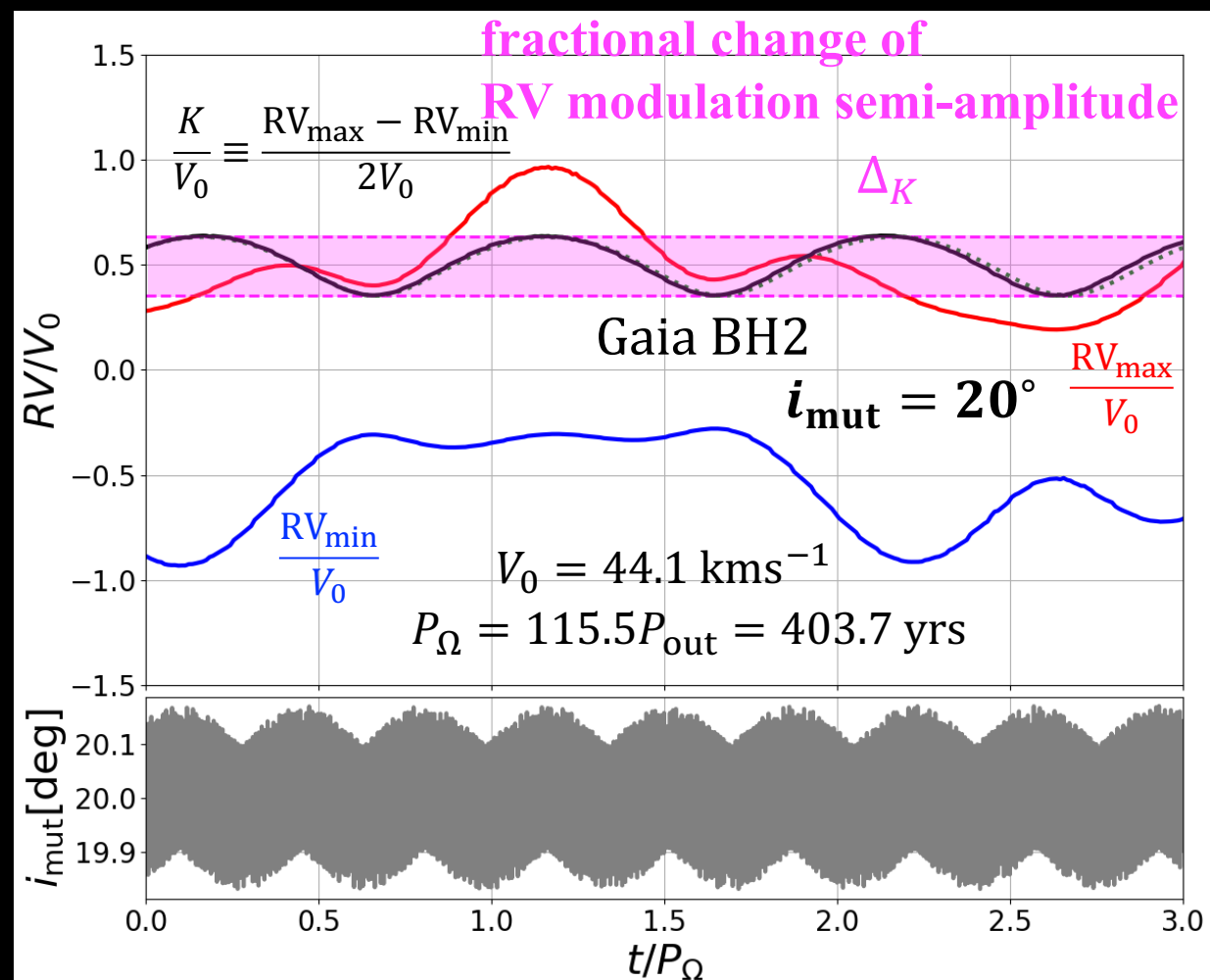
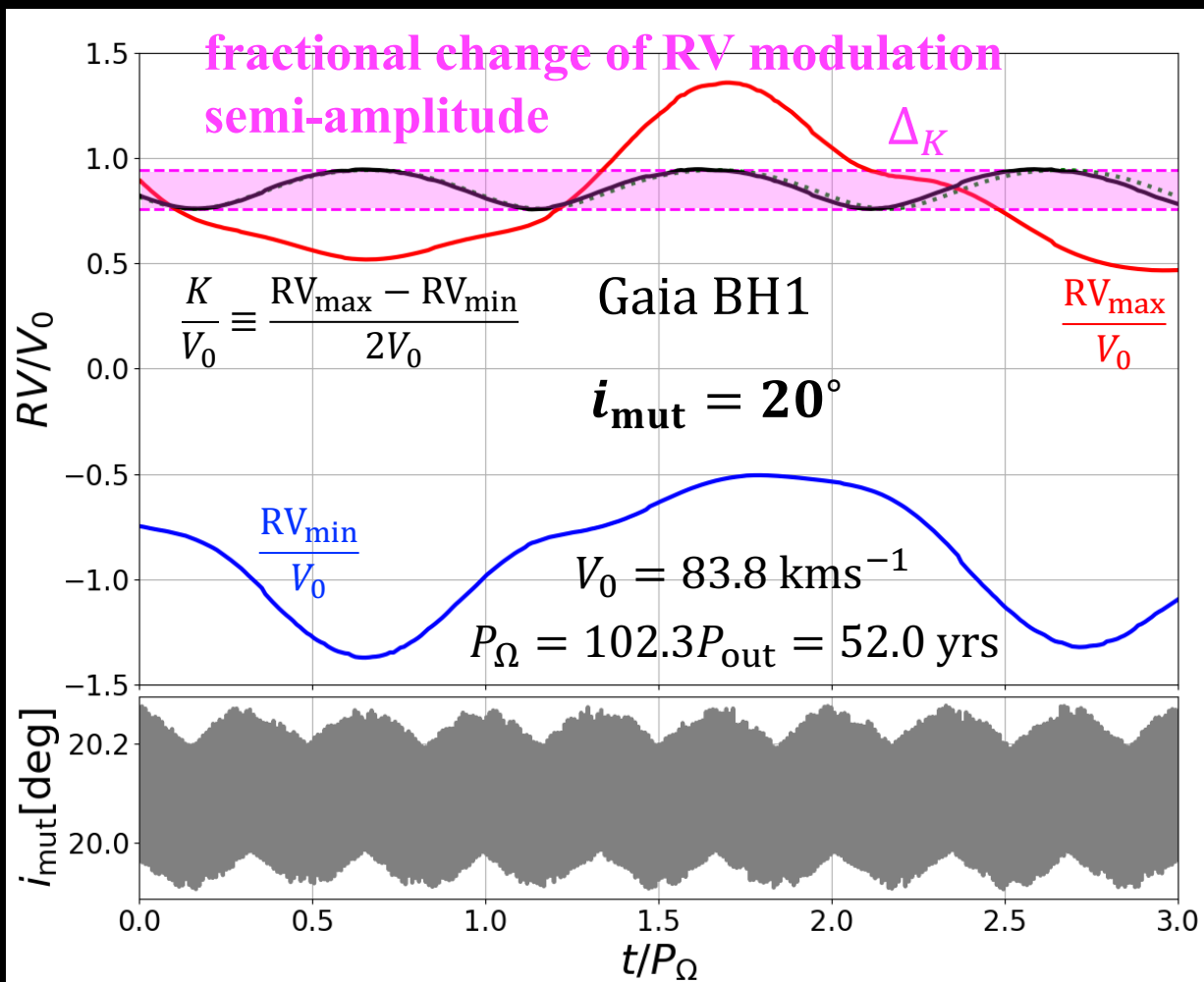


$I_{\text{out}}(t)$

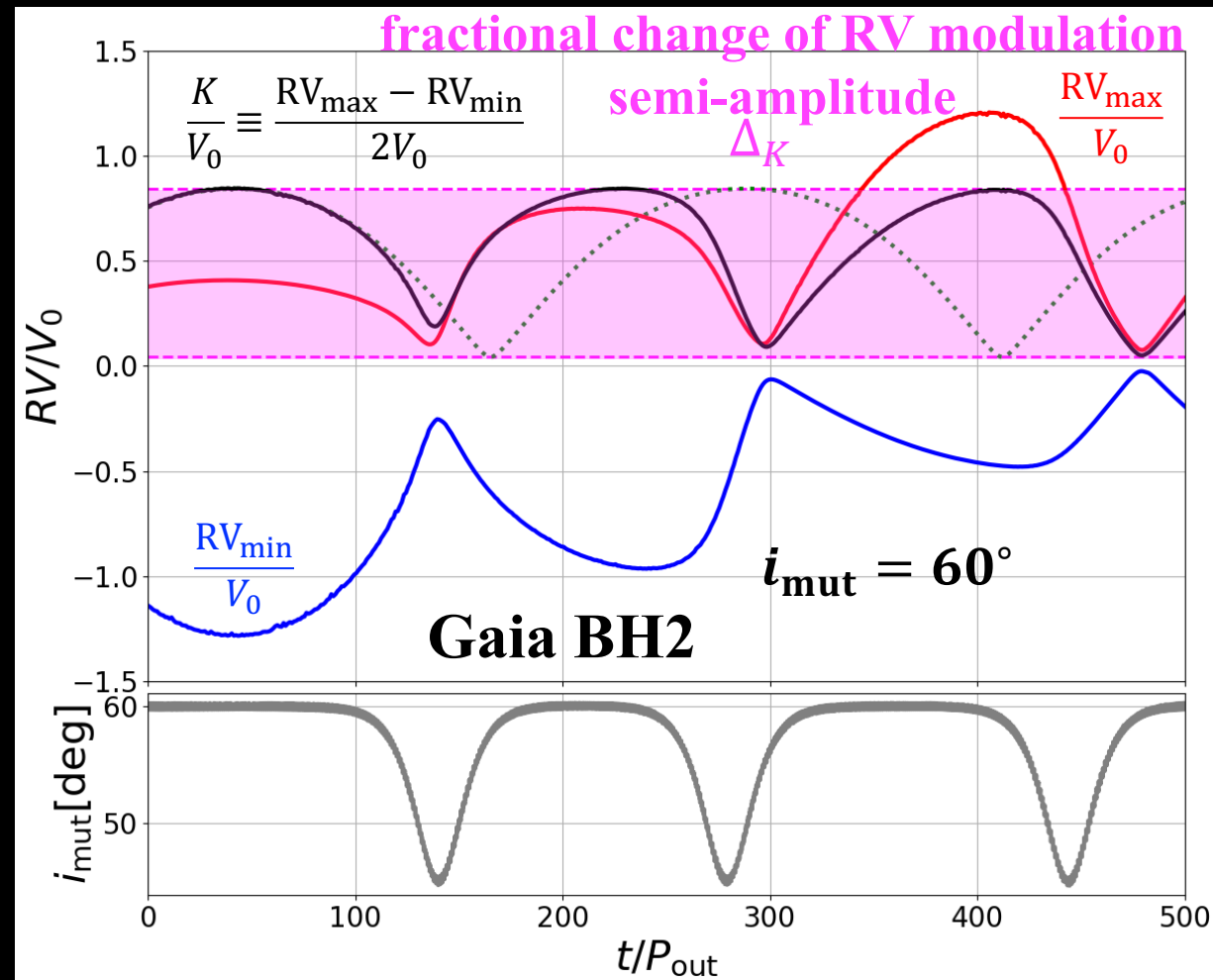
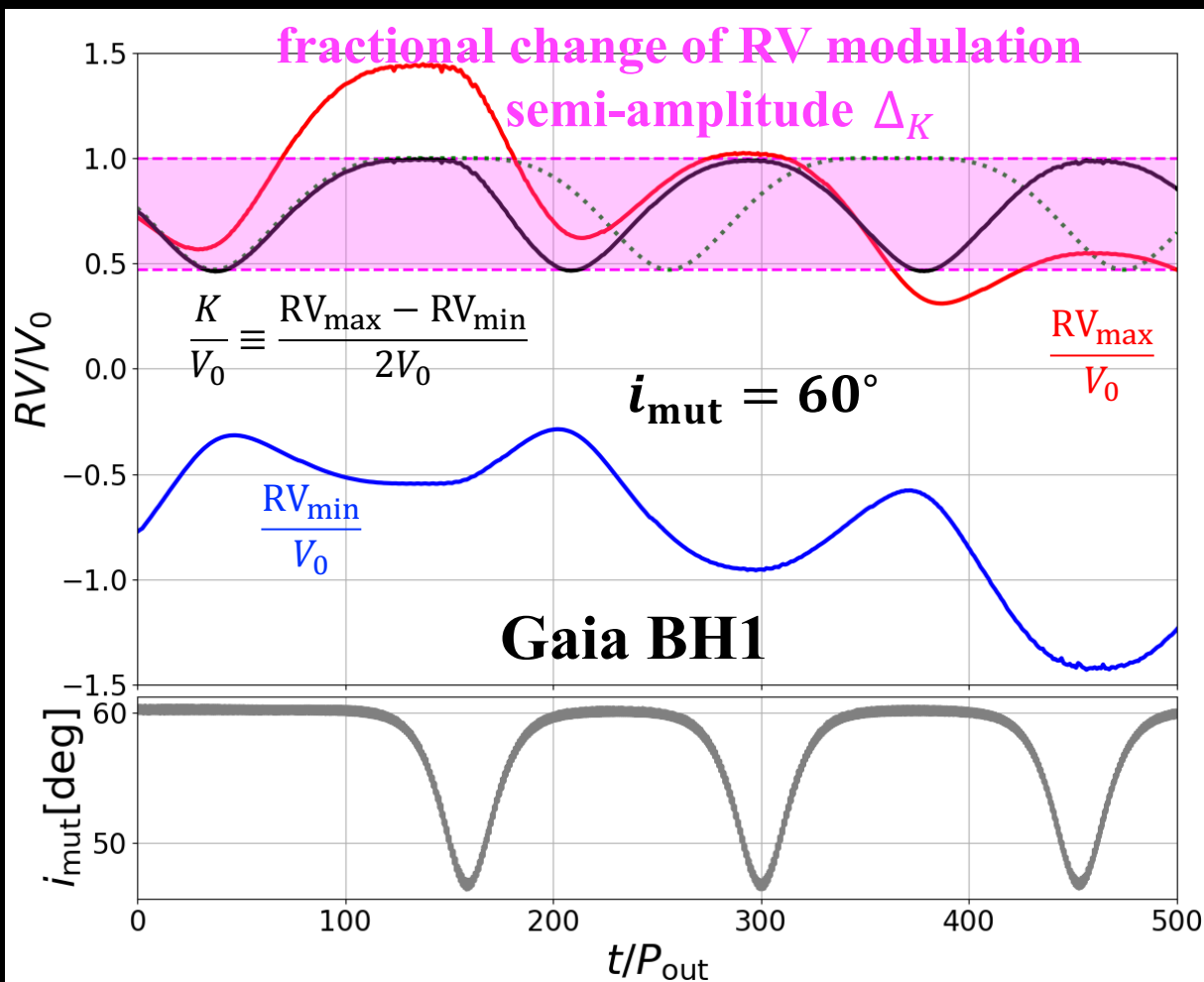


$t/P_{\text{out}}^{(0)}$

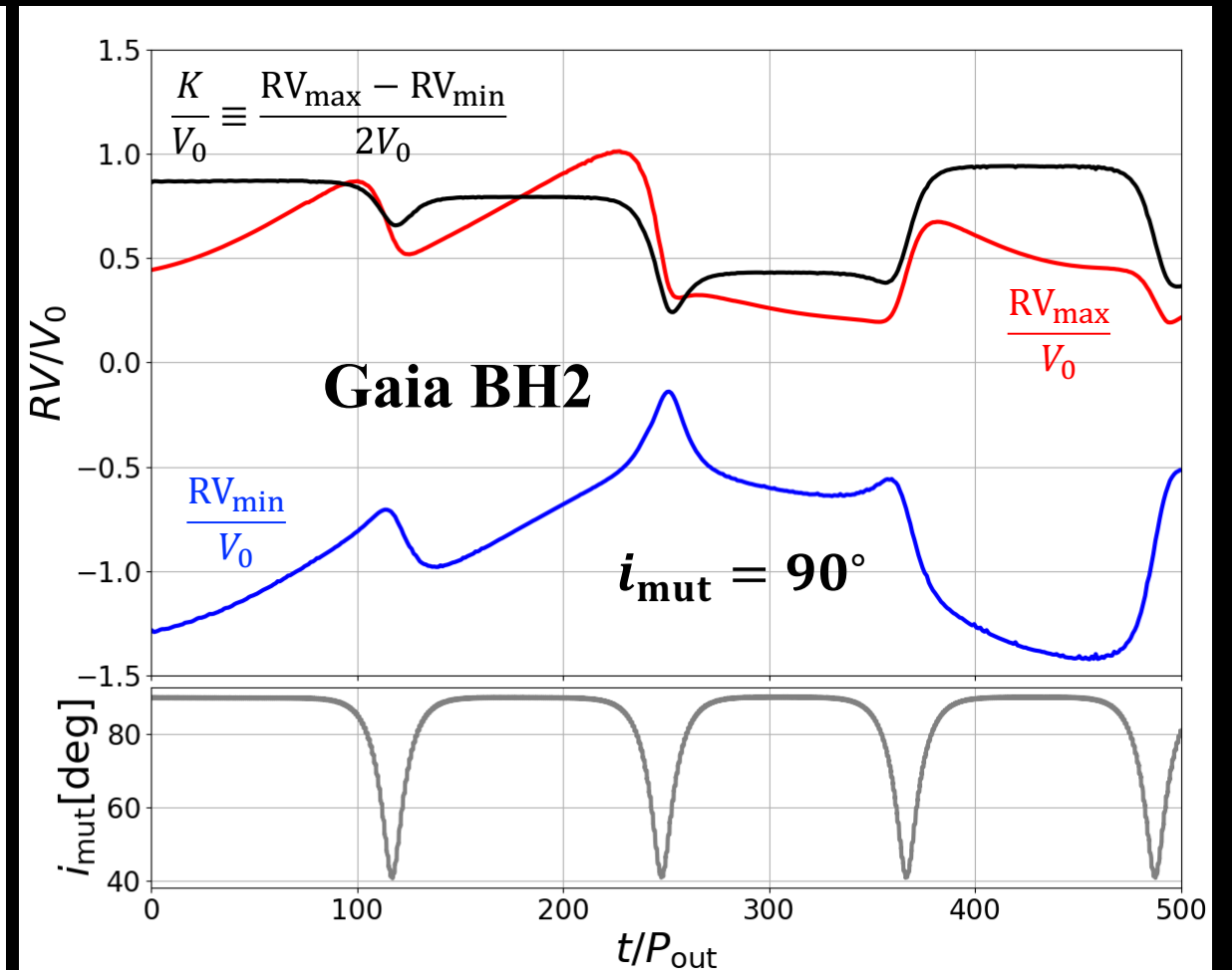
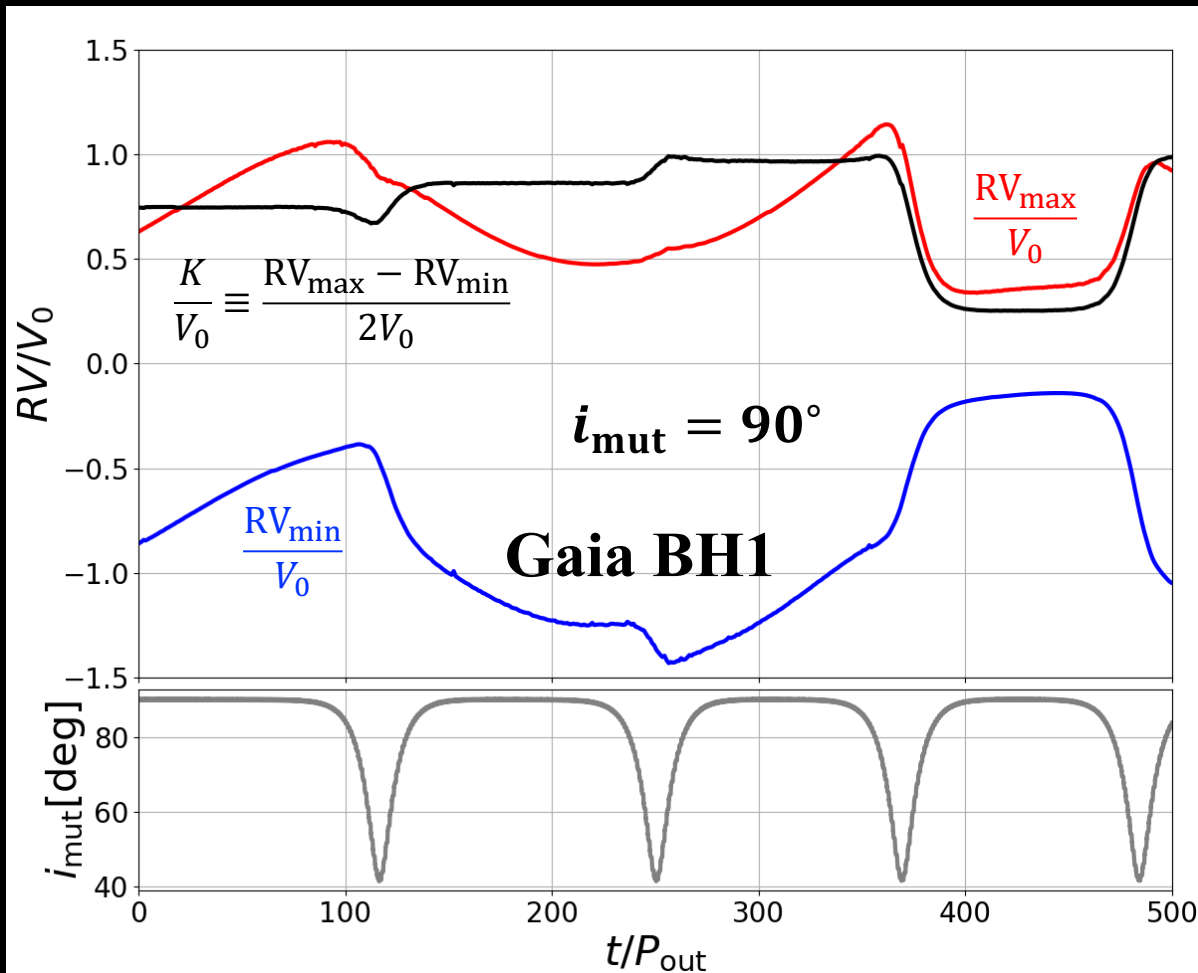
Long-term RV modulations due to nodal precession ($i_{mut} = 20^\circ$)



Long-term RV modulations due to moderate ZKL oscillations ($i_{mut}=60^\circ$)



Long-term RV modulations due to strong ZKL oscillations ($i_{mut}=90^\circ$)



Hayashi, YS + Trani (2023)

Conclusion: RV signatures of inner binary black holes in triple systems may be detectable

- Radial velocity (RD) monitoring of star-black hole binary candidates may reveal inner binary black holes if exist at all
 - short-term RD variations [Hayashi, Wang + YS: ApJ 890\(2020\)112](#)
 - periodic modulations of $O(0.1)$ percent of the Kepler orbital velocity amplitude with a half inner orbital period
 - long-term RD variations in inclined triples [Hayashi + YS: ApJ 897\(2020\)29](#)
 - the semi-amplitude of the Kepler orbital velocity modulated quasi-periodically by the nodal precession and/or the ZKL oscillations of the inner and outer orbits over $O(100)$ years
 - A proof-of-concept study for Gaia BH1 and BH2 systems
 - may be even detectable for Gaia BH1! [Hayashi, YS + Trani: arXiv:2307.01793](#)

False positive: *Tant pis? Non, Tant mieux!*

- *Suppose that Gaia BH1 exhibits a short-term RV modulation of $\sim 100\text{m/s}$ with period P_{short}*
 - **Signal (=false positive for people in this session)**
 - the first discovery of a stellar-mass binary blackhole (orbital period of $2P_{\text{short}}$) in a triple system
 - **False positive (=signal for people in this session)**
 - the first discovery of a planetary system (orbital period of P_{short}) orbiting a stellar-mass blackhole

see Morais & Correia (2008, 2012), Hayashi, Wang & YS (2020)