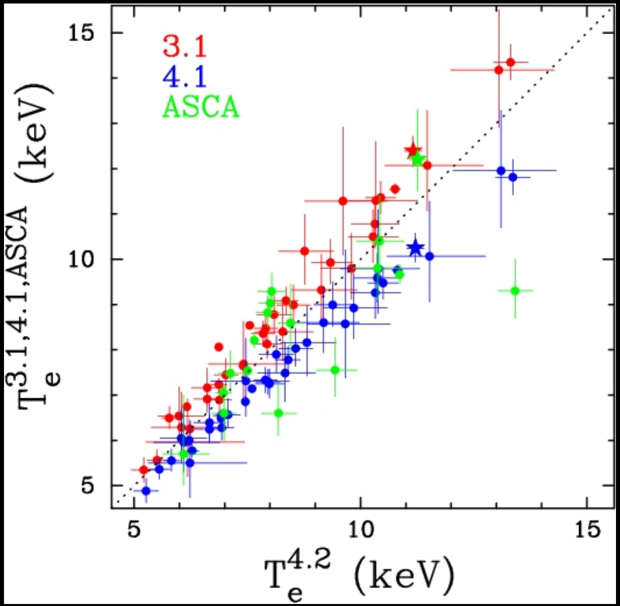
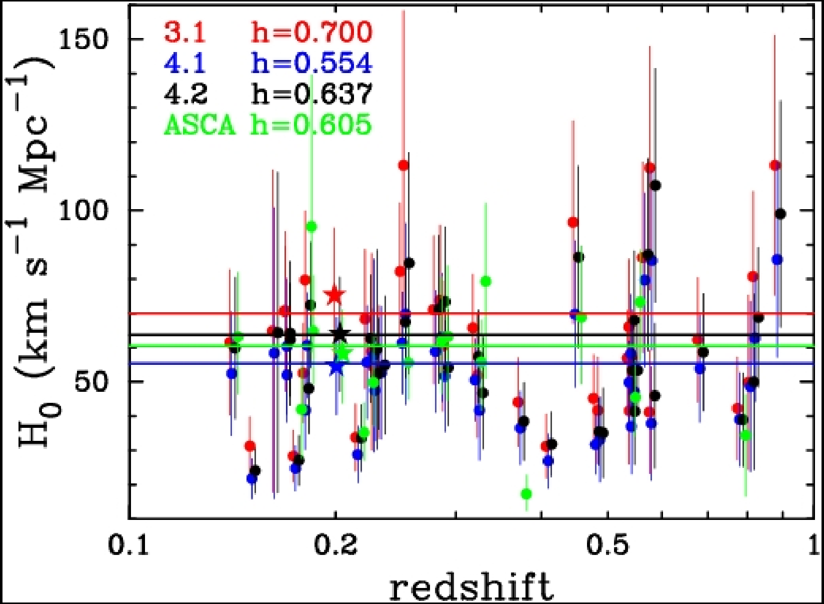
Impact of Chandra calibration uncertainties on cluster temperatures: application to H_0 from the Sunyaev-Zel'dovich effect





Yasushi Suto *Department of Physics, The University of Tokyo, and Global Scholar at Department of Astrophysical Sciences, Princeton University*

Caltech theoretical astrophysics group seminar, 14:00- June 25, 2010

Collaborators and references

- **E.Reese, H.Kawahara, T.Kitayama, N.Ota, Shin Sasaki, & Y.Suto; arXiv:1006.4486**
- **Kawahara et al. (2007)**
  - *Radial Profile and Lognormal Fluctuations of the Intracluster Medium as the Origin of Systematic Bias in Spectroscopic Temperature*
    ApJ 659(2007)257
- **Kawahara et al. (2008a)**
  - *Systematic Errors in the Hubble Constant Measurement from the Sunyaev-Zel'dovich effect* ApJ 674(2008)11
- **Kawahara et al. (2008b)**
  - *Extracting Galaxy Cluster Gas Inhomogeneity from X-ray Surface Brightness: A Statistical Approach and Application to Abell 3667*
    ApJ 687(2008)936

Temperature of galaxy clusters is ill-defined; mass-weighted, emission-weighted, and spectroscopic temperatures

$$\langle T \rangle_w = \frac{\int T W dV}{\int W dV}$$

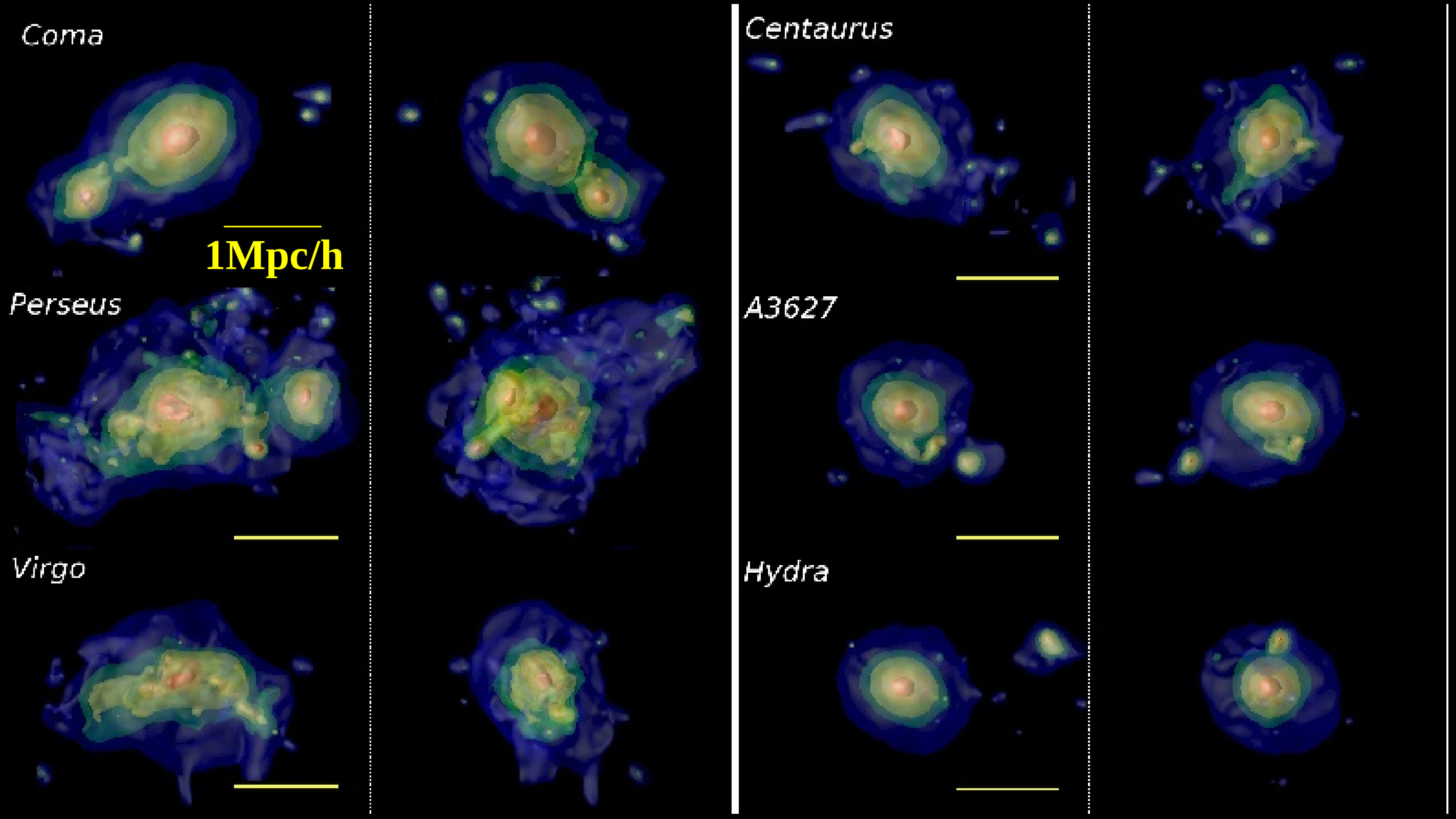
Clusters have multi-phase temperature structure and substructures/fluctuations

	name	W	
T_m	mass–weighted	n	
T_{ew}	emission–weighted	$n^2\Lambda(T)$	
T_{spec}	spectroscopic	spectral fit	
T_{sl}	spectroscopic–like	$n^2T^{-0.75}$	Mazzotta et al. (2004)

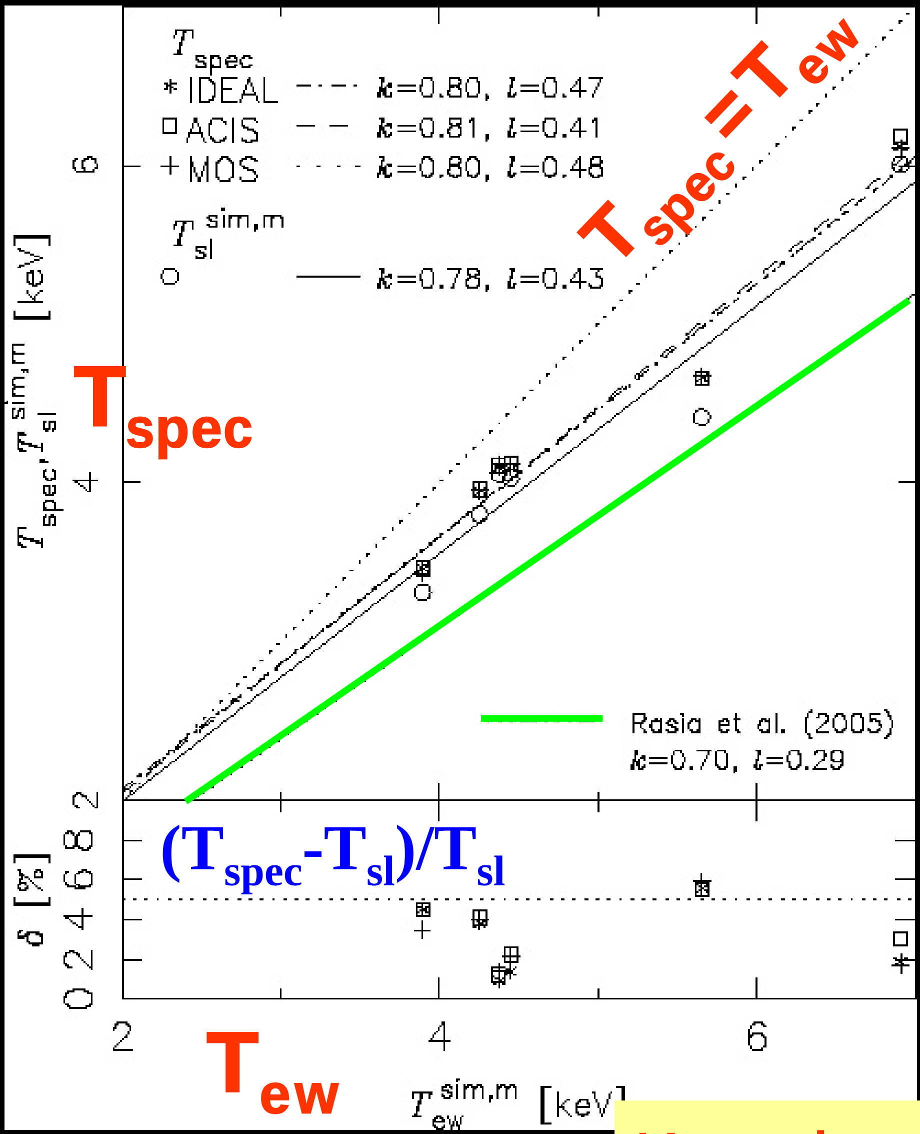
Simulated clusters in the local universe

- SPH simulations by Dolag et al. (2005)
- Local universe distribution in a sphere of r=110Mpc
- Initial condition: smoothing the observed galaxy density field of IRAS 1.2 Jy survey (over $5h^{-1}$Mpc), linearly evolving back to z=50
- with cooling, star formation, SN feedback, and metalicity evolution in ΛCDM

Projected views of *simulated clusters*



T_{spec} is systematically smaller than T_{ew}



- Spectroscopically more weight (more lines) toward cooler regions
  - Mazzotta et al. (2004) & Rasia et al. (2005) found $T_{spec} \sim 0.7\ T_{ew}$ from simulations
  - We confirm their results using simulated clusters of Dolag et al. (2005) $T_{spec} \sim 0.8\ T_{ew}$
    (see also Mathiesen & Evrard 2001)

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An analytic model for T_{spec}/T_{ew}

- Spherical polytropic β -model as global mean radial profiles
- Log-normal density and temperature fluctuations
  - Density and temperature correlations ignored
  - Radius independent dispersion adopted
- $\Rightarrow$ Analytic expressions for the temperature underestimate, T_{sl}/T_{ew}
  - Explain numerical simulations well

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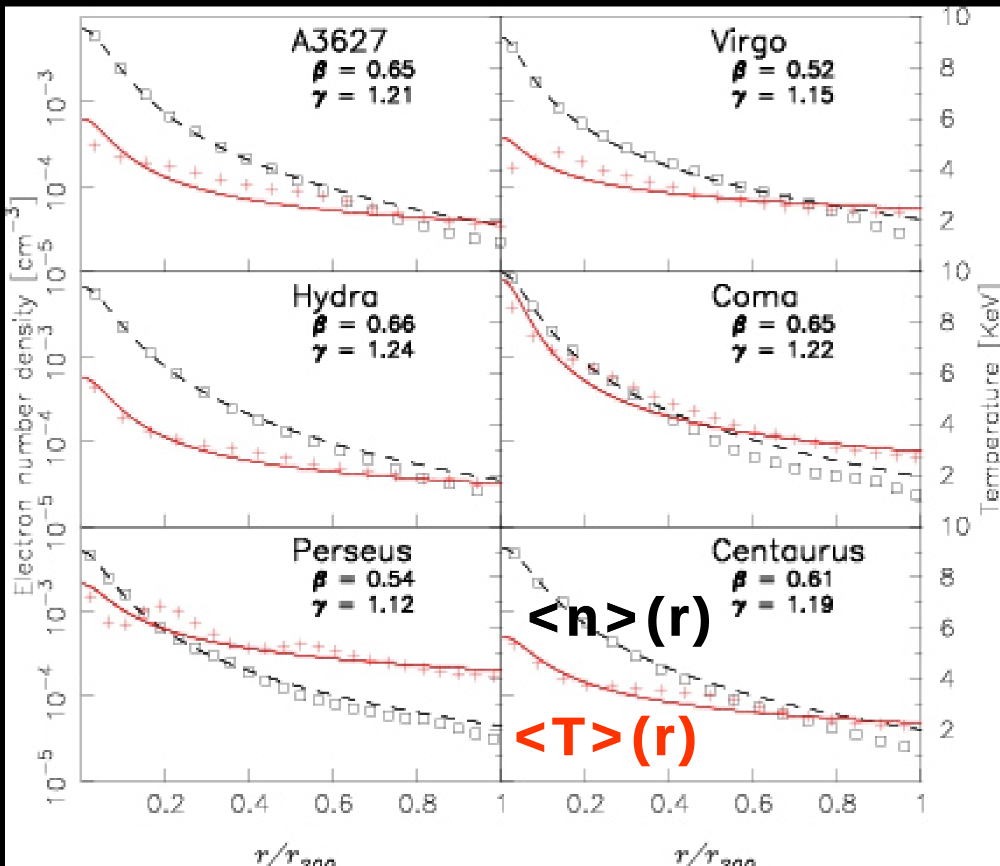
Origin of $T_{spec} < T_{ew}$ (1) mean radial profile



- **Density and temperature radial profiles of simulated clusters**
- Polytropic β model

$$< n > (r) = n_0 \left[\frac{1}{1 + (r / r_c)^2} \right]^{3\beta/2}$$

$$< T > (r) = T_0 [< n > (r) / n_0]^{\gamma - 1}$$

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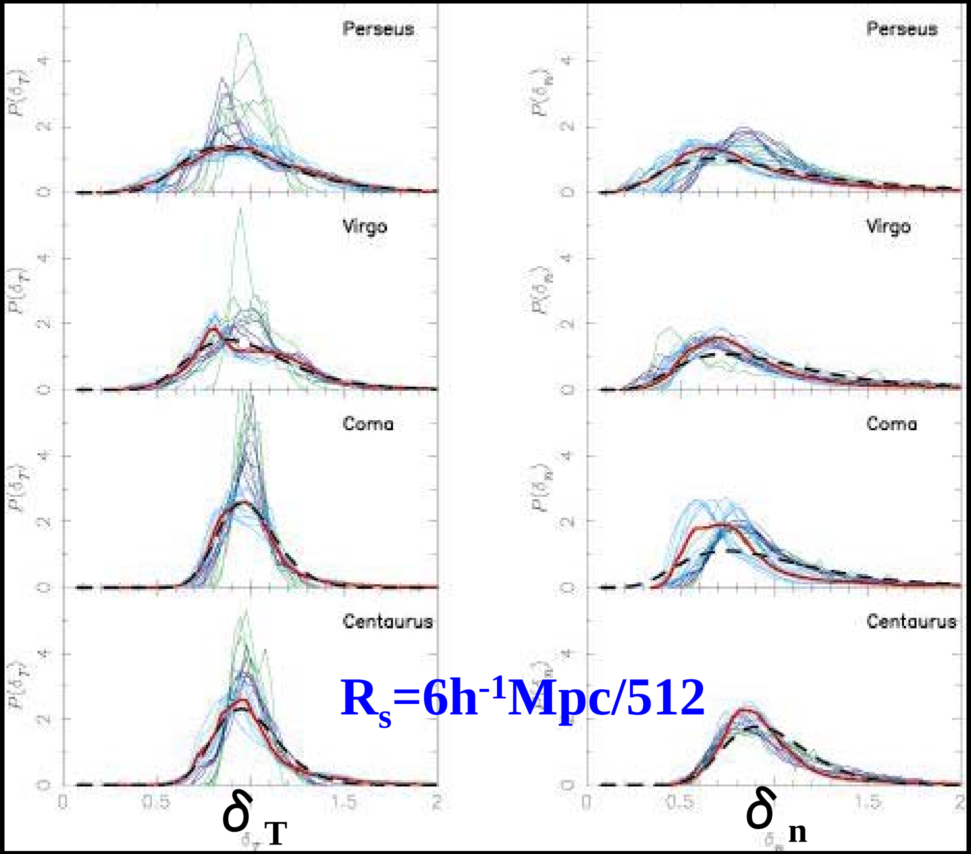
Origin of $T_{spec}<T_{ew}$ (2) Local inhomogeneity



- Local inhomogeneities of density and temperature of simulated clusters
  - $\delta_n = n(r,\theta,\phi)/\langle n\rangle(r)$
  - $\delta_T = T(r,\theta,\phi)/\langle T\rangle(r)$
- Log-normal PDF provides reasonable approximations

$$P_{LN}(\delta)d\delta = \frac{1}{\sqrt{2\pi\sigma}}\exp\left[-\frac{(\log\delta+\sigma^2/2)^2}{2\sigma^2}\right]\frac{d\delta}{\delta}$$

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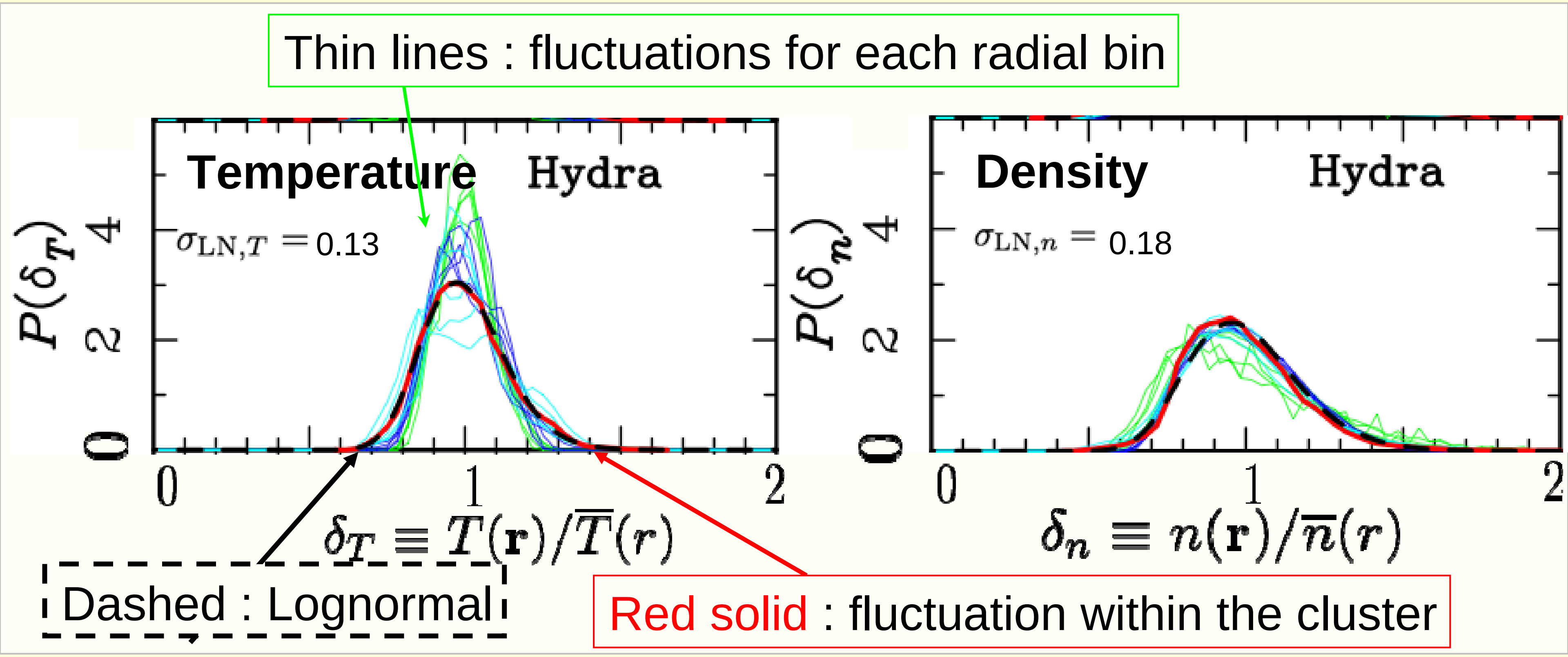
Lognormal Model from hydro simulations

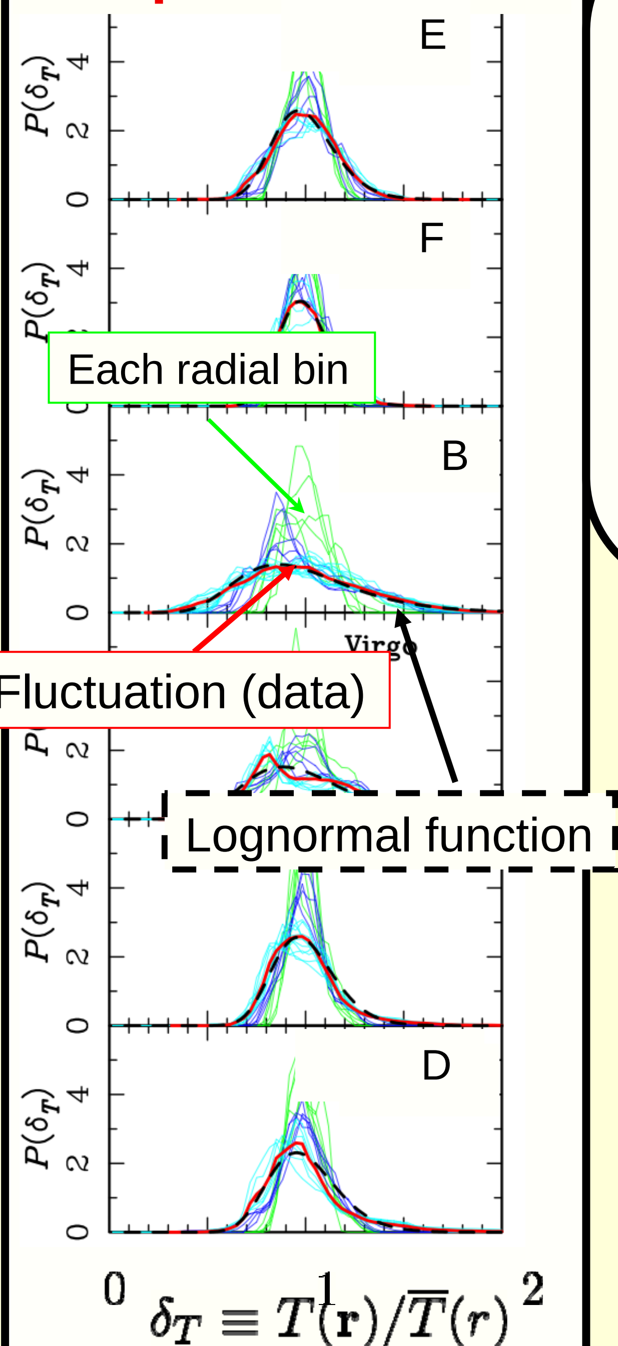


- Both the density and temperature fluctuations can be approximated by lognormal distribution:

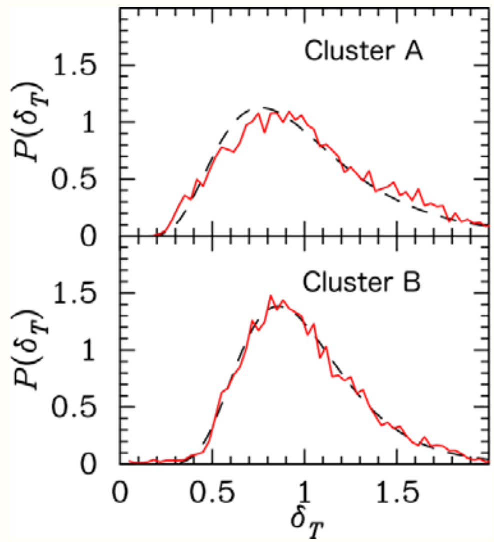
$$P(\delta_x;\sigma_{\mathrm{LN},x})d\delta_x = \frac{1}{\sqrt{2\pi}\sigma_{\mathrm{LN},x}}\exp\left[\frac{-(\log\delta_x + \sigma_{\mathrm{LN},x}^2/2)^2}{2\sigma_{\mathrm{LN},x}^2}\right]\frac{d\delta_x}{\delta_x}$$

$$\delta_x \equiv \frac{x(\mathbf{r})}{\bar{x}(r)} \quad (x = n \text{ or } T)$$

Temperature : SPH

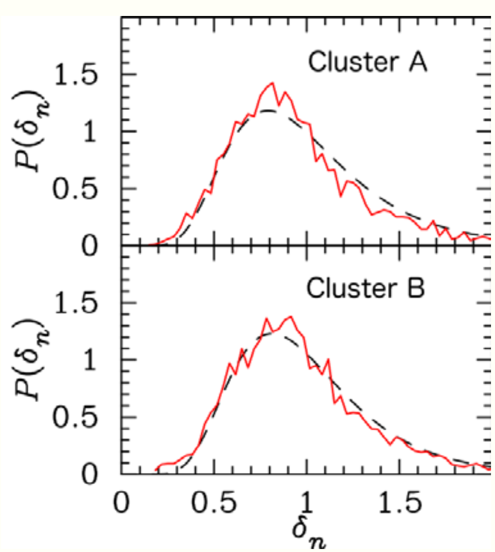


Temperature : Mesh

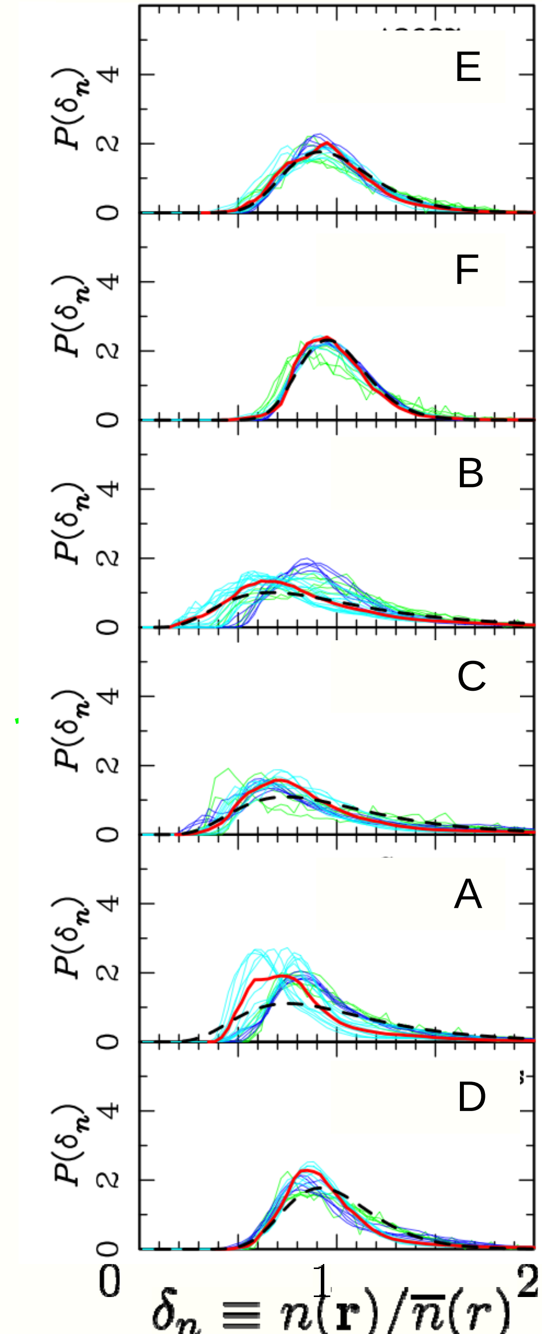


Other 6 + 2 clusters

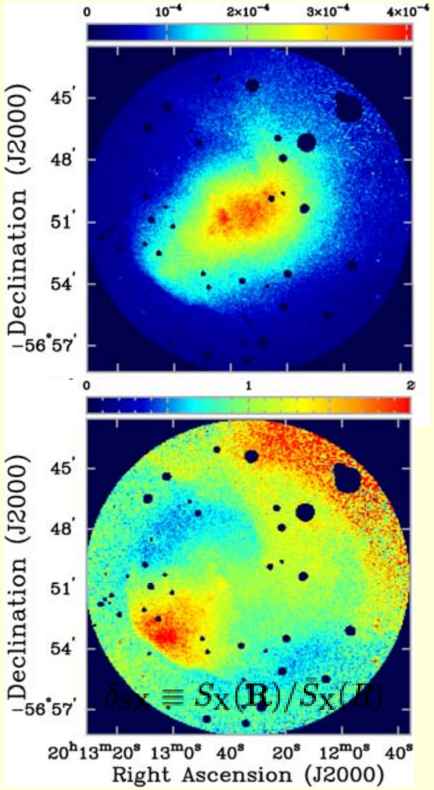
Density : Mesh

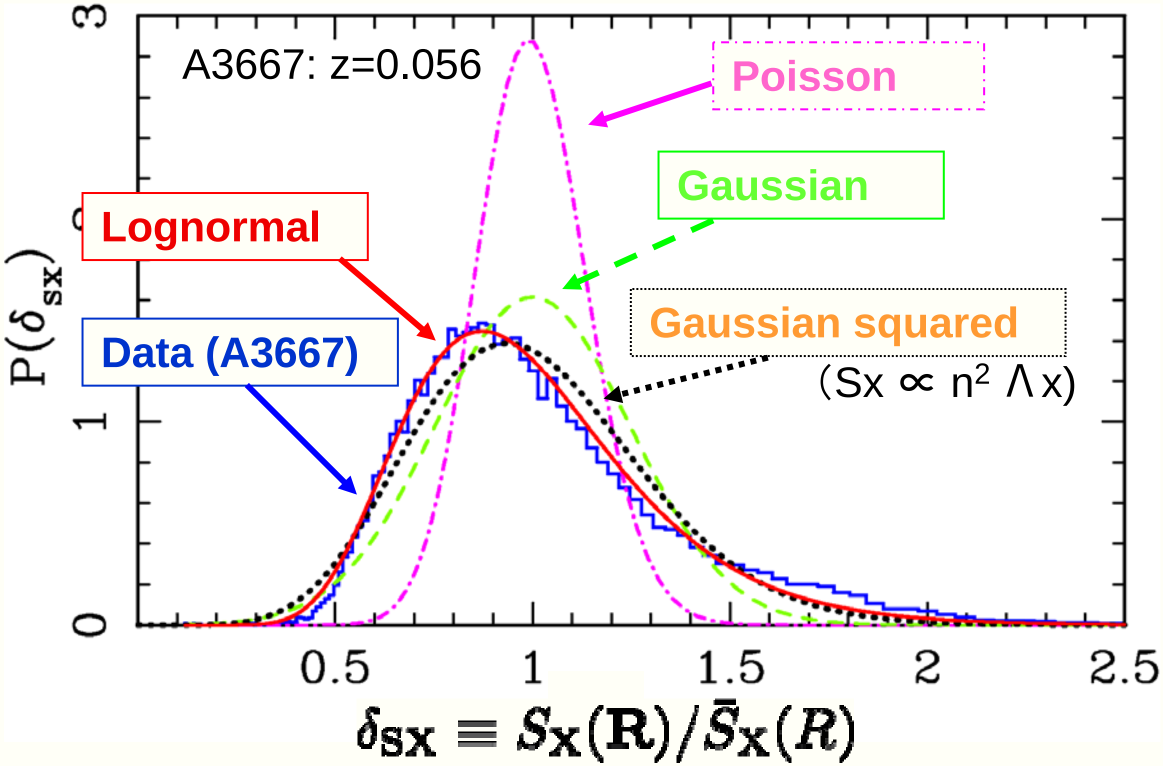


Density : SPH



Application to a real cluster: A3667





Good agreement with the Lognormal distribution

Estimated value of the density fluctuation: $\sigma_{\rm LN,n} = \left[0.75 + \frac{50}{(\alpha_{\rm Sx} - 0.2)^4}\right] \sigma_{\rm LN,Sx}$ ∽0.4

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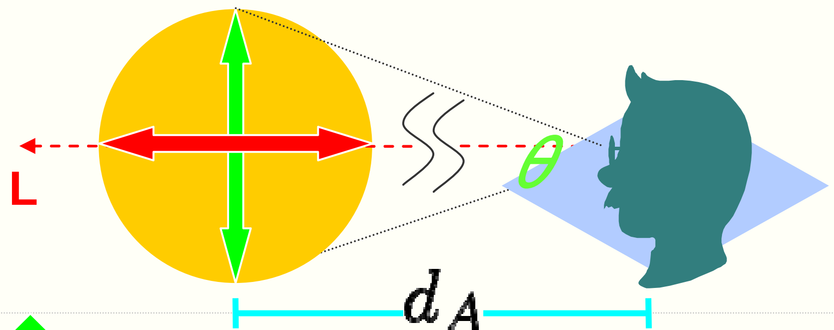
The Hubble constant measurement using galaxy clusters

- SZ: primary distance indicator
- Assumption : the spherical isothermal β model



: Angle θ **from X-ray map**

$$d_A = L/\theta$$

$$H_0 = \frac{cz}{d_A(z)}\left[1 + \frac{2\lambda_0 - \Omega_0 - 6}{4} z + \mathcal{O}(z^2)\right]$$

: the **SZ effect**

$$\frac{-\Delta I}{I} \propto y \approx n\,T\,L$$

+ X-ray brightness

$$S_x \propto n^2 \Lambda_x(T)\,L$$

+ spectroscopic T

$T = T_{\rm spec}$ →**length L**

Isothermal β -model fit by force

- Isothermal β –model fit to polytropic density and temperature profiles

$$< n > (r) = n_0 \left[\frac{1}{1 + (r/r_c)^2} \right]^{3\beta/2}$$

$$< T > (r) = T_0 [< n > (r)/n_0]^{\gamma - 1}$$

- core radius estimated from X–ray + SZ

$$r_{c,iso\beta}(T_{spec}) = \frac{y(0)^2}{S_X(0)} \frac{m_e^2 c^4 \Lambda(T_{spec})}{4\pi(\sigma_T k T_{spec})^2 (1+z)^4} \frac{G(\beta_{fit})}{G(\beta_{fit}/2)^2}$$

$$\beta_{fit} = \beta \frac{\gamma + 3}{4}$$

Analytic modeling of H_0 measurement

- Spherical polytropic β-model as mean radial profiles
- Log-normal density and temperature fluctuations
- Still fit to the isothermal β-model by force, and the estimated H_0 is biased as

$$f_{H,polyLN|iso\beta} \equiv \frac{H_{0,est}}{H_{0,true}} = \chi_\sigma \; \chi_T(T_{ew}) \frac{\chi_T(T_{spec})}{\chi_T(T_{ew})}$$

inhomogeneity $\chi_\sigma = \exp(\sigma_{LN,n}^2 - \sigma_{LN,T}^2/8) \approx (1.1-1.3)$

non-isothermality

$$\chi_T(T_{ew}) = J(\beta,\gamma,r_c/r_{vir})^{1.5}\left[\frac{G(\beta(\gamma+3)/8)}{G(\beta\gamma/2)}\right]^2 \approx (0.8-1)$$

temperature bias $\dfrac{\chi_T(T_{spec})}{\chi_T(T_{ew})} \approx \left(\dfrac{T_{spec}}{T_{ew}}\right)^{1.5} \approx (0.8-0.9)$

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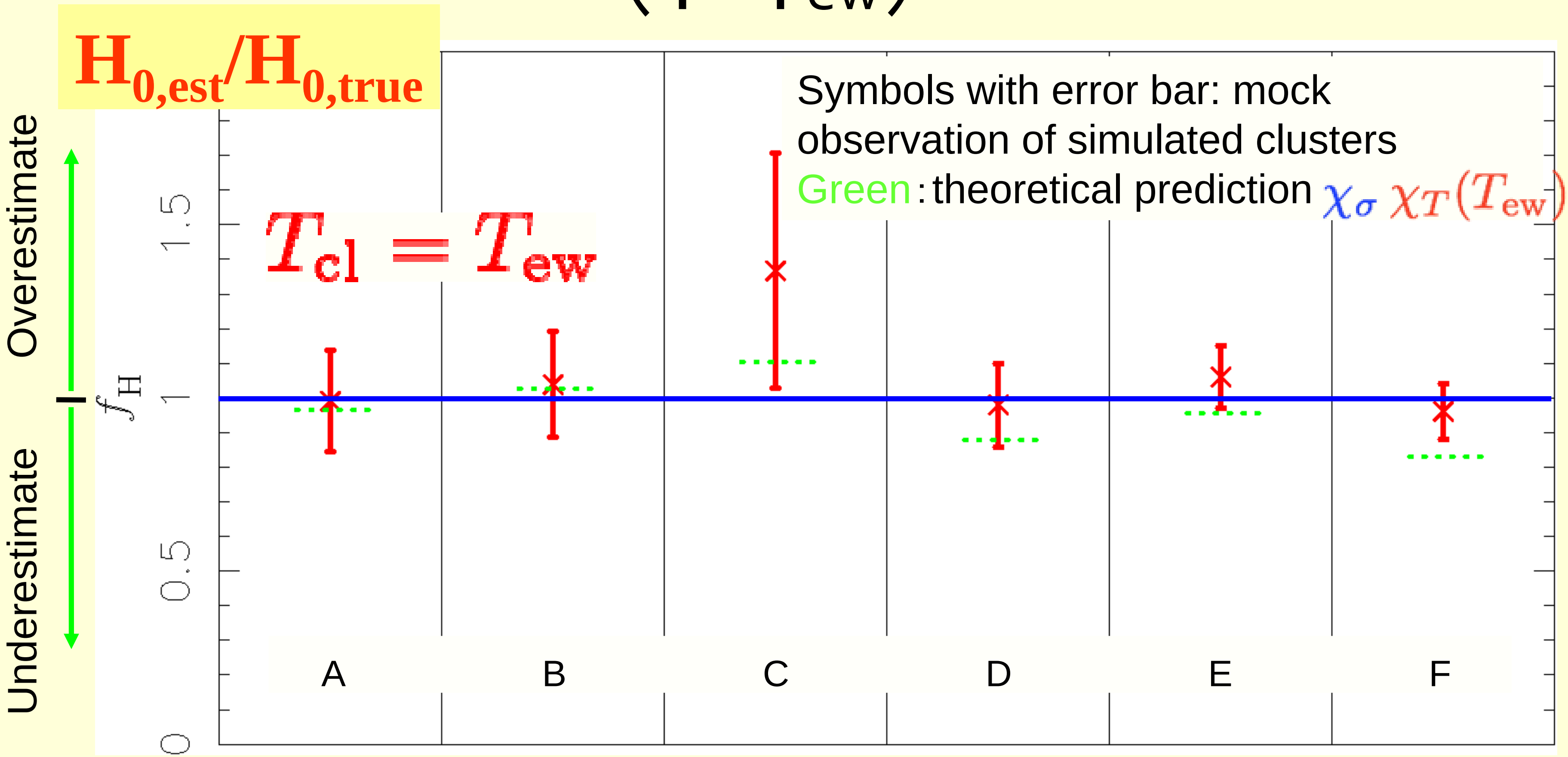
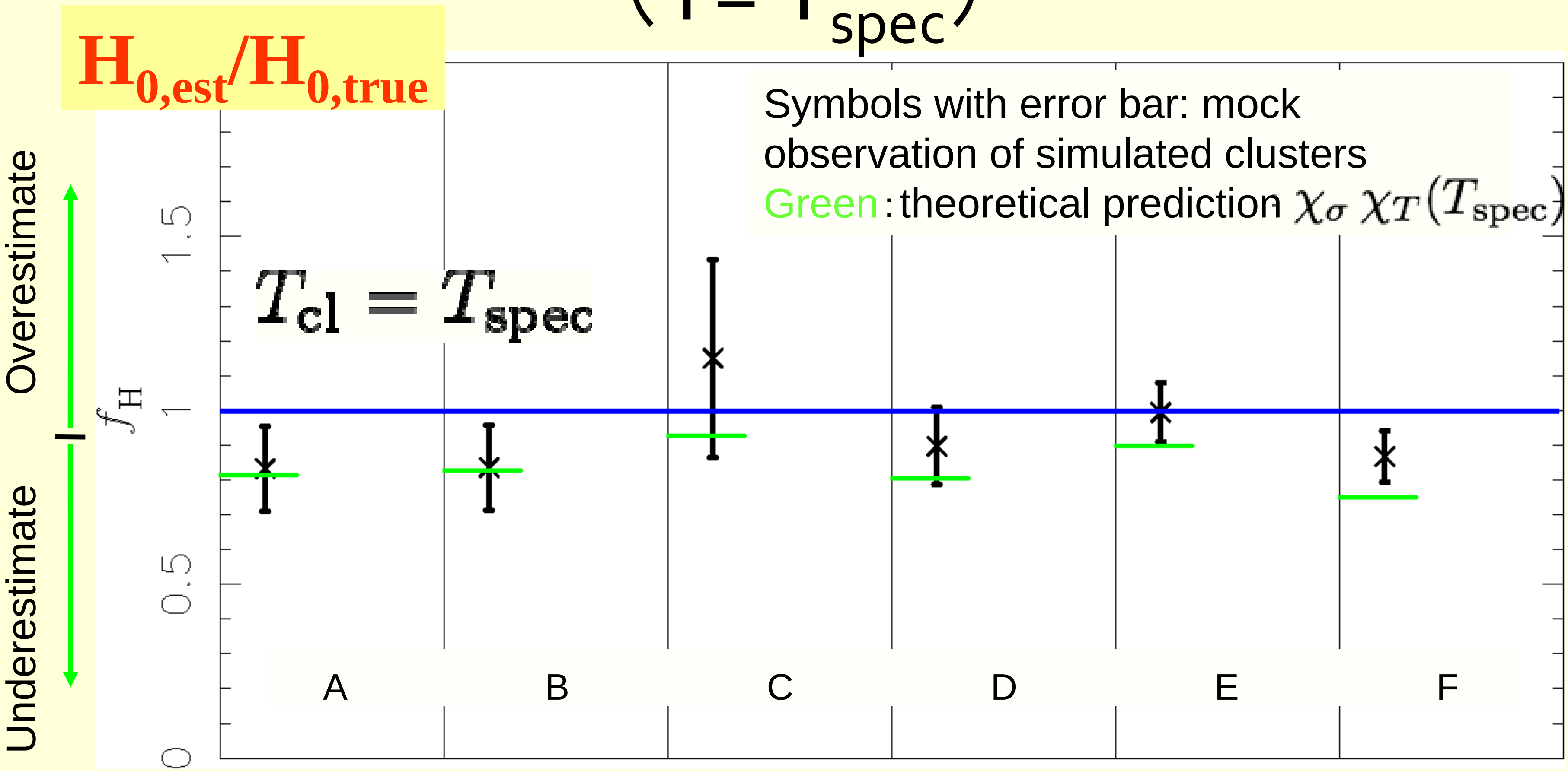
Analytic model vs Simulation
($T=T_{ew}$)



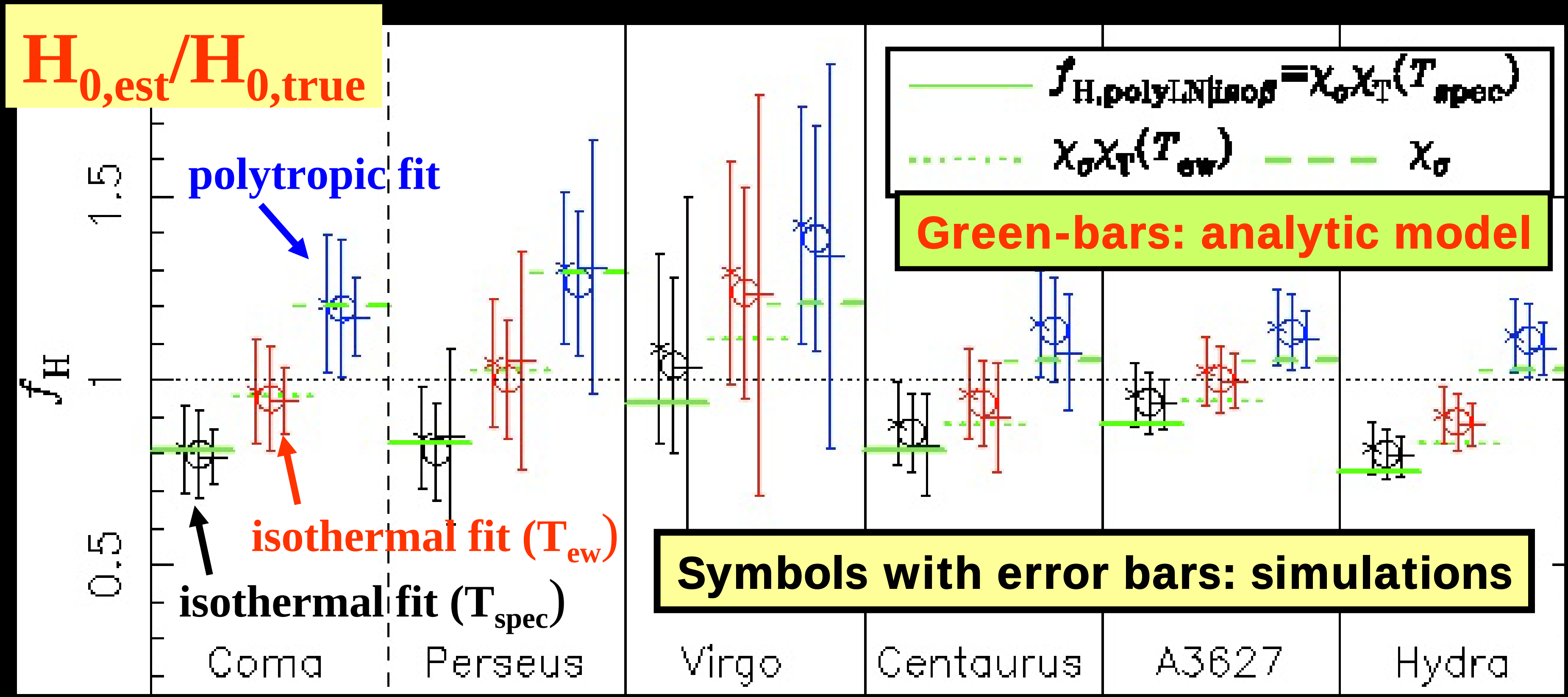
If $T= T_{ew}$, our results are consistent with the previous numerical studies (Inagaki et al. 1995, Yoshikawa et al. 1998)

Analytic model vs Simulation
(T= T_{spec})



- SZ+X clusters should underestimate the value of H_0 by 10-20%

Analytic model vs simulated clusters



- **Mean values are in good agreement with the analytic model**
- **Additional small bias expected due to non-sphericity of clusters even after averaging over l.o.s. angles**

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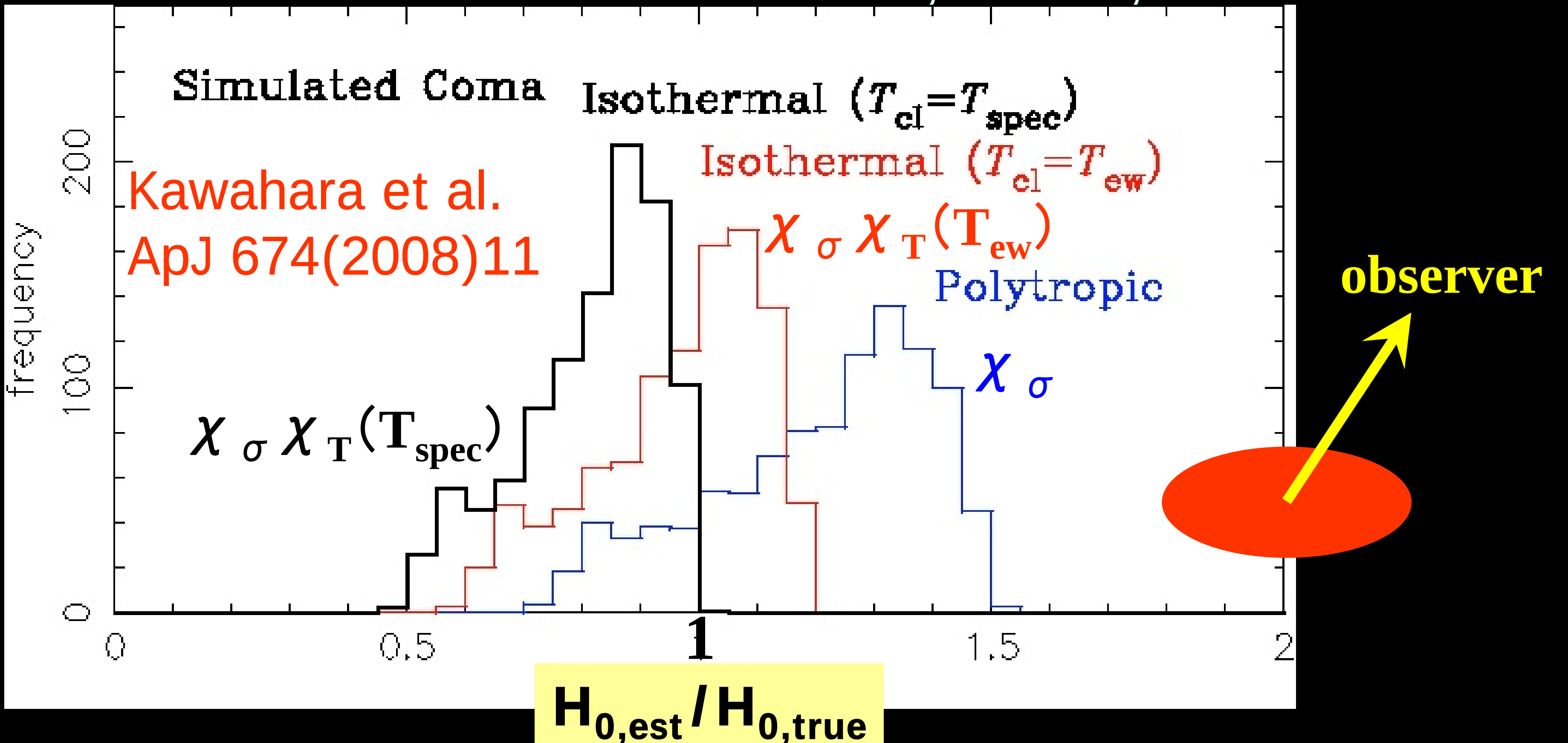
Distribution of $H_{0,est}/H_{0,true}$

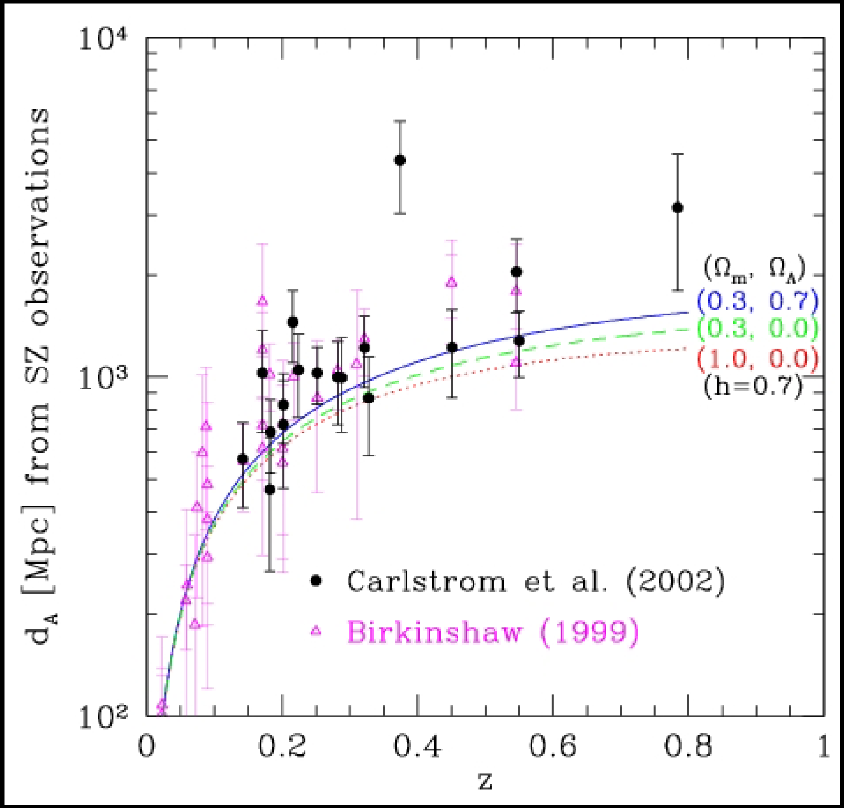


- Skewed distribution due to the prolateness
- Previous studies did not find the large bias because we set $T_{cl}=T_{ew}$ instead of T_{spec} (Inagaki, Suginohara & YS 1995, Yoshikawa, Itoh & YS 1998), consistent with our results of the isothermal fit with T_{ew}

Summary of theoretical predictions

- $H_{0,est}/H_{0,true}$= 0.8-0.9 from simulated clusters
- Analytic modeling of H_0 from the SZ effect
- $H_{0,est}/H_{0,true}$= 0.8-0.9 from simulated clusters is well explained by the combination of inhomogeneity and non-isothermality of ICM
- Is this consistent with the existing SZ observations ?

H_0 estimated from the SZ effect



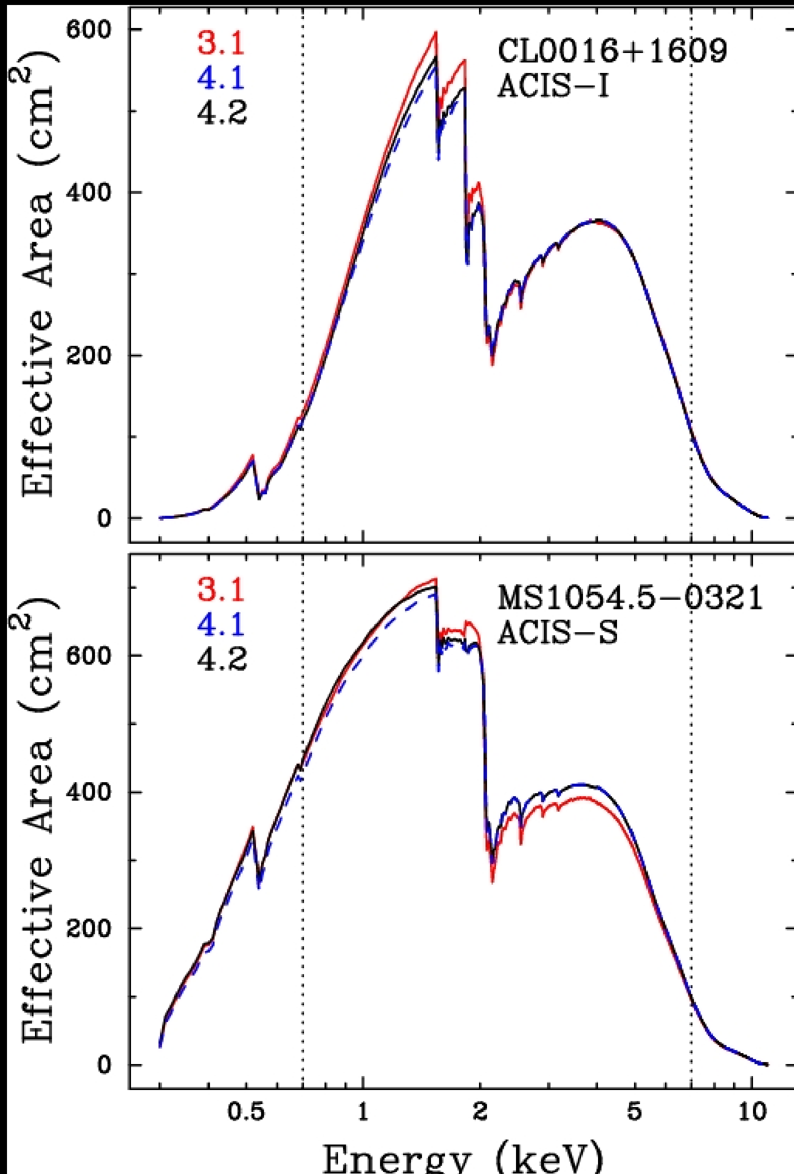
- ROSAT+SZ:
  - 60±3 km/s/Mpc (Reese et al. 02)
- Chandra+SZ
  - $76.9^{+3.9}_{-3.4}{}^{+10.0}_{-8.0}$ km/s/Mpc (Bonamente et al. 06)
- WMAP:
  - 73±3 km/s/Mpc (Spergel et al. 07)
- Which is believable (if any at all !) ?

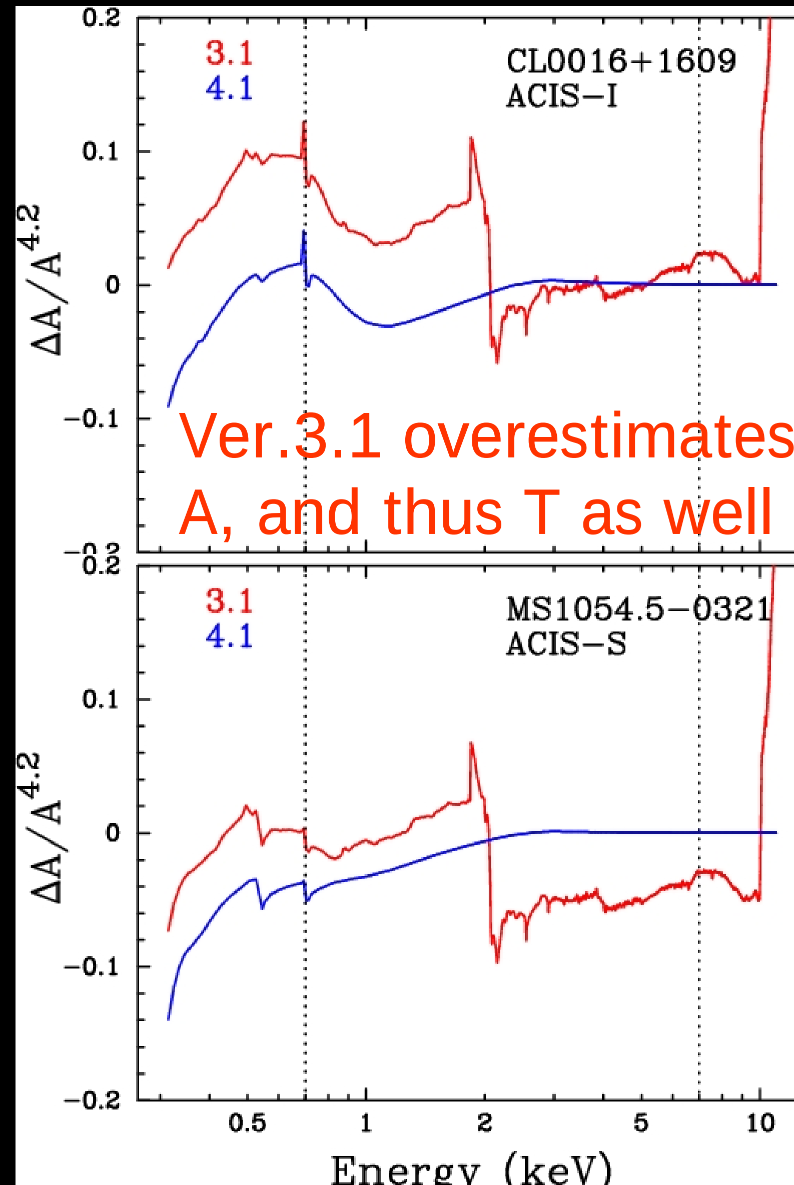
The same SZ but different X-ray data

- Reese et al. (2002)
  - 60 km/s/Mpc with ROSAT
- Bonamente et al. (2006)
  - 77 km/s/Mpc with Chandra
  - calibration data ver.3.1
- Chandra calibration data revision (2009)
  - Jan. 2009 ver.4.1: effective area of mirror
  - Dec. 2009 ver.4.2: ACIS (AXAF CCD Imaging Spectrometer) contamination model

Effective area

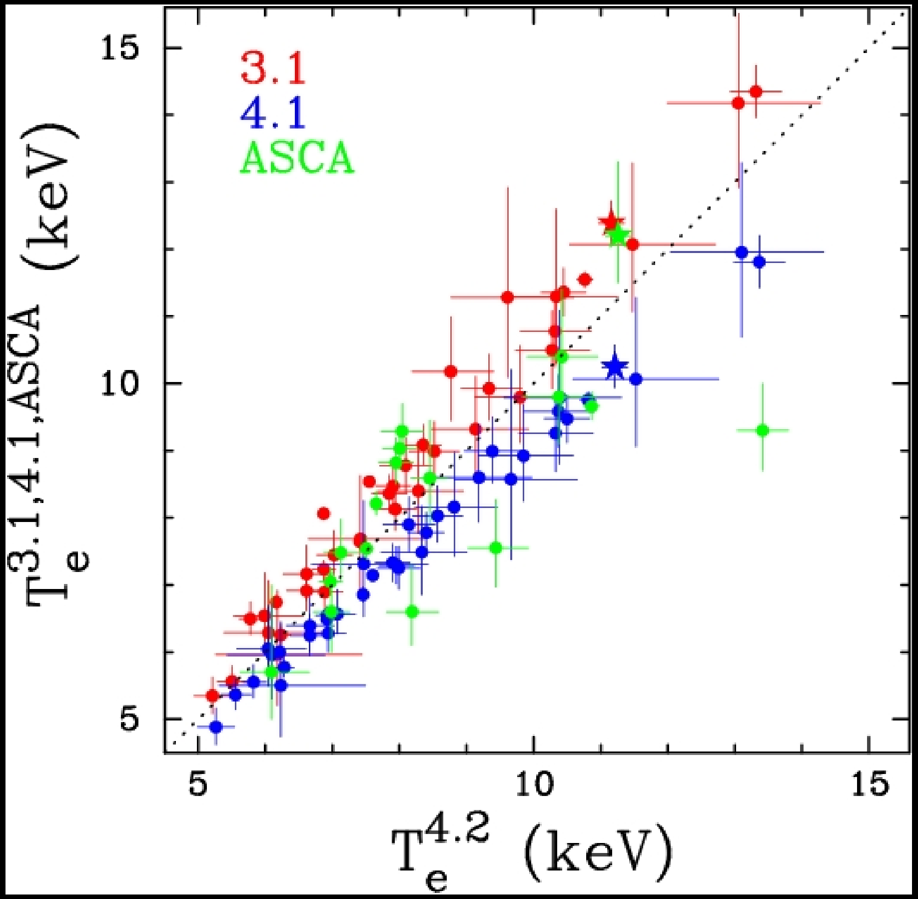
Majority of clusters are observed with ACIS-I (front illuminated chips)

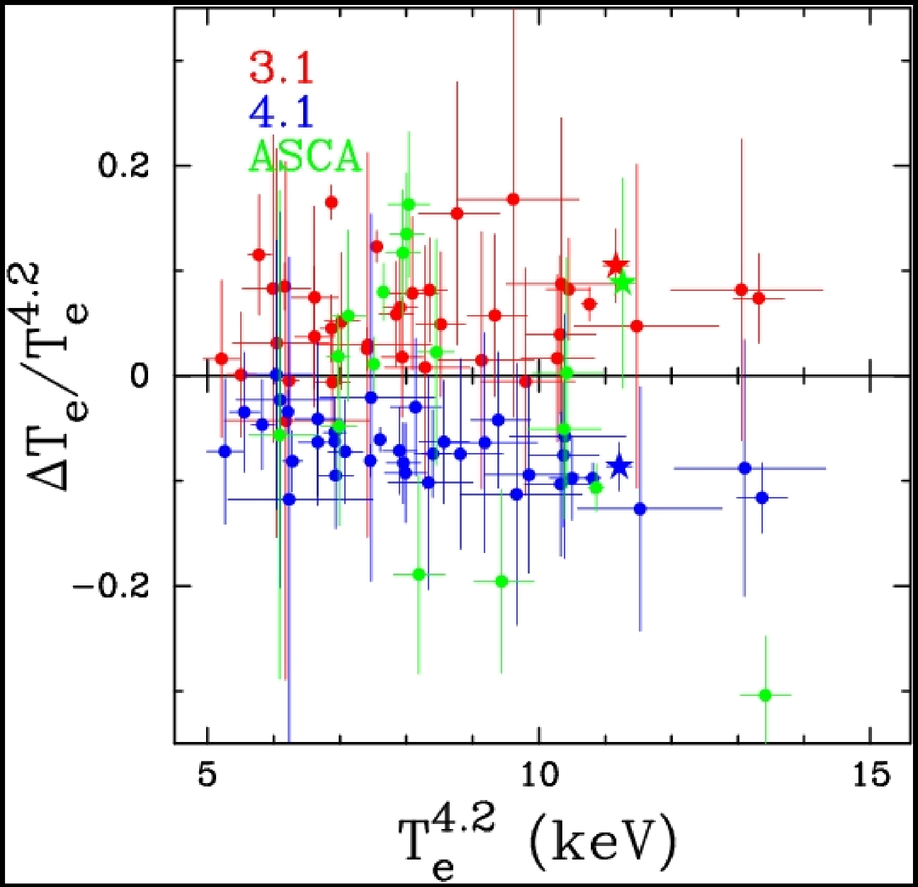




Ver.3.1 overestimates A, and thus T as well

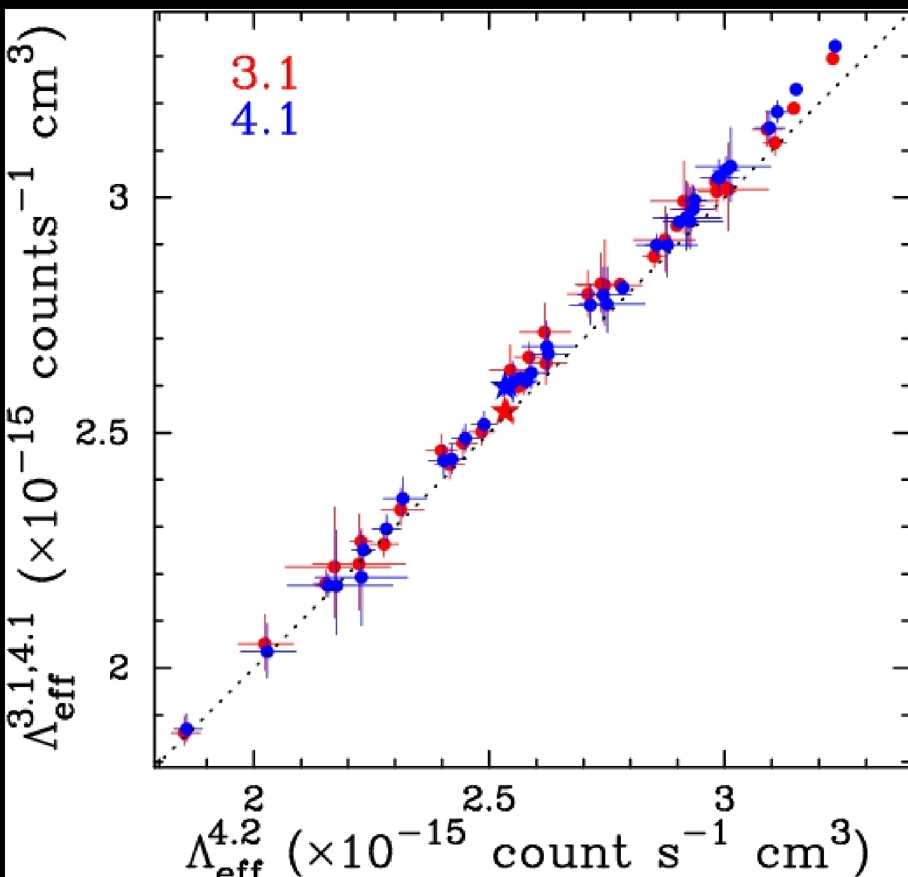
Spectroscopic temperatures

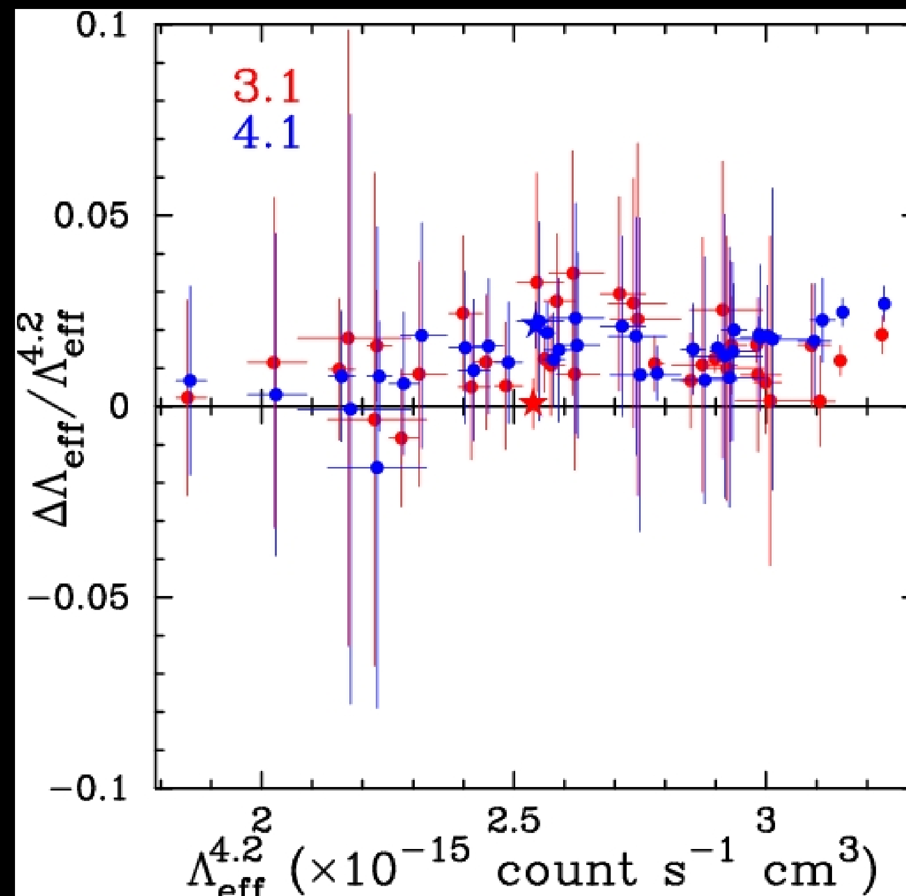




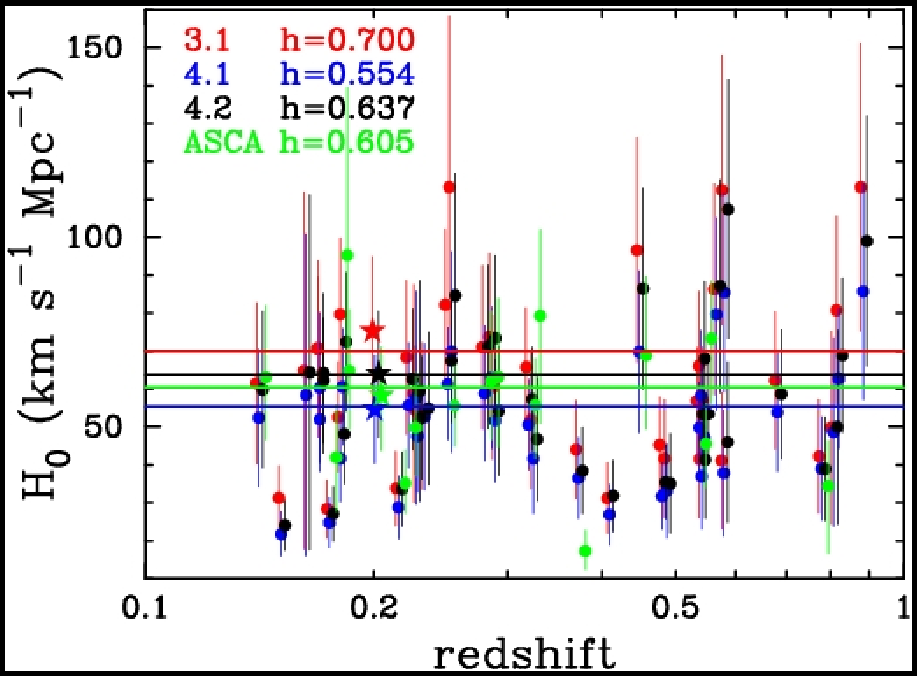
- Relative to the latest calibration data (ver.4.2)
  - Ver. 3.1 overestimates T by 6%
  - Ver. 4.1 underestimates T by 7%

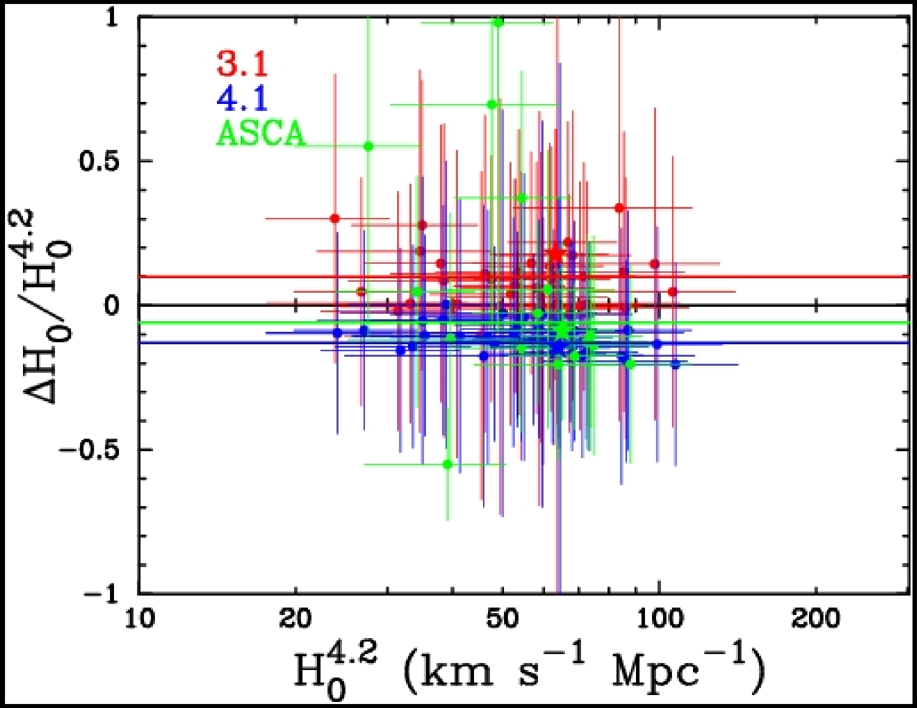
X-ray emissivitiy





The Hubble constant of each SZ cluster

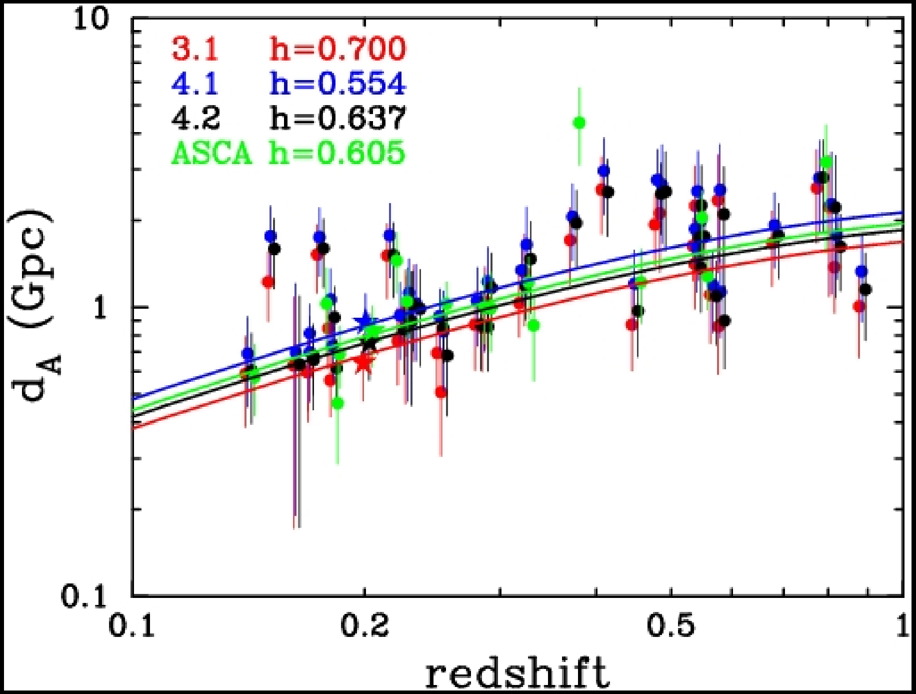


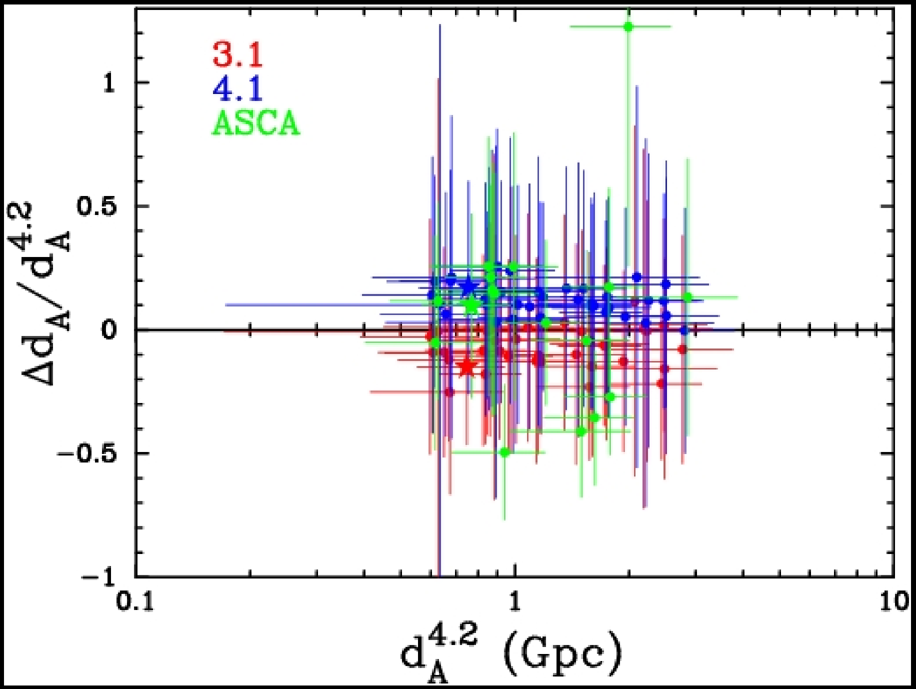


$$\frac{H_{0,2}}{H_{0,1}} = \left(\frac{T_2}{T_1}\right)^2 \frac{\Lambda_2^{\rm eff}(T_1)}{\Lambda_2^{\rm eff}(T_2)} \frac{\Lambda_1^{\rm eff}(T_1)}{\Lambda_2^{\rm eff}(T_1)} \frac{A_1(E_{\rm fid})}{A_2(E_{\rm fid})}$$

$\Omega_\Lambda=0.73$, $\Omega_m=0.27$ assumed

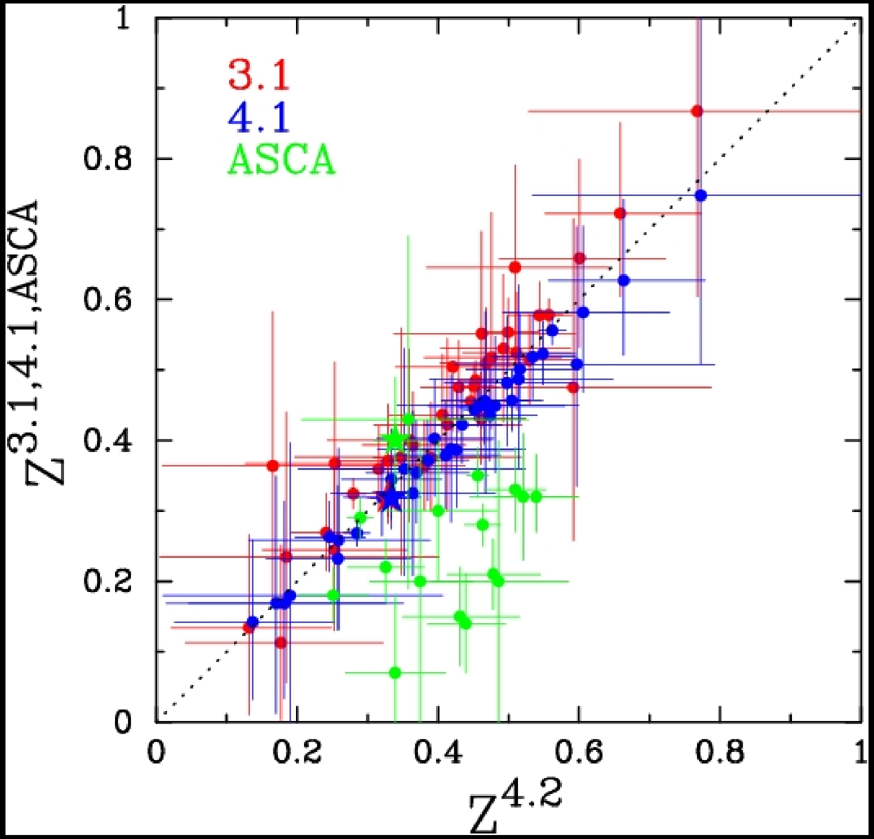
Angular diameter distances



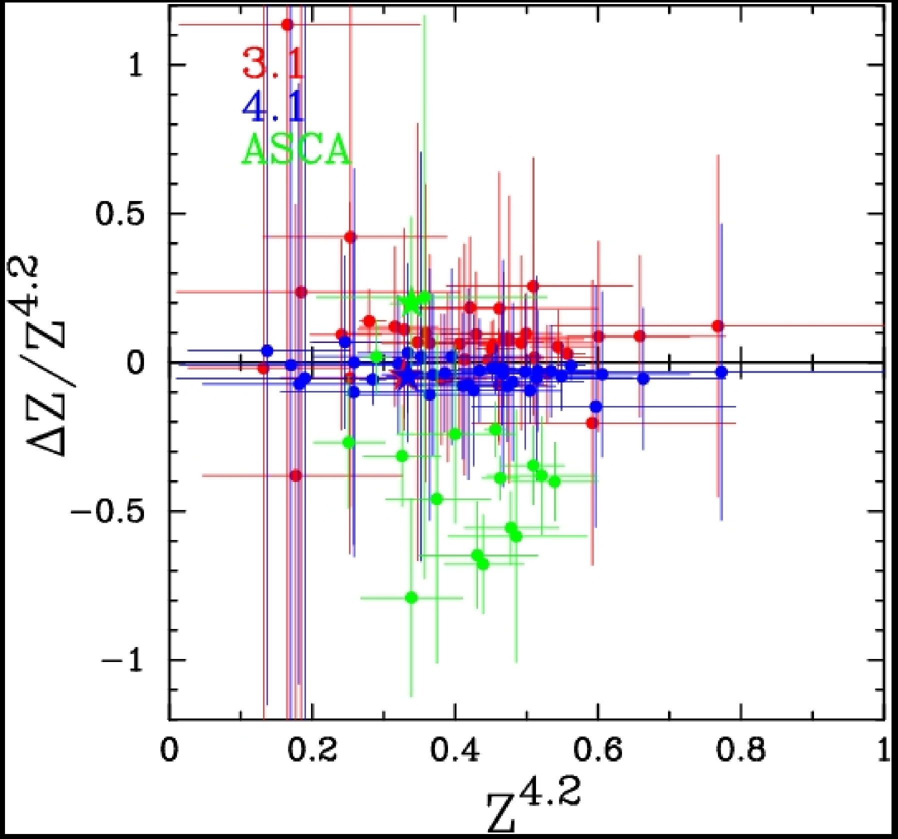


$\Omega_\Lambda = 0.73$, $\Omega_m = 0.27$ assumed

Abundances



3.1
4.1
ASCA
$Z^{3.1,4.1,ASCA}$
$Z^{4.2}$
0
0.2
0.4
0.6
0.8
1



3.1
4.1
ASCA
$\Delta Z/Z^{4.2}$
$Z^{4.2}$
1
0.5
0
−0.5
−1
0
0.2
0.4
0.6
0.8
1

Summary of comparison

Table 3. Compilation of Mean Ratios: Updated A2163 N_H

parameter	3.1/4.2	4.1/4.2	3.1/B06	4.1/B06	4.2/B06	*ASCA*/4.2
T_e	1.06 ± 0.05	0.93 ± 0.03	1.05 ± 0.11	0.92 ± 0.10	0.99 ± 0.11	0.98 ± 0.12
Z	1.08 ± 0.21	0.96 ± 0.04	1.16 ± 0.43	1.03 ± 0.31	1.08 ± 0.34	0.66 ± 0.28
$\Lambda_{\rm eff}$	1.01 ± 0.01	1.01 ± 0.01	1.03 ± 0.07	1.03 ± 0.07	1.02 ± 0.07	$\cdots$
$f_{(\nu,T_e)}$	0.998 ± 0.002	1.002 ± 0.001	0.999 ± 0.003	1.003 ± 0.004	1.001 ± 0.003	$\cdots$
A(1kev)[a]	1.01 ± 0.02	0.95 ± 0.01	0.96 ± 0.10	0.91 ± 0.10	0.95 ± 0.10	$\cdots$
d_A[b]	0.93 ± 0.08	1.13 ± 0.06	1.06 ± 0.24	1.29 ± 0.29	1.15 ± 0.25	1.07 ± 0.37

[a]B06 are the effective areas from the 3.1 calibration using only those data sets that appear in Bonamente et al. 2006.

[b]B06 are the published distances from Bonamente et al. 2006.

- Systematic difference between different calibration data of Chandra

Compilation of H_0 results

H_0	DL A2163 N_H	Updated A2163 N_H	No A2163
χ^2 Full sample	38	38	37
$H_0^{3.1}$	$82.8 \pm 4.6(75.9)$	$70.0 \pm 3.7(40.6)$	$69.7 \pm 3.7(40.5)$
$H_0^{4.1}$	$58.4 \pm 3.1(42.4)$	$55.4 \pm 2.9(34.3)$	$55.5 \pm 2.9(34.3)$
$H_0^{4.2}$	$68.8 \pm 3.7(52.2)$	$63.7 \pm 3.3(38.8)$	$63.7 \pm 3.4(38.8)$
χ^2 R02 overlap	17	17	16
$H_0^{3.1}$	$90.1 \pm 7.0(48.5)$	$66.9 \pm 4.7(15.8)$	$66.1 \pm 4.8(15.5)$
$H_0^{4.1}$	$58.2 \pm 4.1(21.2)$	$52.3 \pm 3.6(11.8)$	$52.2 \pm 3.8(11.8)$
$H_0^{4.2}$	$70.1 \pm 5.1(28.7)$	$60.5 \pm 4.3(14.4)$	$60.2 \pm 4.4(14.3)$
Avg Full sample	38	38	37
$H_0^{3.1}$	66.1 ± 30.3	62.9 ± 21.7	62.6 ± 21.9
$H_0^{4.1}$	52.5 ± 17.2	51.3 ± 15.4	51.2 ± 15.6
$H_0^{4.2}$	59.7 ± 22.1	58.0 ± 18.9	57.8 ± 19.1
Avg R02 overlap	17	17	16
$H_0^{3.1}$	68.3 ± 36.1	61.2 ± 17.6	60.4 ± 17.7
$H_0^{4.1}$	51.8 ± 16.9	49.2 ± 12.0	48.9 ± 12.3
$H_0^{4.2}$	60.0 ± 23.3	56.1 ± 15.5	55.6 ± 15.9
χ^2 B06 refit	38		37
H_0^{B06}	$76.2 \pm 4.1(55.9)$	...	$73.5 \pm 4.1(51.7)$
χ^2 R02 refit	18	17	16
H_0^{R02}	$60.8 \pm 4.0(16.5)$	$60.5 \pm 4.1(16.4)$	$60.7 \pm 4.3(16.4)$

DL:
Dickey & Lockman (1990)

R02:
Reese et al. (2002)

B06:
Bonamente et al. (2006)

$\Omega_\Lambda = 0.73$
$\Omega_m = 0.27$
assumed

Ups and downs of H_0 from SZ+Xray

X-ray data	H_0 [km/s/Mpc]	reference
ROSAT+ASCA	60 ± 3	Reese et al. (2002)
Chandra: ver.3.1	$77^{+3.9}_{-3.4}$	Bonamente et al. (2006)
WMAP	73 ± 3	Spergel et al. (2007)
Chandra: ver. 3.1	70.0 ± 3.7	this work
Chandra: ver. 4.1	55.4 ± 2.9	this work
Chandra: ver. 4.2	63.7 ± 3.3	this work

Conclusions

- X-ray calibration is not robust as believed before
  - Cluster temperature may vary ±7%
  - H_0 combined with SZ may vary ±12%
- If the latest Chandra calibration data (ver.4.2) is the most reliable, $H_0(SZ) \sim 0.9 H_0(WMAP)$
  - This might indicate the presence of the inhomogeneities in intra-cluster medium (Kawahara et al. 2008a)
- Possible systematics for cluster cosmology in general
  - ***Previous results based old Chandra calibration need to be re-examined***
  - Mass-temperature relation of clusters
  - Cluster abundances and σ_8