

# *Reliability of galaxy clusters as cosmological probes*

**Department of Physics  
University of Tokyo  
Yasushi Suto**

**Japan-Germany workshop  
on galaxies and clusters of galaxies**

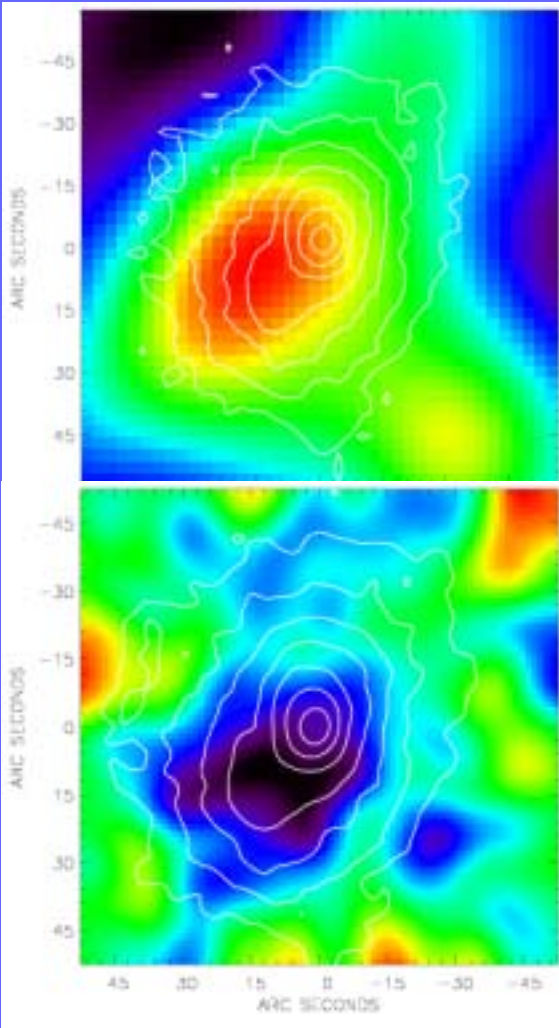
October 31, 2002@ Laforet Shuzenji, Japan

**SZ map of RX J1347-1145**

**Upper: submm (350GHz) with SCUBA at JCMT**

**Lower: mm (150GHz) with NOBA at Nobeyama**

**(Komatsu et al. 1999, 2001)**



# Precision cosmology with clusters

- Power spectrum from cluster distribution (c.f., talk by Schuecker)
- $\sigma_8 - \Omega_0$  relation from cluster abundance
- consistent with CMB, SN and galaxy surveys (c.f., talk by Boehringer).
- Certainly useful and complementary, but can it be precise enough to be competitive with the other probes, especially in the next generation ?
- Or, have we understood what are the clusters ?

# What is the definition of galaxy clusters ?

## Abell (optical) clusters

the Abell radius  
 $m_3 < m < m_3 + 2$   
richness class

## Press-Schechter halos

spherical collapse  
 $\text{vir} = 18^2$

## *SZ clusters*

$I_{\text{SZ}}$   
 $n_e T_e$

## Halos in N-body simulations

friend-of-friend  
linking length = 0.2

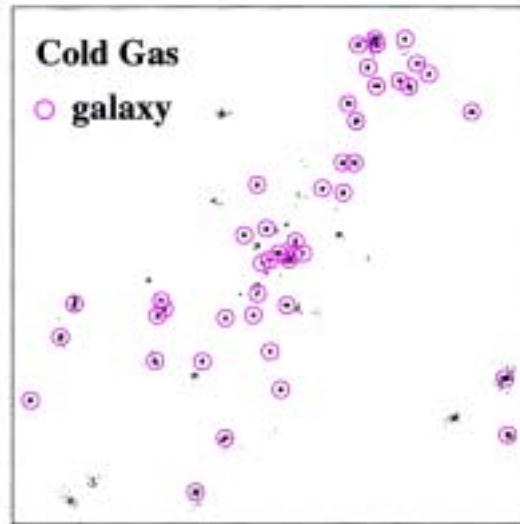
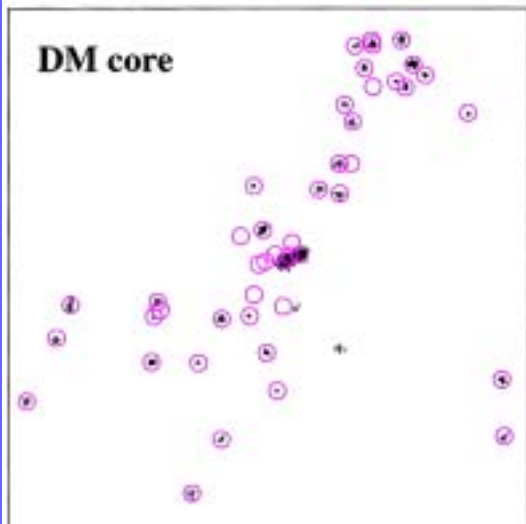
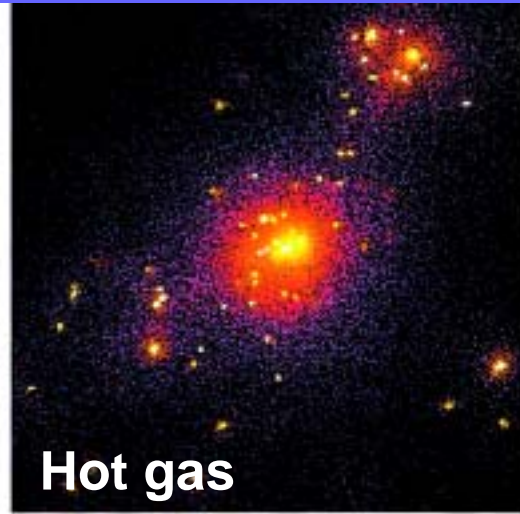
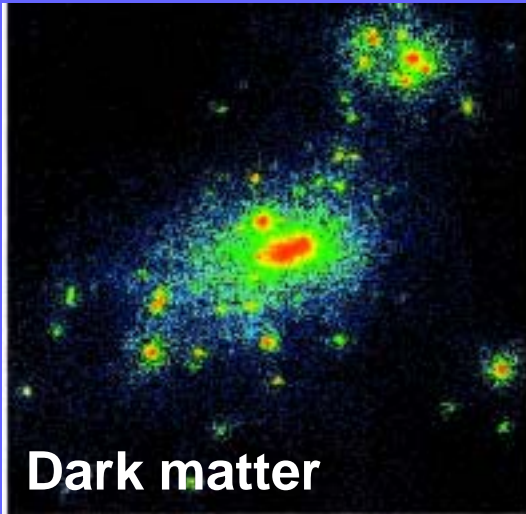
## *X-ray clusters*

$S_x$   $n_e^2 T_e^{1/2}$

- Definitely they are closely related, but the exact one-to-one correspondence is unlikely....

# Relation between dark halos and clusters

A cluster-size halo ( $8 \times 10^{14} M_{\text{sun}}$  at  $z=0$ )



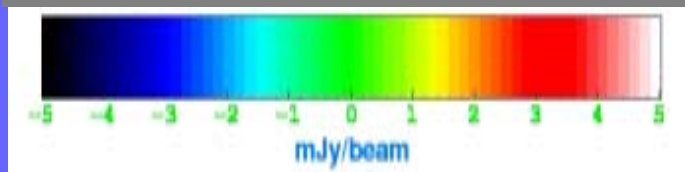
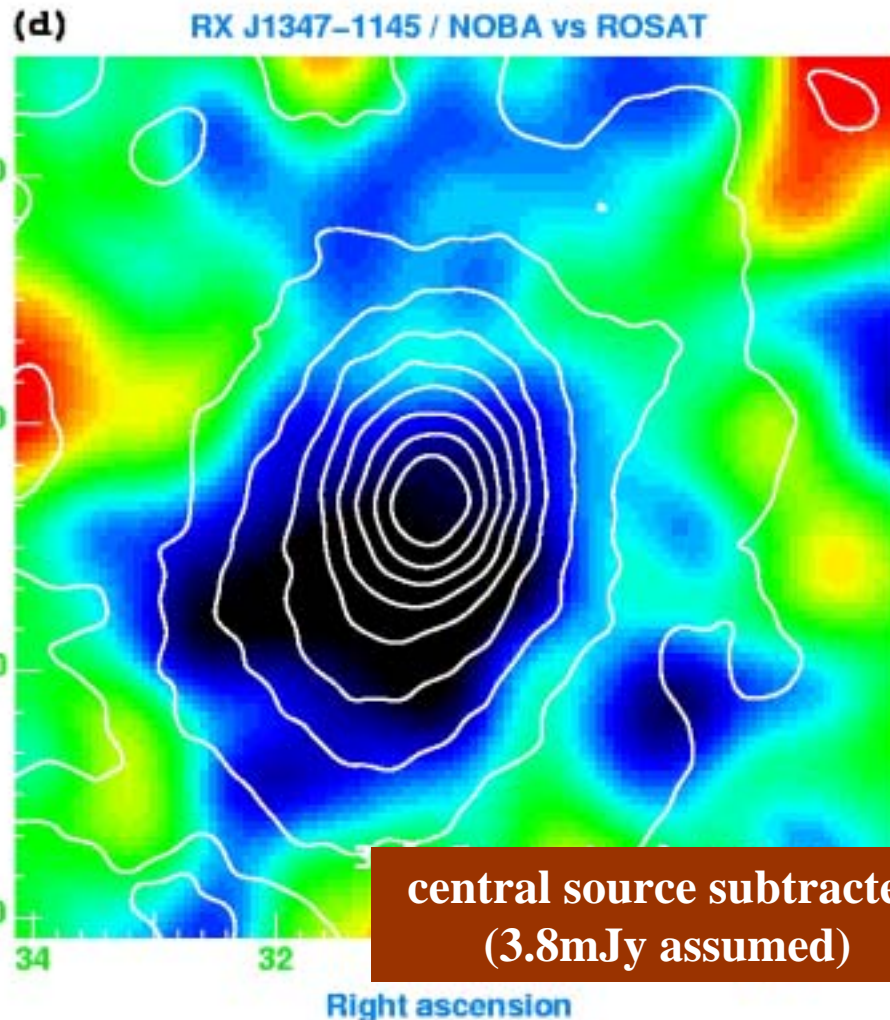
- Globally similar distribution, but their precise relation is unclear because definitions of clusters (especially at high  $z$ ) are very ambiguous.

SPH simulations in LCDM:  
 $N=128^3$  boxsize:  $75 h^{-1} \text{Mpc}$   
(Yoshikawa, Taruya,  
Jing & Suto 2001)

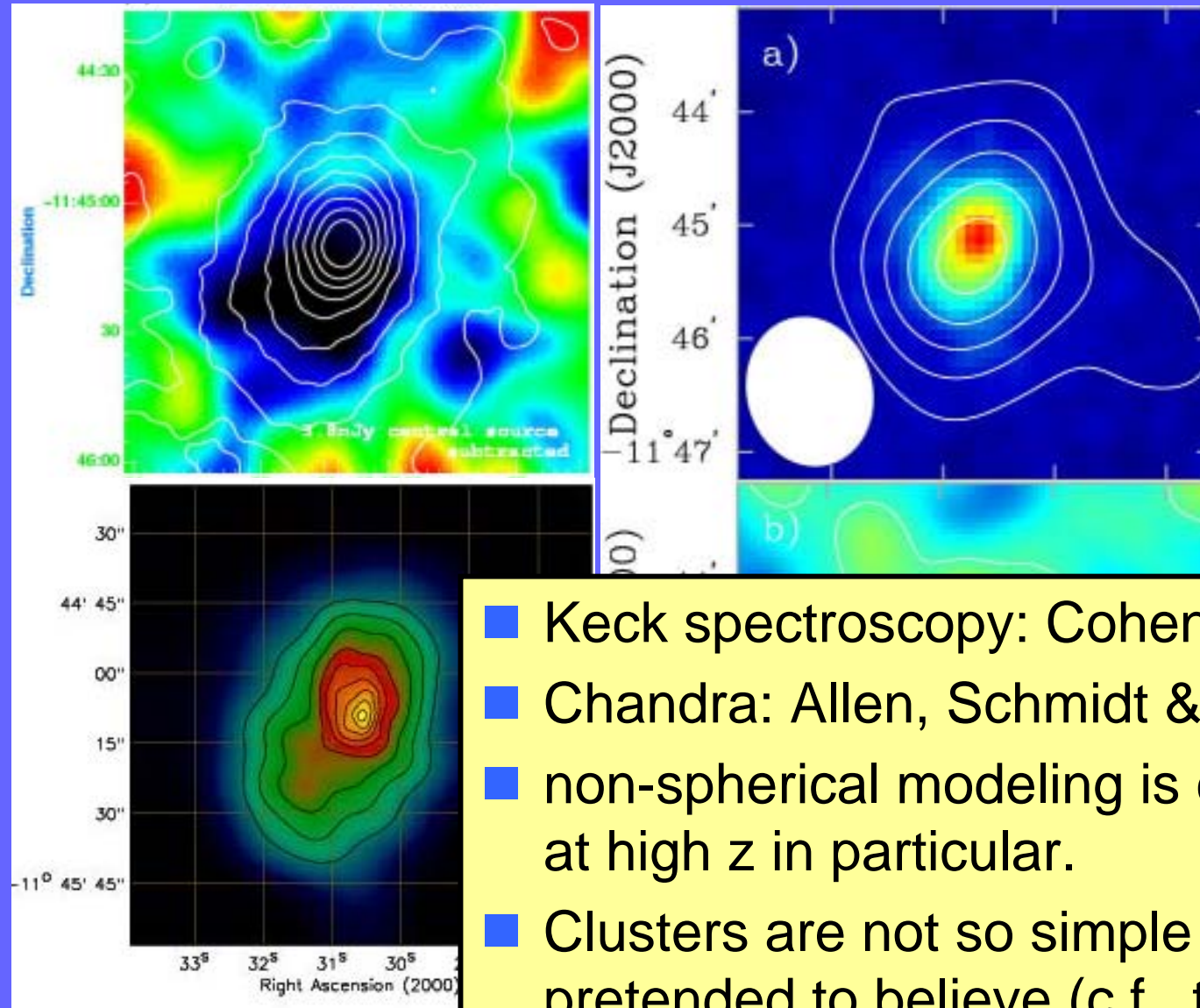
# An example; substructure of RXJ1347-1145 ( $z=0.45$ ) detected via SZ map at 150 GHz

150GHz with NOBA  
(Nobeyama Bolometer  
Array) at Nobeyama  
45m telescope  
in March, April, 1999  
and February 2000  
**FWHM=13"**

- Globally similar morphology to the X-ray image
- Substructure in the South-East direction



# Confirmed by Chandra and BIMA observations



RXJ1347-1145

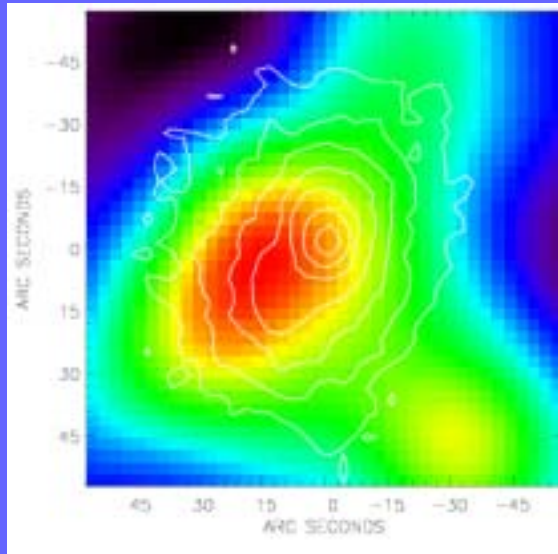
BIMA@30GHz  
63" x 80" beam  
(10.3mJy point  
source removed)

Carlstrom et al.  
(2001)

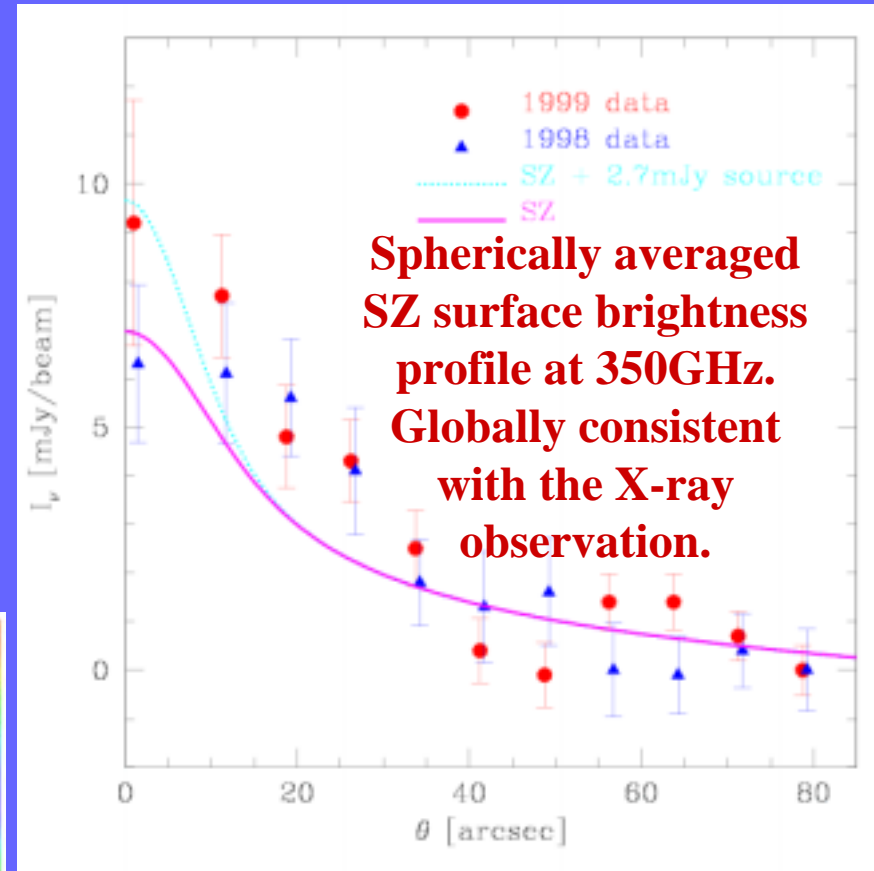
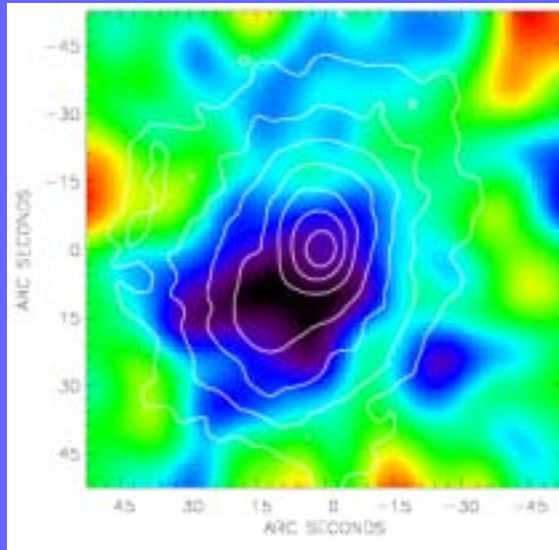
- Keck spectroscopy: Cohen & Kneib (2002)
- Chandra: Allen, Schmidt & Fabian (2002)
- non-spherical modeling is crucial, perhaps at high  $z$  in particular.
- Clusters are not so simple as we have pretended to believe (c.f., talk by Briel)

# Submm map (350GHz) of RX J1347-1145

The first SZ map of a cluster in the submm band with SCUBA, JCMT. (contours: Chandra X-ray map)

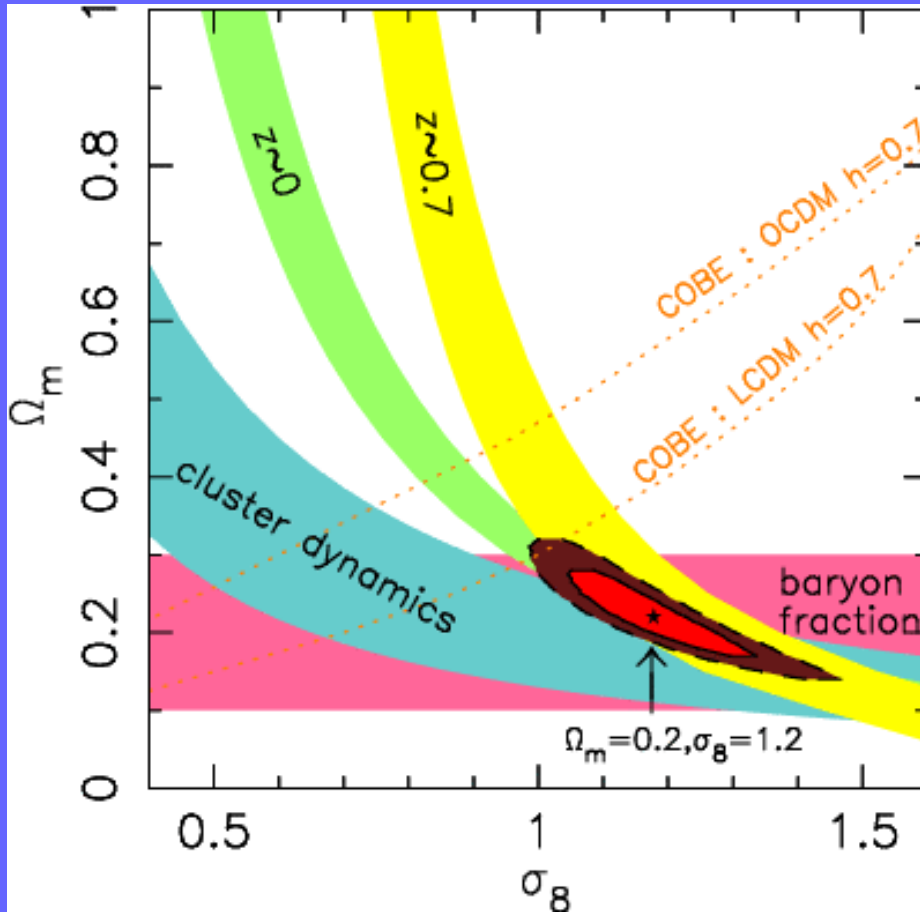


The highest angular resolution SZ map of a cluster in the mm band with NOBA, Nobeyama

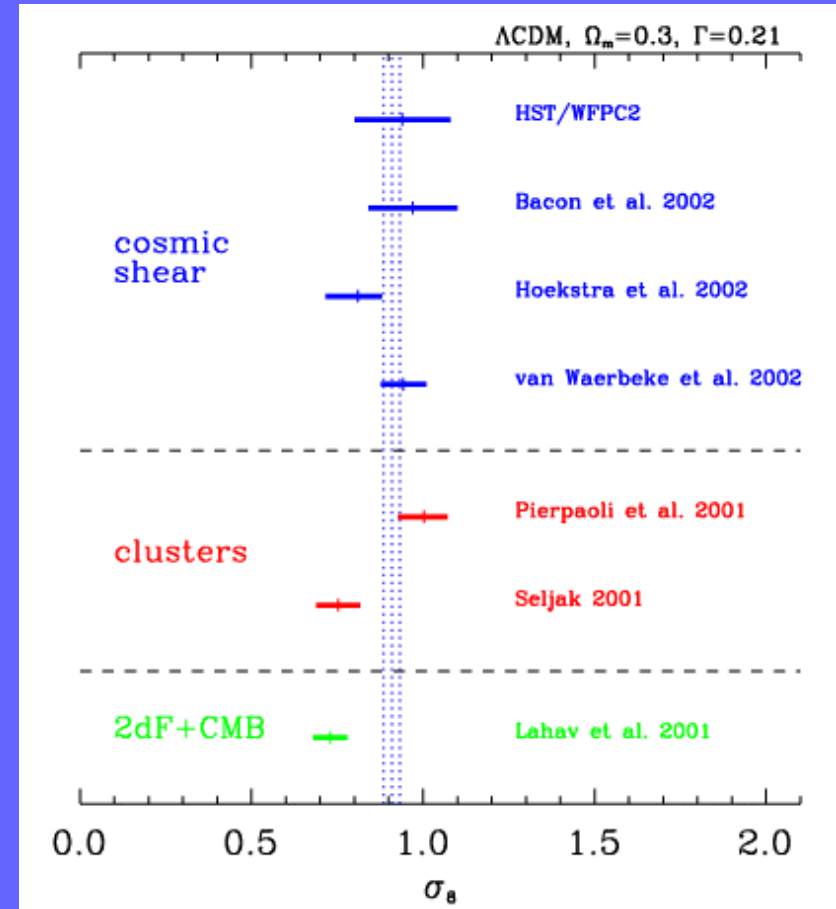


Komatsu et al.  
ApJ 516(1998)L1  
PASJ 53(2001)57

# $\sigma_8$ from cluster abundances and lensing



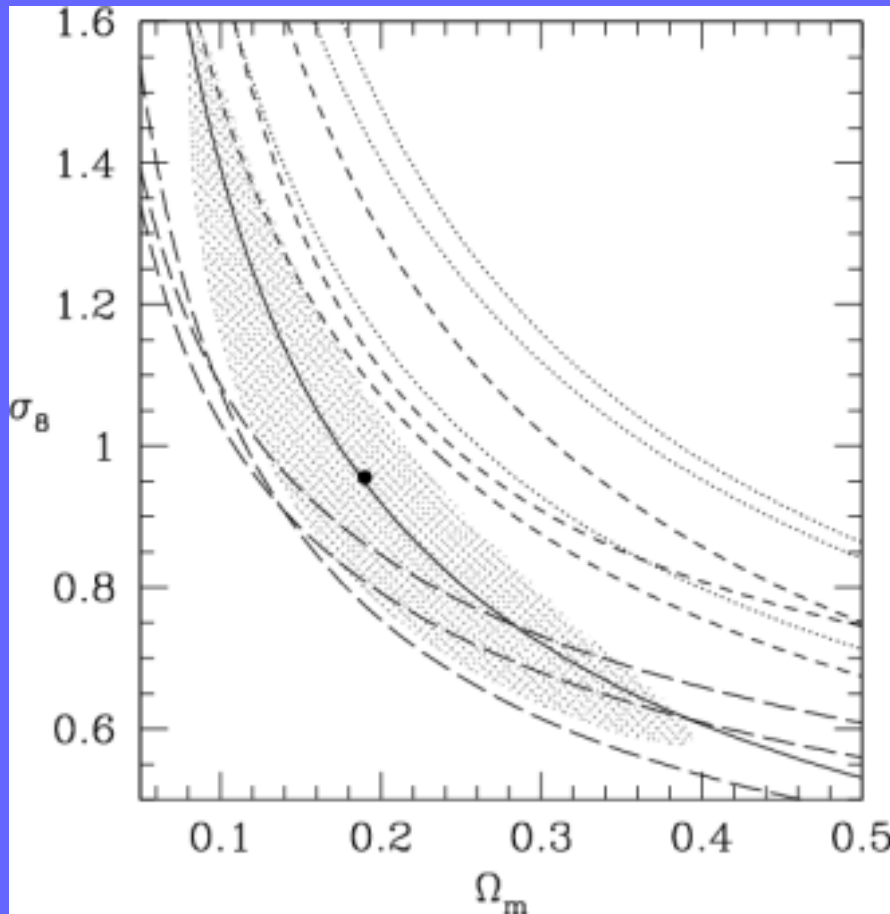
N.Bahcall:  
 Physica Scripta T85(2000)32



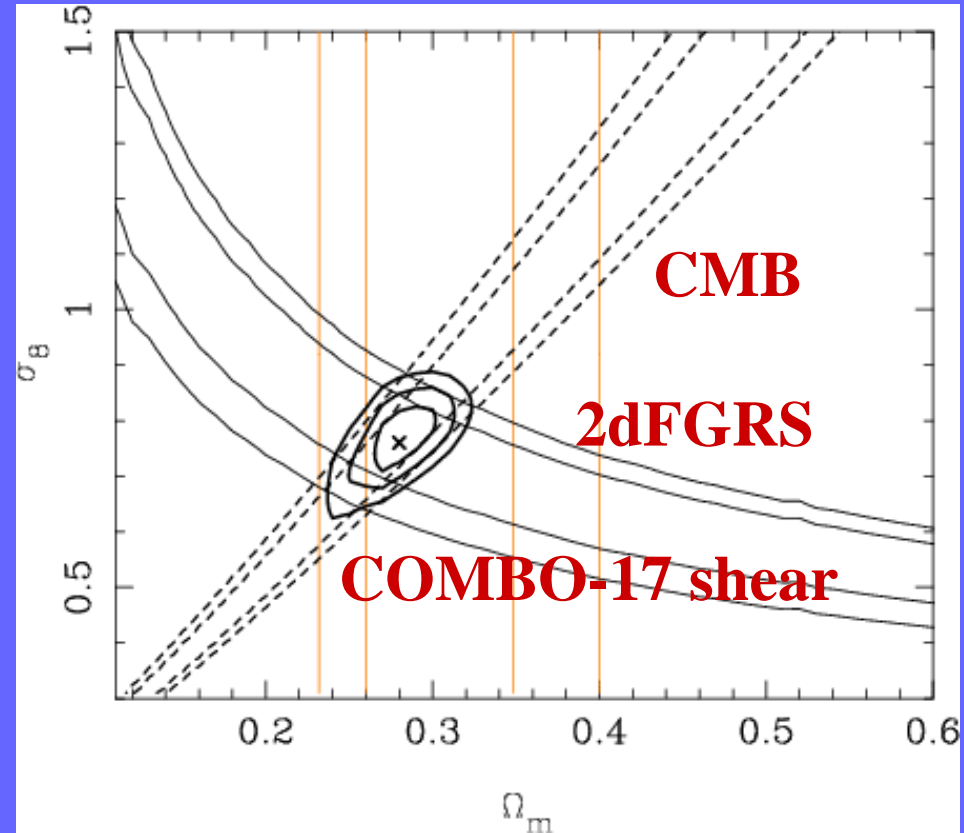
Refregier et al.  
 ApJ 572(2002)131



# More recent estimate of $\sigma_8$

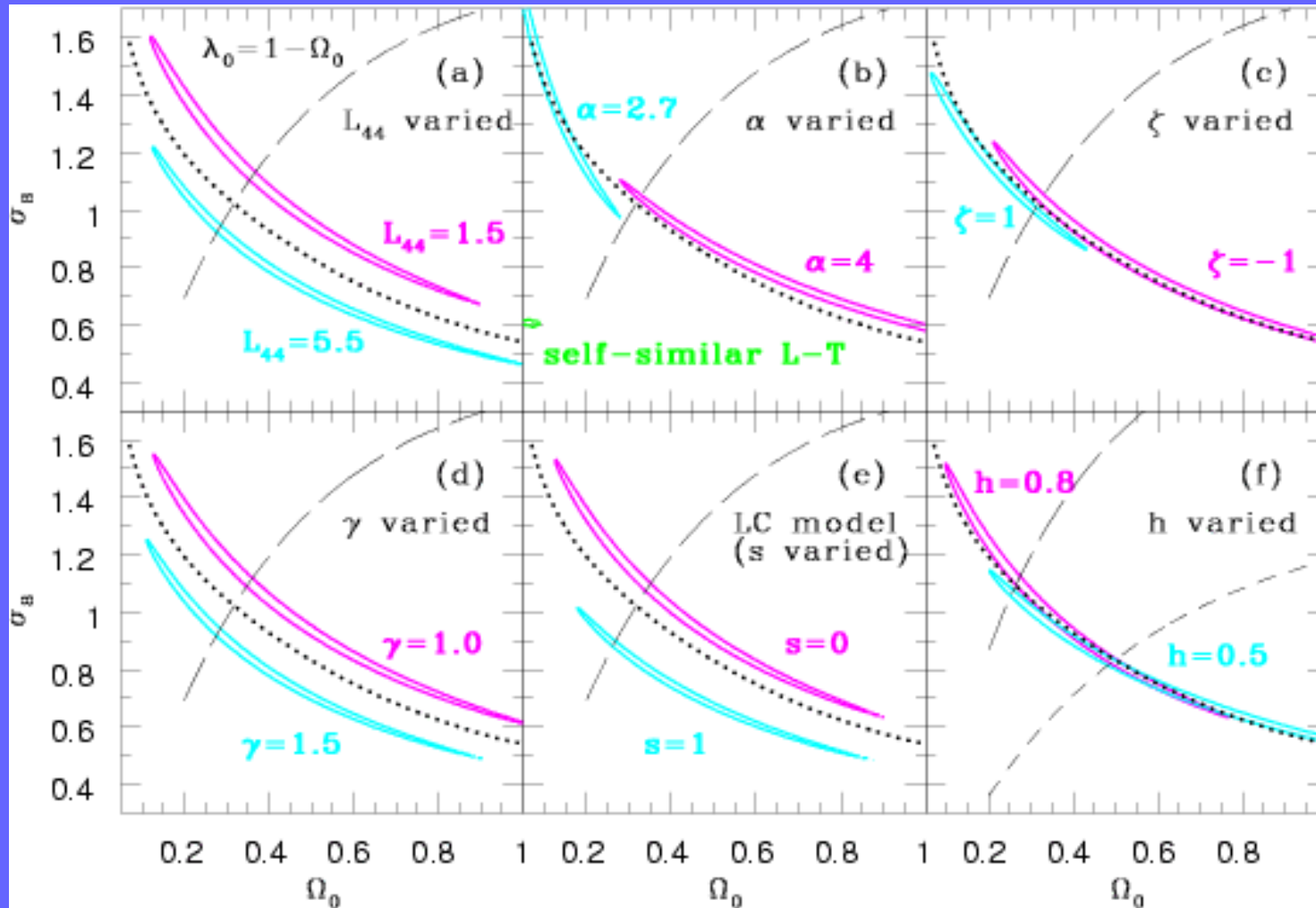


Bahcall et al.(SDSS)  
astro-ph/0205490



Brown et al.  
astro-ph/0210213  
COMBO-17 survey

# Systematic uncertainties



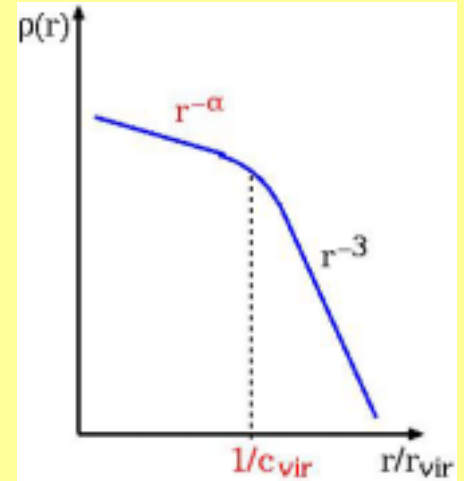
Kitayama & Suto ApJ 490(1997)557

# Theoretical modeling of X-ray clusters

## ■ Halo density profile

$$\rho(r) = \frac{\delta_c \rho_{crit}}{(r/r_s)^\alpha (1+r/r_s)^{3-\alpha}}$$

$$c_{vir}(M) \equiv \frac{r_{vir}(M)}{r_s(M)} = \frac{9}{1+z} \left( \frac{M}{2 \times 10^{13} h_{70}^{-1} M_{Sun}} \right)^{-0.13}$$



## ■ Hydrostatic equilibrium gas distribution

$$\rho_{gas}(r) = \rho_{gas,0} \exp \left[ \frac{2c_{vir}}{m(c_{vir})} \frac{T_{vir}}{T_{gas}} f(x) \right]$$

$$f(x) = 1 - \frac{\ln(1+x)}{x} \quad (\alpha = 1)$$

$$= 2\sqrt{\frac{1+x}{x}} - \frac{2}{x} \ln(\sqrt{x} + \sqrt{1+x}) \quad (\alpha = 3/2) \Rightarrow \text{analytic!}$$

# Mass – temperature relation to X-ray luminosity

- Convert the observed MT relation ( $M_{500}$  and  $M_{2500}$  to  $M_{\text{vir}}$  in our adopted dark matter halo profile) :

- Finoguenov et al. (2001)

$$T_{\text{gas}} = (1.92 \pm 0.06) \text{keV} \left( \frac{M_{\text{vir}}}{10^{14} h_{70}^{-1} M_{\text{Sun}}} \right)^{0.54 \pm 0.02} \quad (\alpha = 1)$$

- Allen et al. (2001)

$$T_{\text{gas}} = (1.53 \pm 0.56) \text{keV} \left( \frac{M_{\text{vir}}}{10^{14} h_{70}^{-1} M_{\text{Sun}}} \right)^{0.57 \pm 0.12} \quad (\alpha = 1)$$

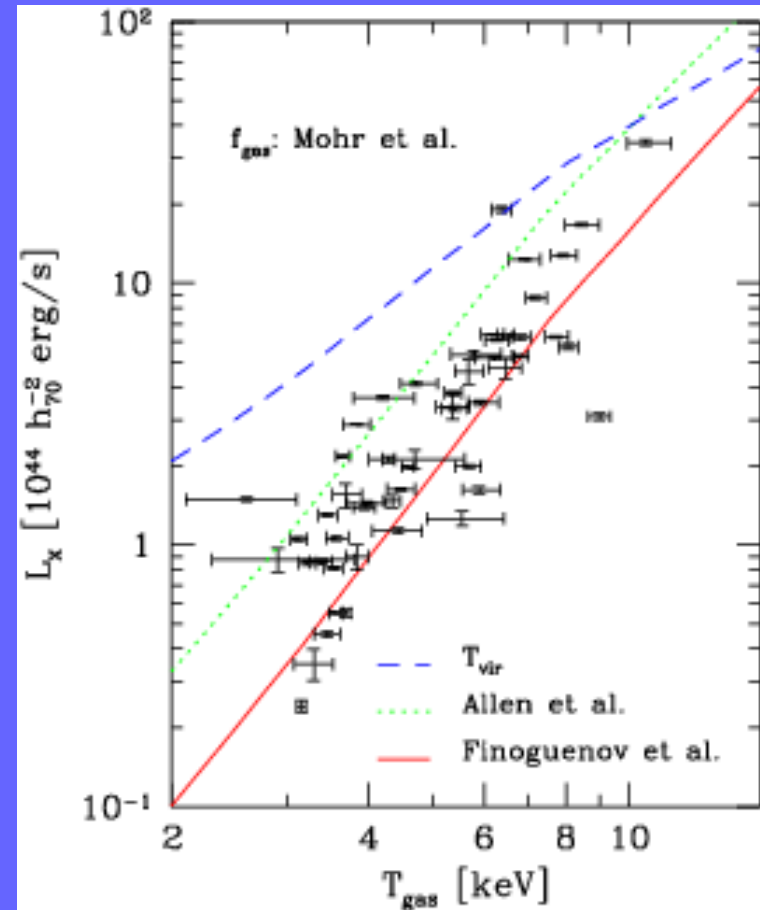
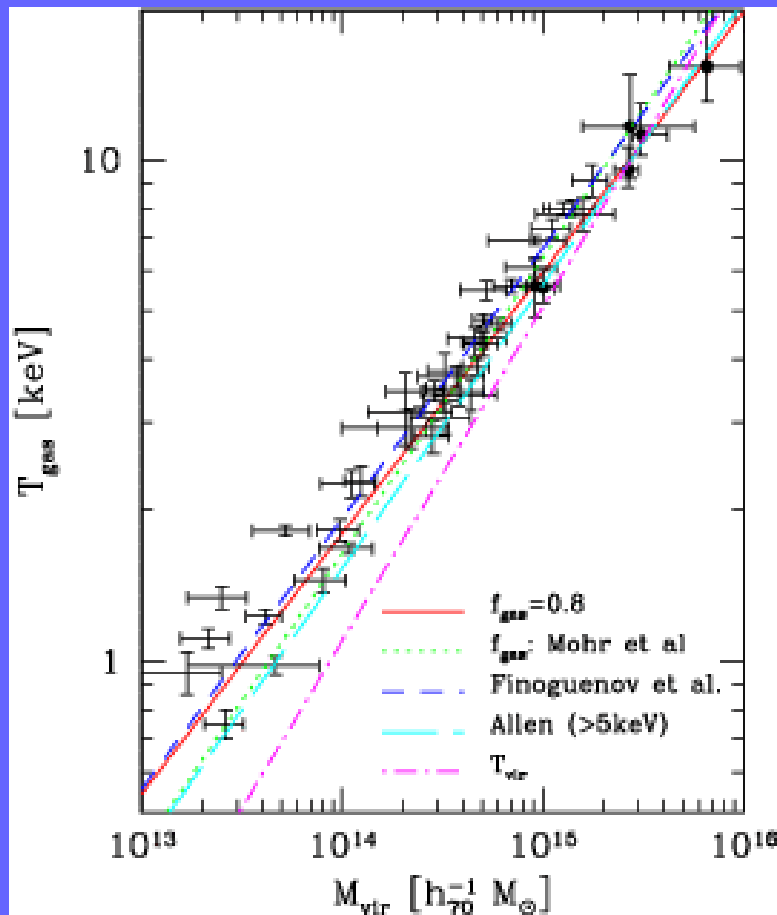
- Gas mass fraction (Mohr et al. 1999)

$$f_{\text{gas}} = \min \left[ 0.92 h_{70}^{-3/2} \left( \frac{T_{\text{gas}}}{6 \text{keV}} \right)^{0.34}, 1 \right]$$

- Compute the X-ray luminosity

$$L_X = 4\pi \int_0^{r_{\text{vir}}} \Lambda(T_{\text{gas}}, Z) \left( \frac{\rho_{\text{gas}}(r)}{\mu m_{\text{proton}}} \right)^2 r^2 dr$$

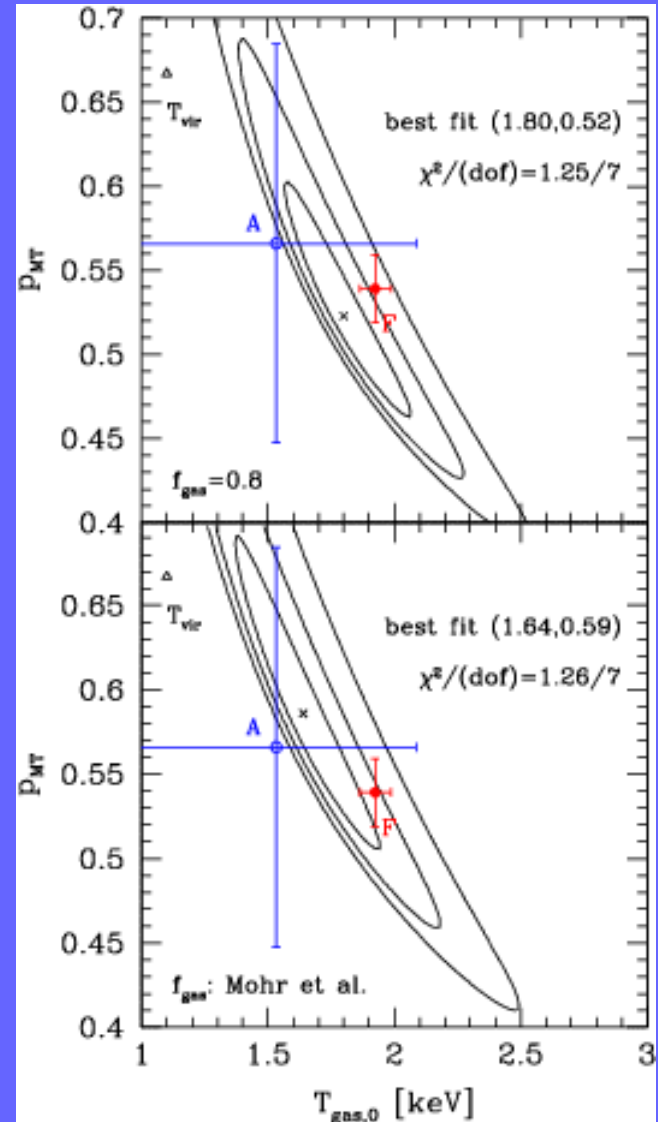
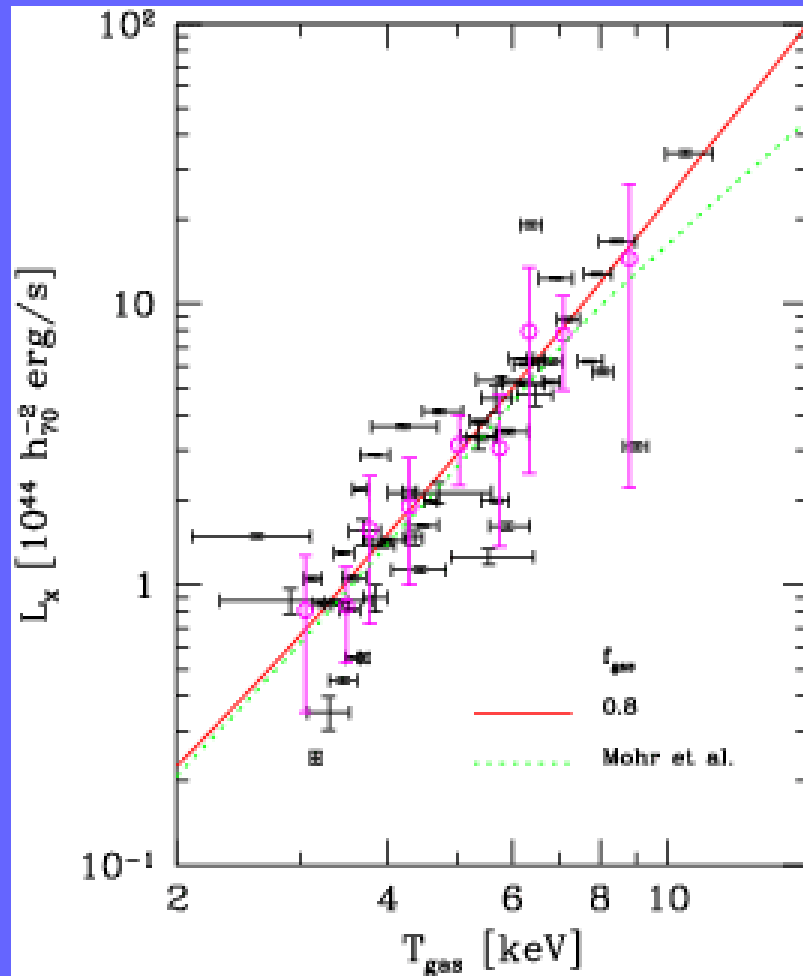
# From the observed mass-temperature relation to the luminosity-temperature relation



■ L-T relation is sensitive to M-T relation

# Limits on a parameterized M-T relation from the observed L-T relation

$$T_{gas} = T_{gas,0} \left( \frac{M_{vir}}{10^{14} h_{70}^{-1} M_{Sun}} \right)^{P_{MT}}$$



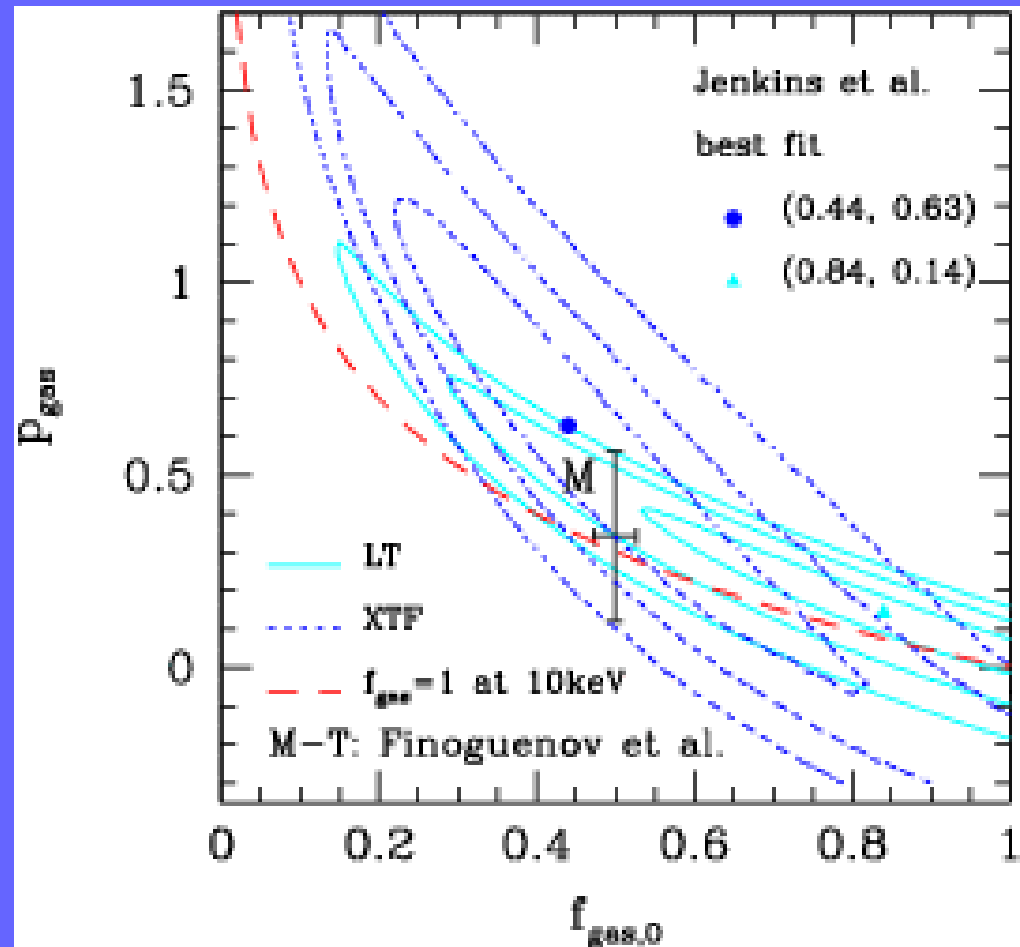
# Limit on gas mass fraction from the observed L-T relation

$$f_{gas}(T_{gas}) = f_{gas,0} \left( \frac{T_{gas}}{1 \text{ keV}} \right)^{p_{gas}}$$

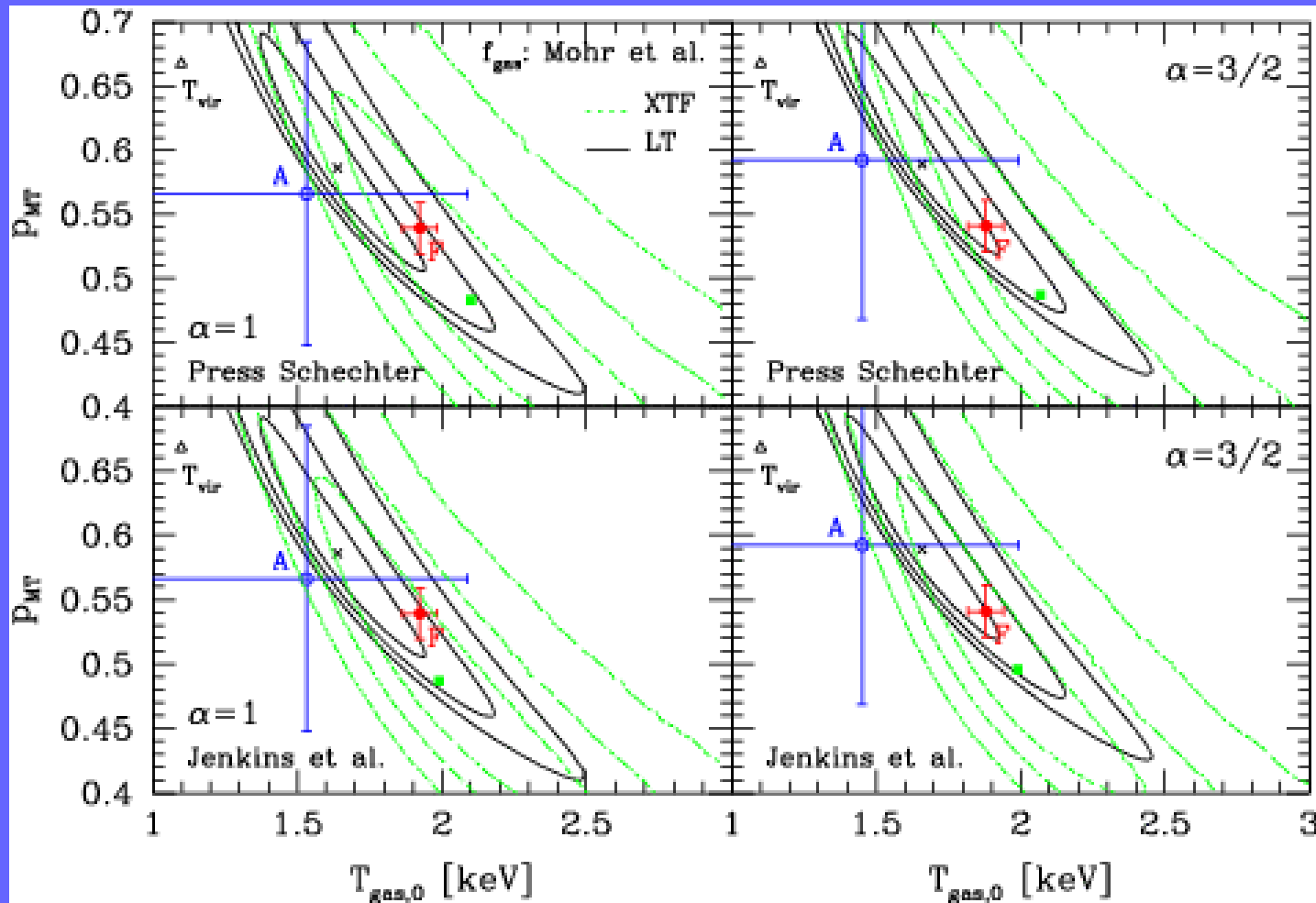
c.f., Mohr et al. (1999)

$$f_{gas} = 0.92 h_{70}^{-3/2} \left( \frac{T_{gas}}{6 \text{ keV}} \right)^{0.34}$$

Shimizu, Kitayama,  
Sasaki & Suto (2003)



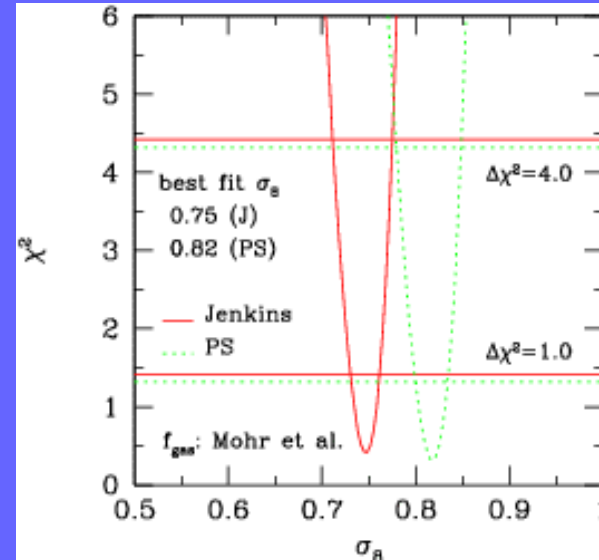
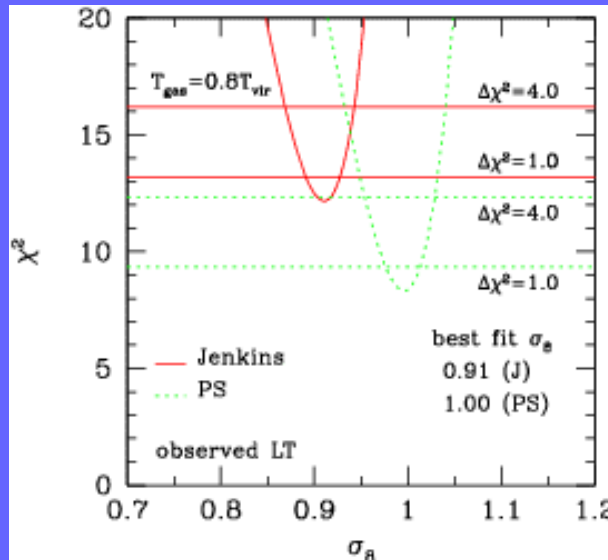
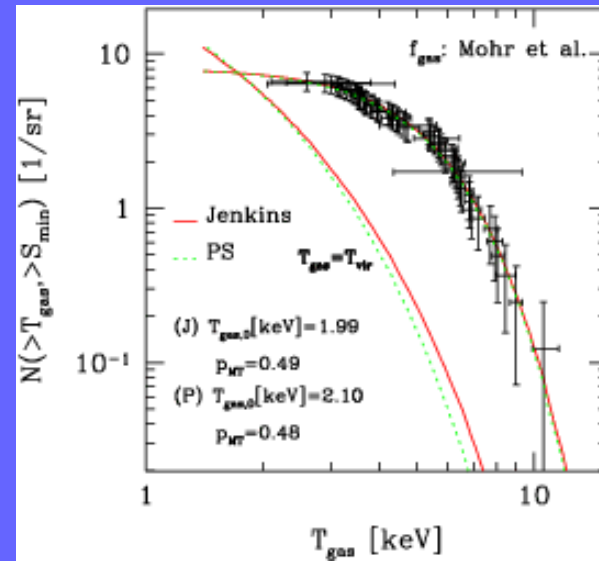
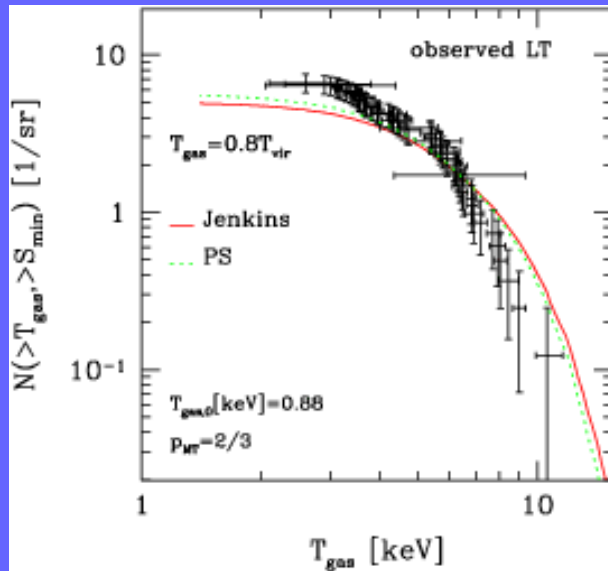
# Limits on a parameterized M-T relation from the observed L-T relation and XTF



Shimizu, Kitayama, Sasaki & Suto (2003)



# $\sigma_8$ from the observed Xray temperature function



# Conclusions

- One can perform statistical analysis of X-ray clusters, *provided a good physical model for halo-cluster connection **beyond the unrealistic one-to-one correspondence*** .
- ***From dark halos to visible objects:***
  - halo mass -- cluster gas temperature relation
  - non-gravitational effects inside dark halos (cooling, star/galaxy formation, preheating, supernova feedback, etc.)
- ***The goal of the next generation cluster surveys is not precision cosmology, but is to understand “what are the clusters of galaxies”.***