



*Clustering
of dark matter halos
on the light-cone*



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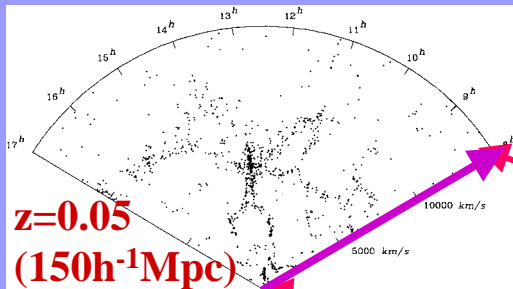
June 13, 2001@第八回台北天文物理検討会

Clustering on the light-cone

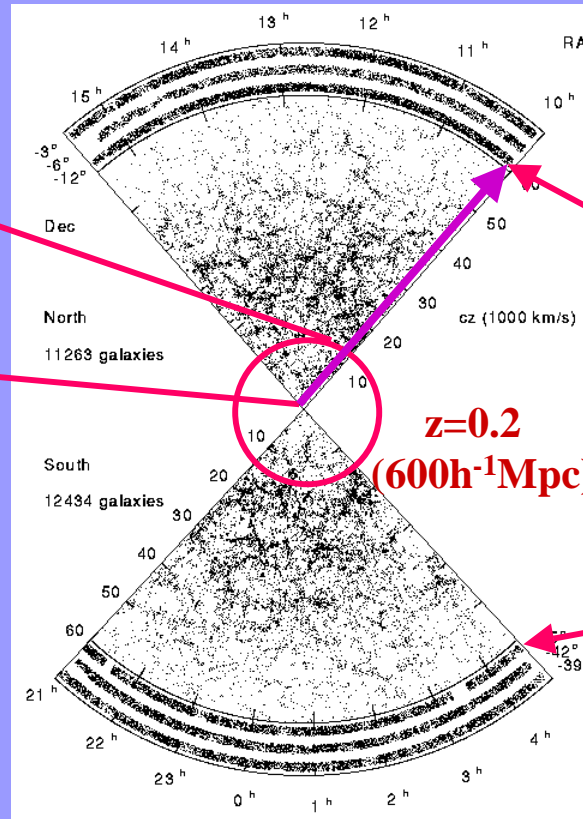
1996

2000

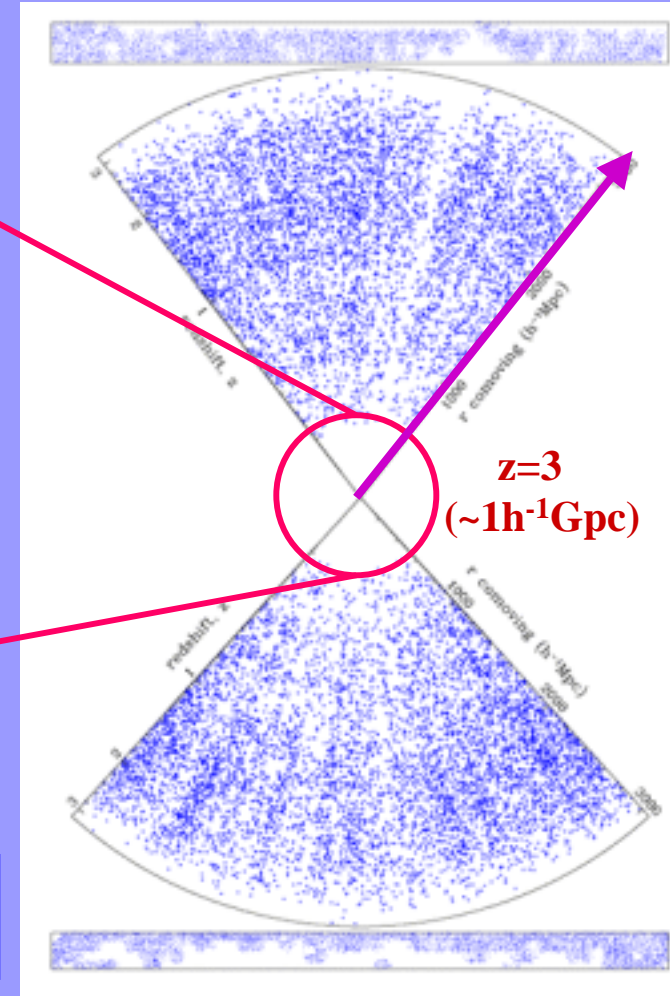
1986



CfA redshift survey:
de Lapparent et al.(1986)



Las Campanas redshift survey:
Schechter et al. (1996)



2dF QSO survey: Shanks et al. (2000)

■ **Evolution along the light-cone is essential even in the current surveys !**

Evolution of “object(s)”

$$z=4.73 \times 10^{-10}$$

$$z=4.60 \times 10^{-10}$$

$$z=4.38 \times 10^{-10}$$

$$z=3.68 \times 10^{-10}$$

$$z=1.45$$

(the Ein
and

redshift

- evolution is rapid !
- evolution is strongly object-dependent.
- evolution cannot be neglected.

Cosmological light-cone effects

- *linear and nonlinear gravitational evolution*
- *redshift-space distortion due to peculiar velocity*
 - linear distortion (the Kaiser effect)
 - nonlinear distortion (finger-of-god effect)
- *evolution of objects on the light-cone*
 - number density (magnitude-limit, luminosity function, etc.)
 - object-dependent biasing relative to mass distribution
- *observational selection function*
 - magnitude-limit and luminosity function
 - shape of the survey boundary

Matsubara, Suto & Szapudi (1997); Mataresse et al. (1997)

Yamamoto & Suto (1998); Suto, Magira, Jing, Matsubara & Yamamoto (1999)

Predicting the clustering on the light-cone

■ redshift-space distortion

$$\xi(r; z) = \frac{1}{2\pi^2} \int_0^\infty k^2 dk P_{nl}^R(k, z) f(k, \beta, \sigma_{1D, \text{vel}}) \frac{\sin kr}{kr}$$

gravitational
nonlinear evolution

linear and nonlinear
redshift-space distortion

■ average over the light-cone

$$\xi^{LC}(r) = \frac{\int_{z_{\min}}^{z_{\max}} dz \xi(r; z) [\phi(z)n(z)]^2 \frac{dV_c}{dz}}{\int_{z_{\min}}^{z_{\max}} dz [\phi(z)n(z)]^2 \frac{dV_c}{dz}}$$

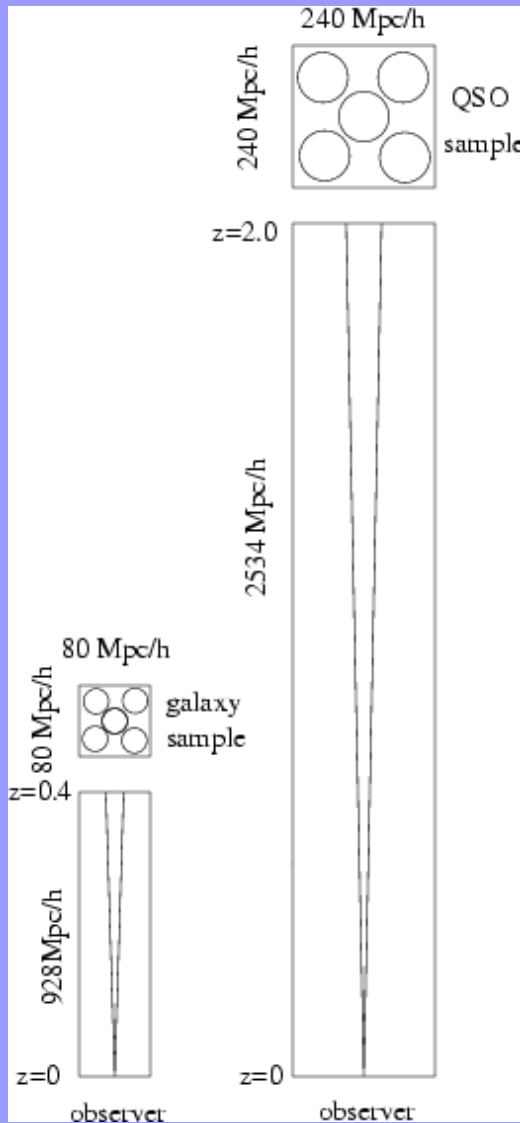
selection function

mean number density

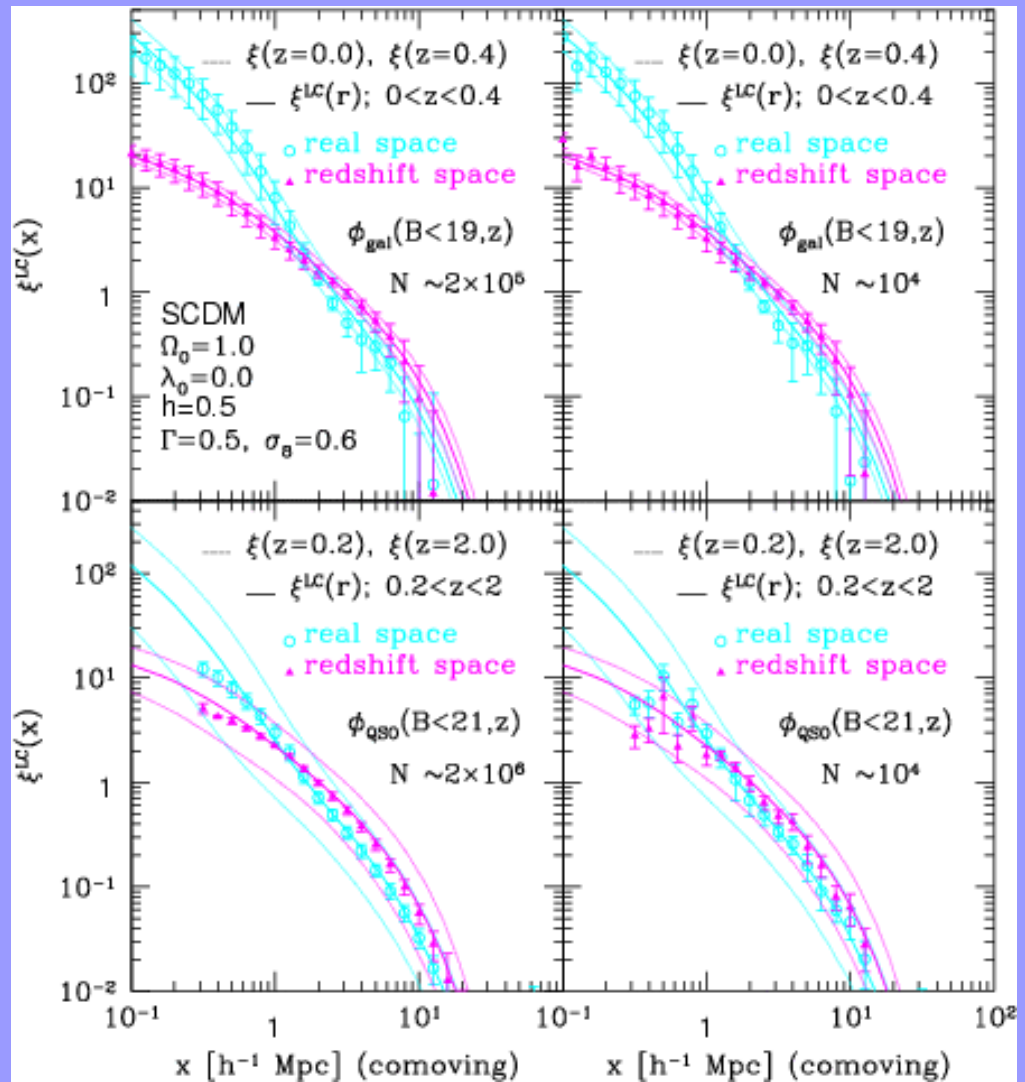
comoving
volume
element

Hamana, Colombi & Suto (2001)

Correlation functions of *dark matter* on the light-cone



Bias is ignored here.

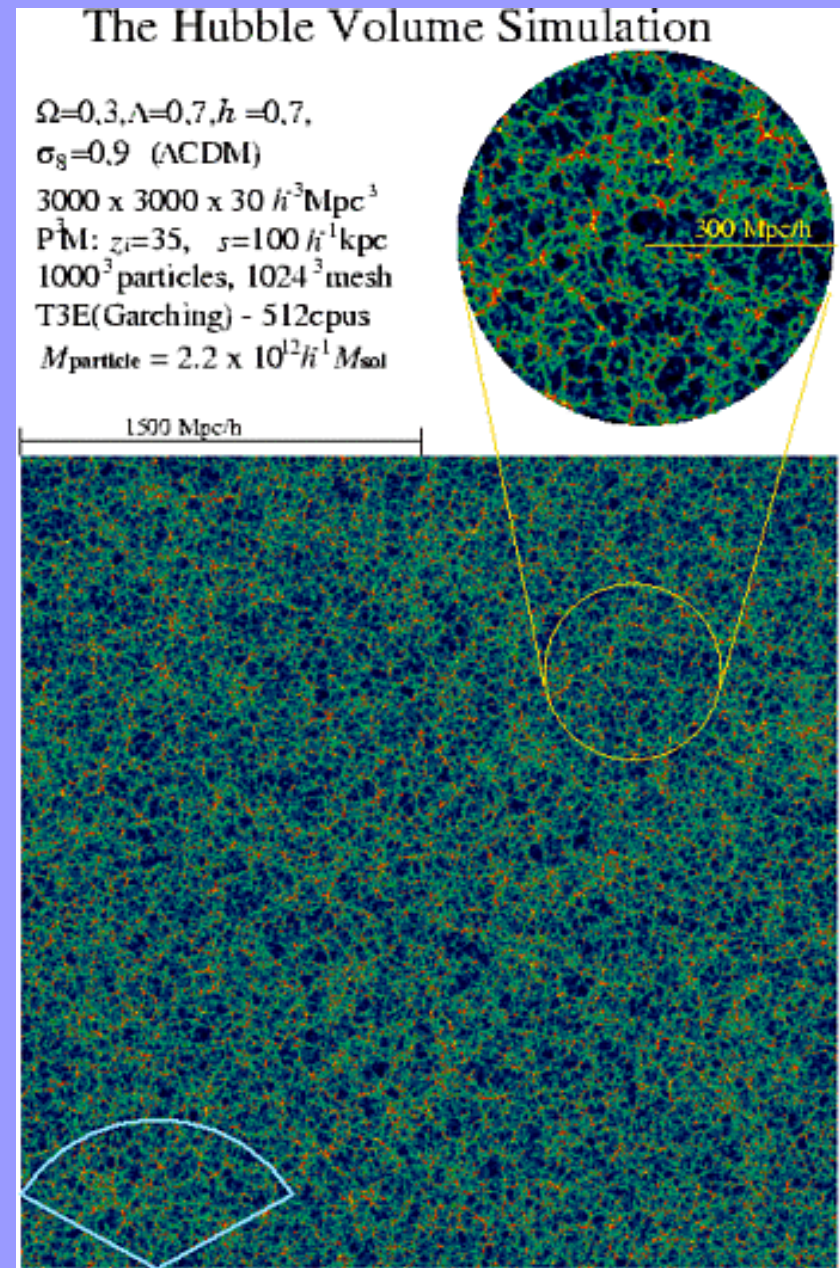


Hamana, Colombi & Suto (2001)

Hubble volume CDM simulation

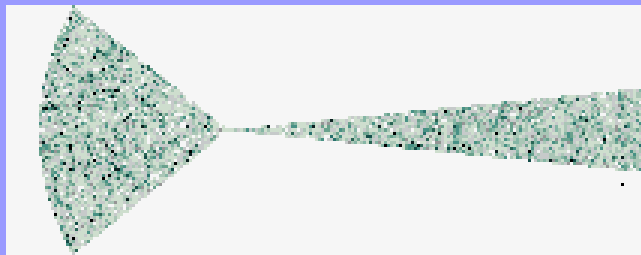
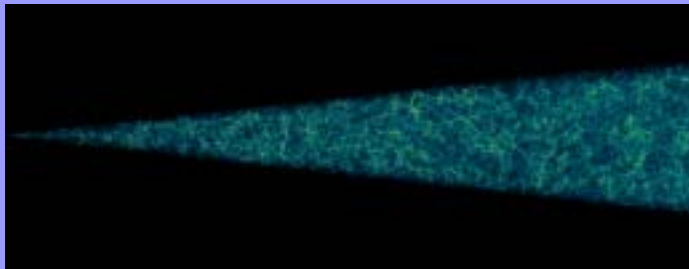
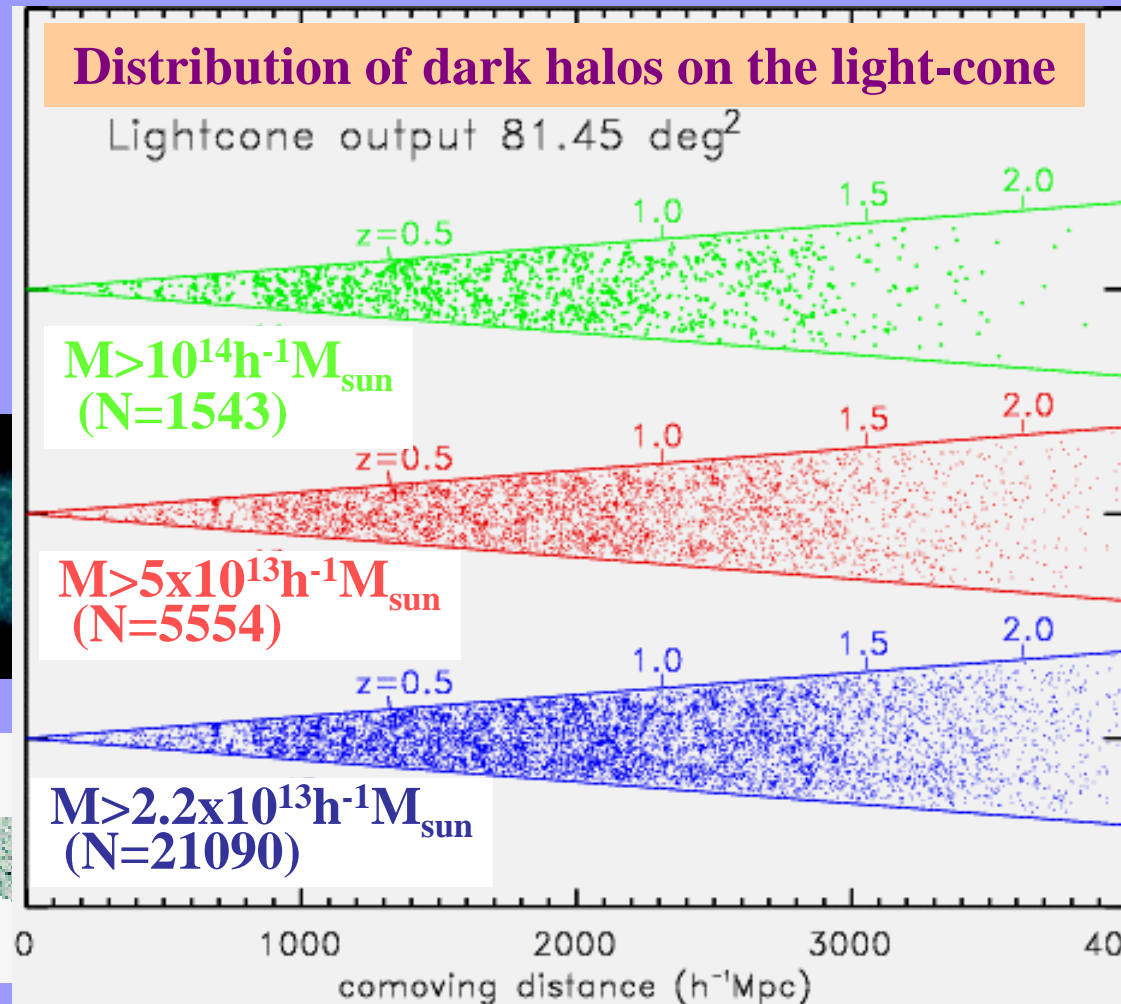
- P³M N-body simulation
- N=10⁹ particles in a (3000h⁻¹Mpc)³ box
- CDM: $\Omega_0=0.3$, $\Lambda_0=0.7$,
h=0.7, $\sigma_8=0.9$
- $m_{\text{particle}}=2.2 \times 10^{12}h^{-1}M_{\text{sun}}$
- $r_{\text{grav}}=100h^{-1}\text{kpc}$

The Virgo Consortium
<http://www.physics.isa.umich.edu/hubble-volume/>



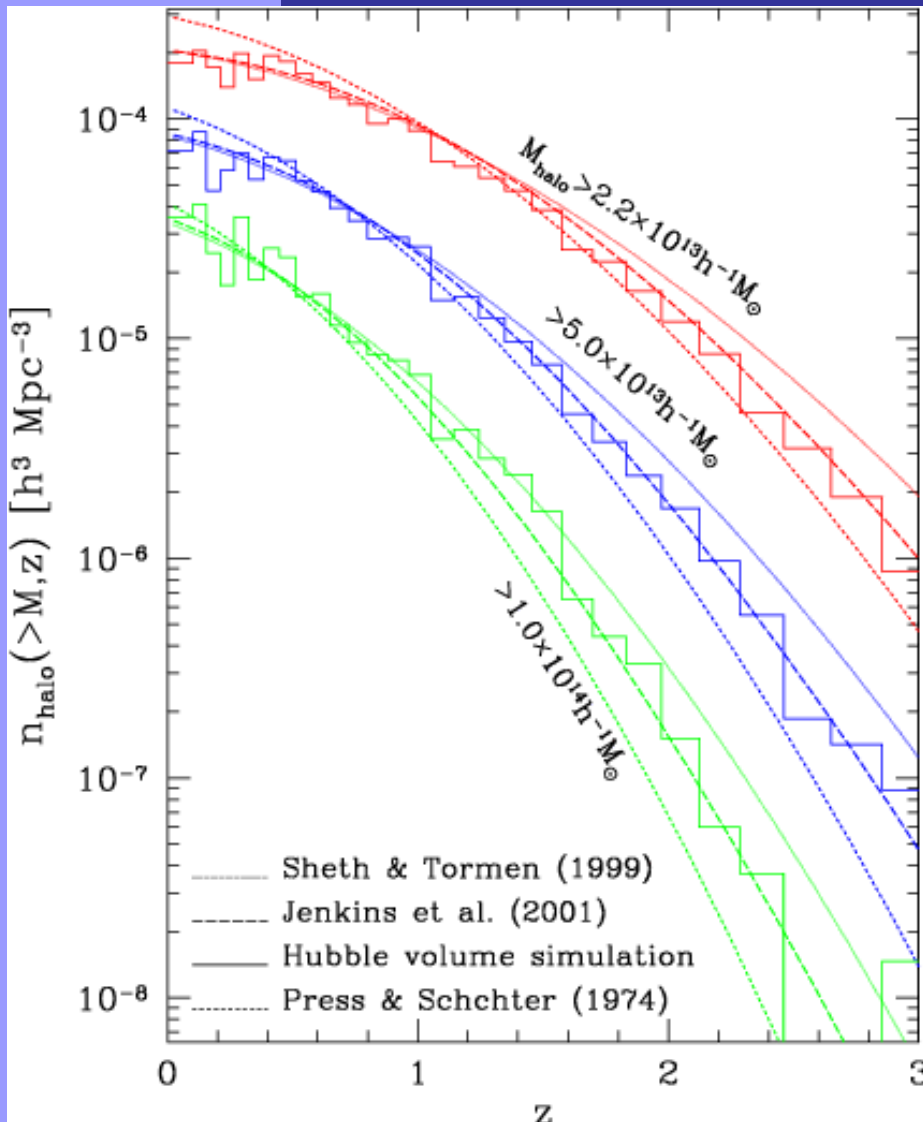
Light-cone output from the Hubble volume simulation

<http://www.physics.isa.umich.edu/hubble-volume/lightcones.htm>



Hamana, Yoshida, Suto & Evrard (2001)

Mass function of dark halos



- The Press-Schechter mass function underpredicts, while an empirical correction by Sheth & Tormen (1999) overpredicts, the Hubble volume simulation data at high mass (Jenkins et al. 2001).

Hamana, Yoshida, Suto & Evrard (2001)

Phenomenological model for scale- and mass-dependent halo biasing

- mass-dependence (Jing 1998; Sheth & Tormen 1999) + scale-dependence (Taruya & Suto 2000) in halo biasing

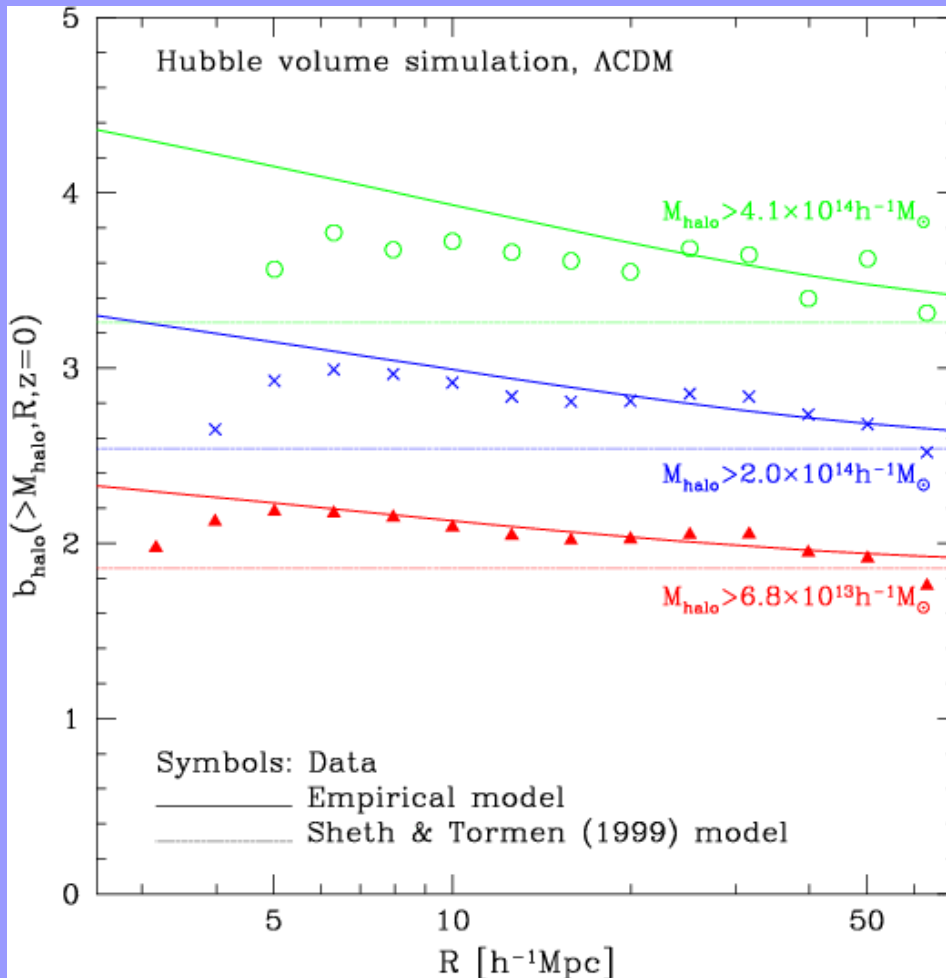
$$b_{halo}(M, R, z) = b_{ST}(M, z) [1 + b_{ST}(M, z) \sigma_{mass}(R, z)]^{0.15}$$

$$\xi_{halo}(M, R, z) = b_{halo}^2(M, R, z) \xi_{mass}(R, z)$$

- average over the light-cone

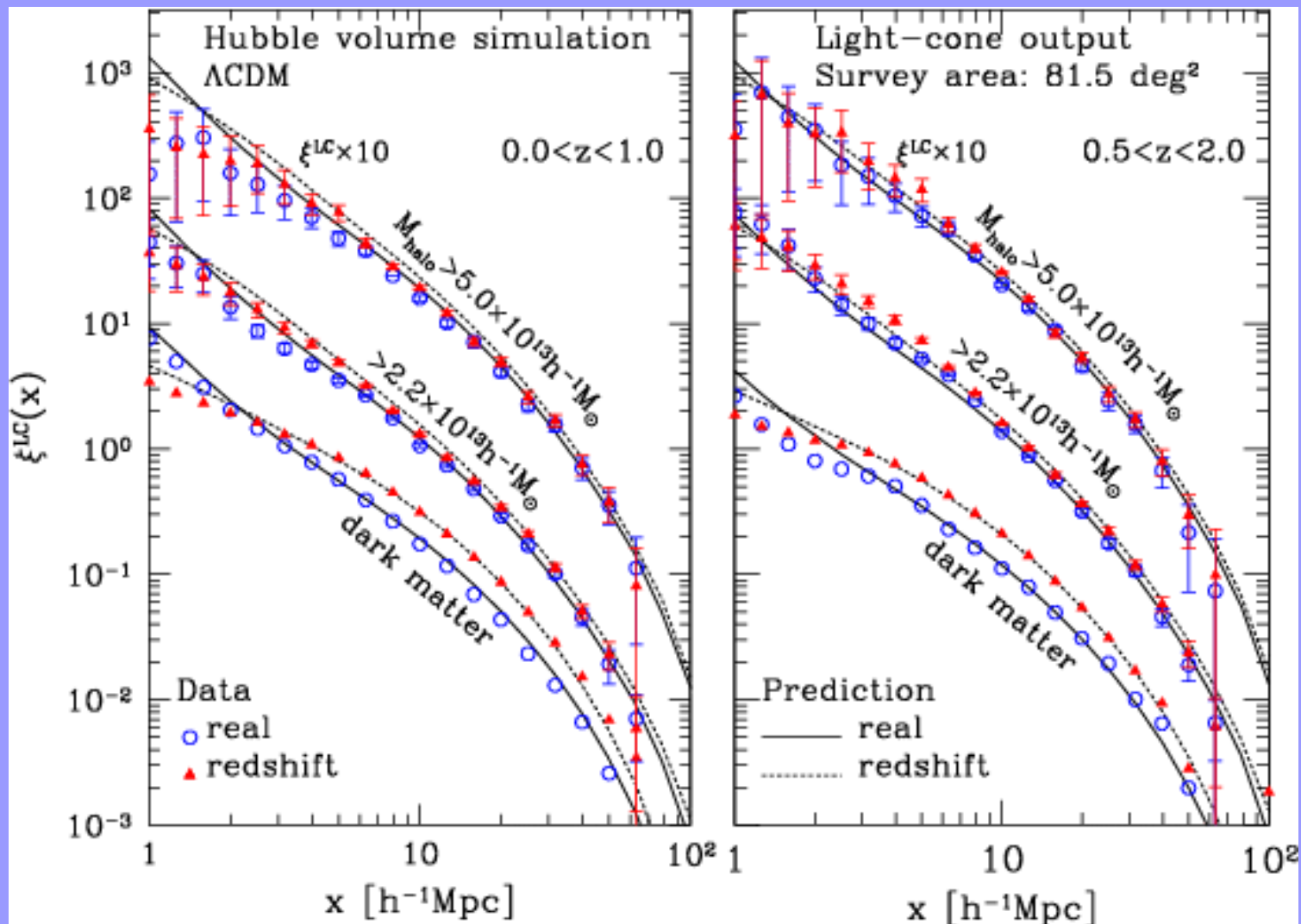
$$\xi_{halo}^{LC}(> M, r) = \frac{\int_{z_{min}}^{z_{max}} dz \int_M^{\infty} dM \xi_{halo}(M, R, z) n_{ST}^2(M, z) \frac{dV_c}{dz}}{\int_{z_{min}}^{z_{max}} dz \int_M^{\infty} dM n_{ST}^2(M, z) \frac{dV_c}{dz}}$$

Calibrating our halo biasing model with the Hubble volume simulation at $z=0$



- Our empirical model works quite well at $R > 20 h^{-1} \text{Mpc}$.
- The suppression of biasing in simulation at $R < 5 h^{-1} \text{Mpc}$ is ascribed to the exclusion effect of their finite size.
- For massive halos, our model underestimates the measured biasing by $< 10\%$ at $5 h^{-1} \text{Mpc} < R < 20 h^{-1} \text{Mpc}$, which would be less than other possible systematic errors.

Correlation functions of halos on the light-cone



Hamana, Yoshida, Suto & Evrard (2001)

In the last century, I would have concluded...

- We have developed an accurate empirical model which successfully describes the clustering of halos in the Hubble volume CDM simulation on the light-cone up to $z=3$.
- Since those dark halos are trivially related to the observed galaxy clusters, our model can be easily applied to the clustering of X-ray/SZ-selected clusters. ***Precision Cosmology !***

But...

From dark halos to galaxy clusters ?

- Definitely they are closely related, but the exact one-to-one correspondence is unlikely....

Abell (optical) clusters

the Abell radius

$$m_3 < m < m_3 + 2$$

richness class

Press-Schechter halos

spherical collapse

$$v_{\text{vir}} = 18^2$$

SZ clusters

$$I_{\text{SZ}} \\ n_e T_e$$

Halos in N-body simulations

friend-of-friend

linking length = 0.2

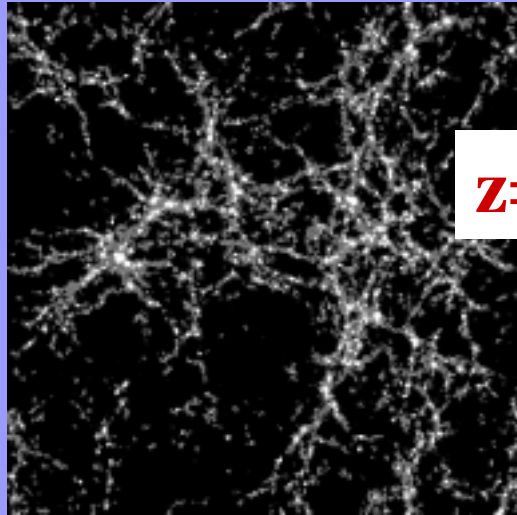
X-ray clusters

$$S_x \quad n_e^2 T_e^{1/2}$$

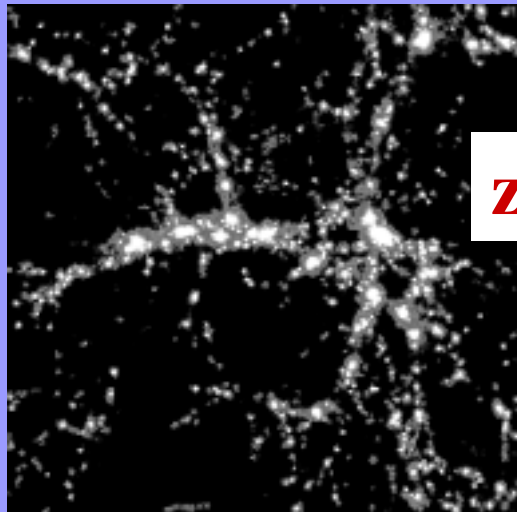
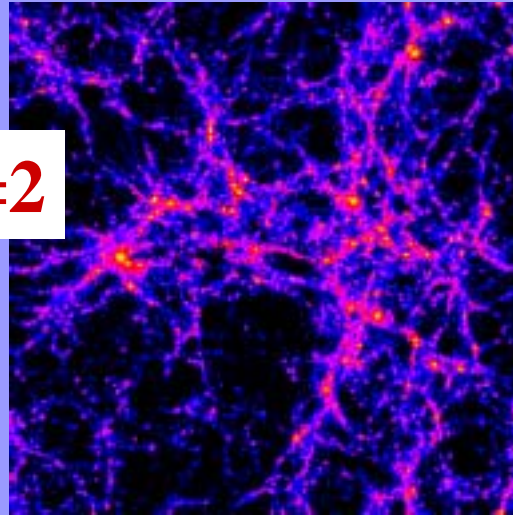
Relation between dark halos and clusters

Dark matter

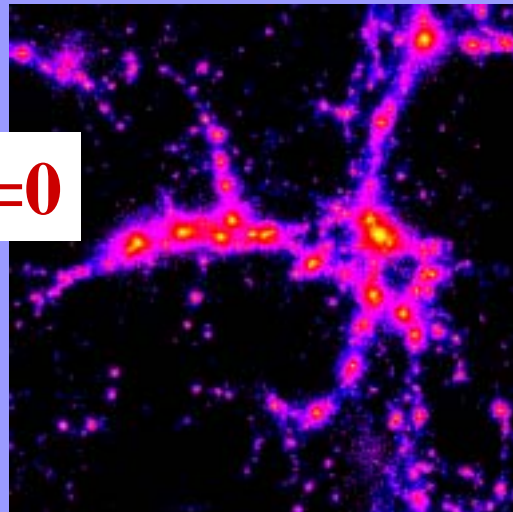
Hot gas



$z=2$



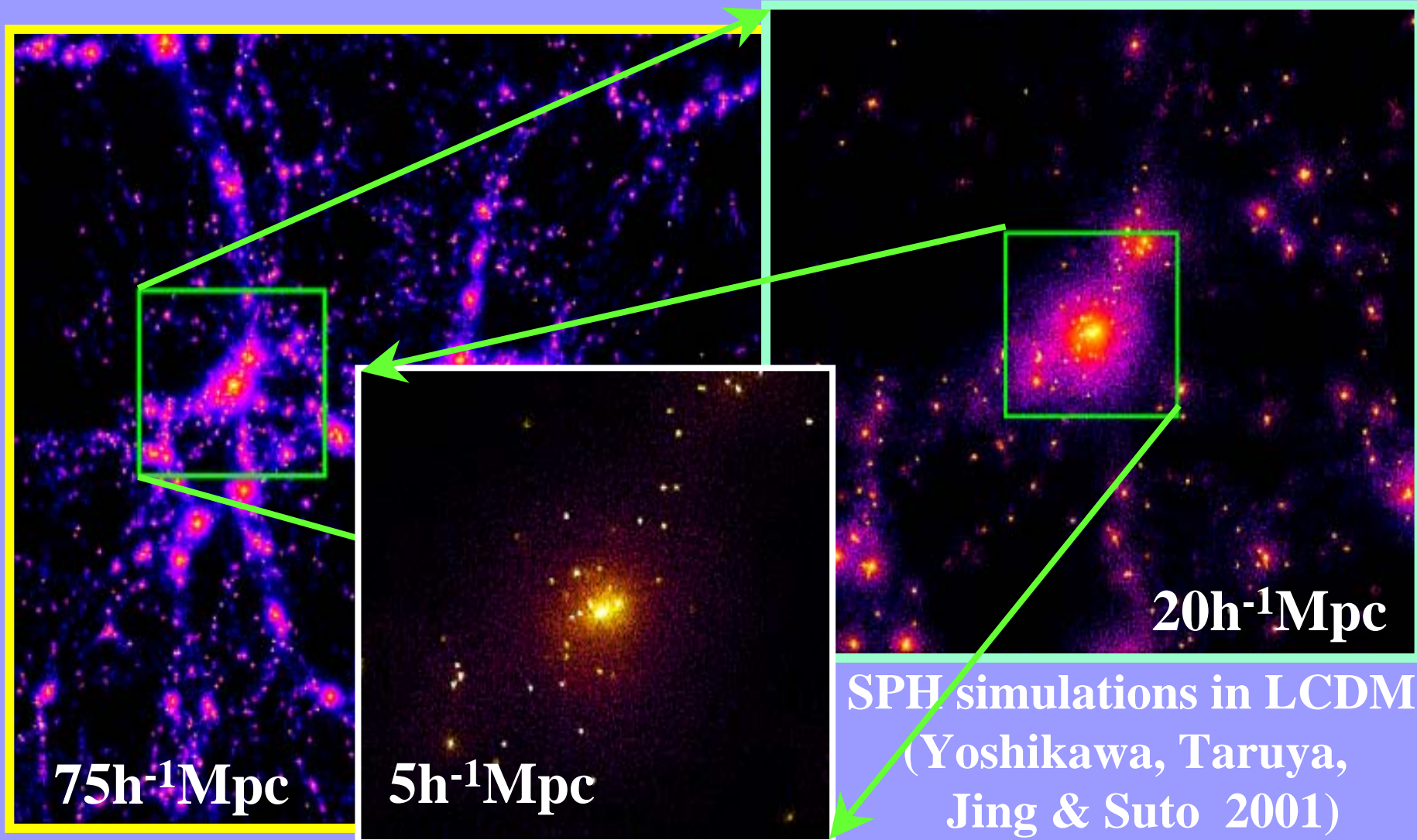
$z=0$



- Globally similar distribution, but their precise relation is unclear because definitions of clusters (especially at high z) are very ambiguous.

SPH simulations in LCDM:
 $75 \times 75 \times 15 \text{ h}^{-3} \text{Mpc}^3$
(Yoshikawa, Taruya,
Jing & Suto 2001)

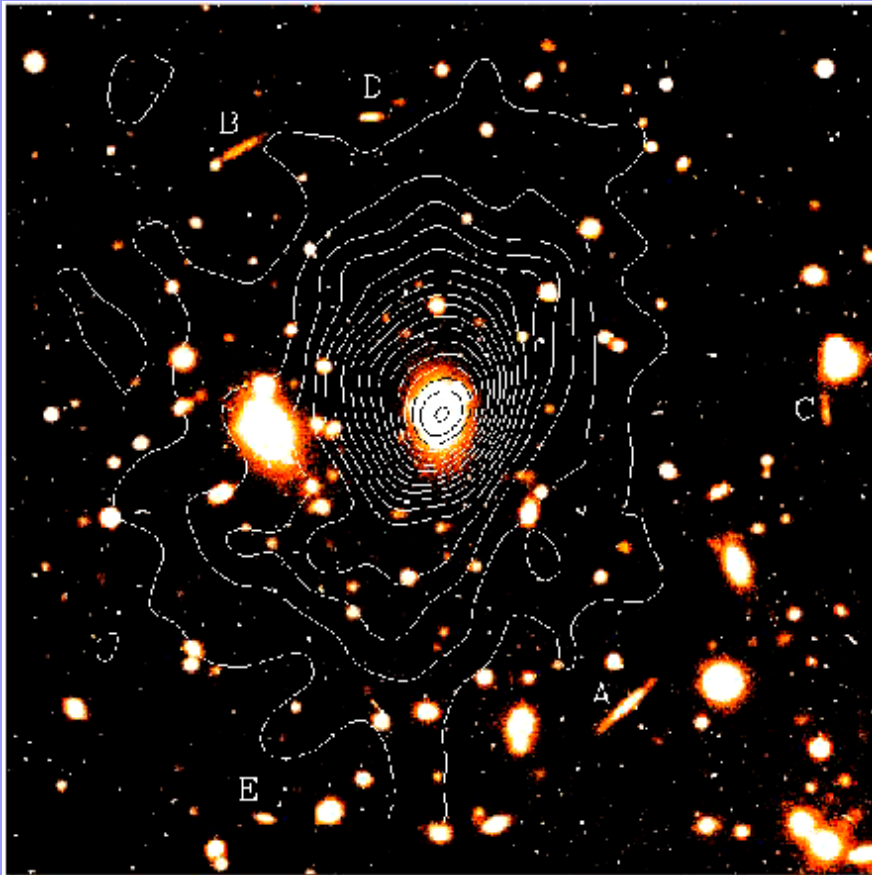
Zooming in the simulated structure



An example: multi-band observation of the most luminous X-ray cluster RXJ1347-1145

- What do clusters look like in different wavelengths ?
- Systematic observational campaign for RXJ1347-1145: the most luminous X-ray cluster at $z=0.45$
 - optical (ESO, NTT)
 - X-ray (ROSAT, ASCA)
 - submm SZ (SCUBA at J.C. Maxwell telescope, Hawaii)
 - mm SZ (NOBA at Nobeyama radio observatory, Japan)
- Collaborators: **E.Komatsu (小松英一郎)**, T.Kitayama, M.Hattori, H.Matsuo, R.Kawabe, H.Matsuo, K.Yoshikawa, K.Kohno, N.Kuno, S.Schindler

Optical and X-ray images of RXJ1347-1145



Optical: ESO NTT 3.5m I-band
X-ray: ROSAT/HRI

- the most luminous high-z X-ray cluster
- strong cooling flow

$$z = 0.45$$

$$L_X h_{50}^2 = 2 \times 10^{46} \text{ erg s}^{-1}$$

$$M (< 2h_{50}^{-1} \text{ Mpc}) = 10^{15} h_{50}^{-1} M_{\text{sun}}$$

$$T = 9.3 \text{ keV}$$

$$\theta_c = 8''.4 \left(57 h_{50}^{-1} \text{ kpc} \right)$$

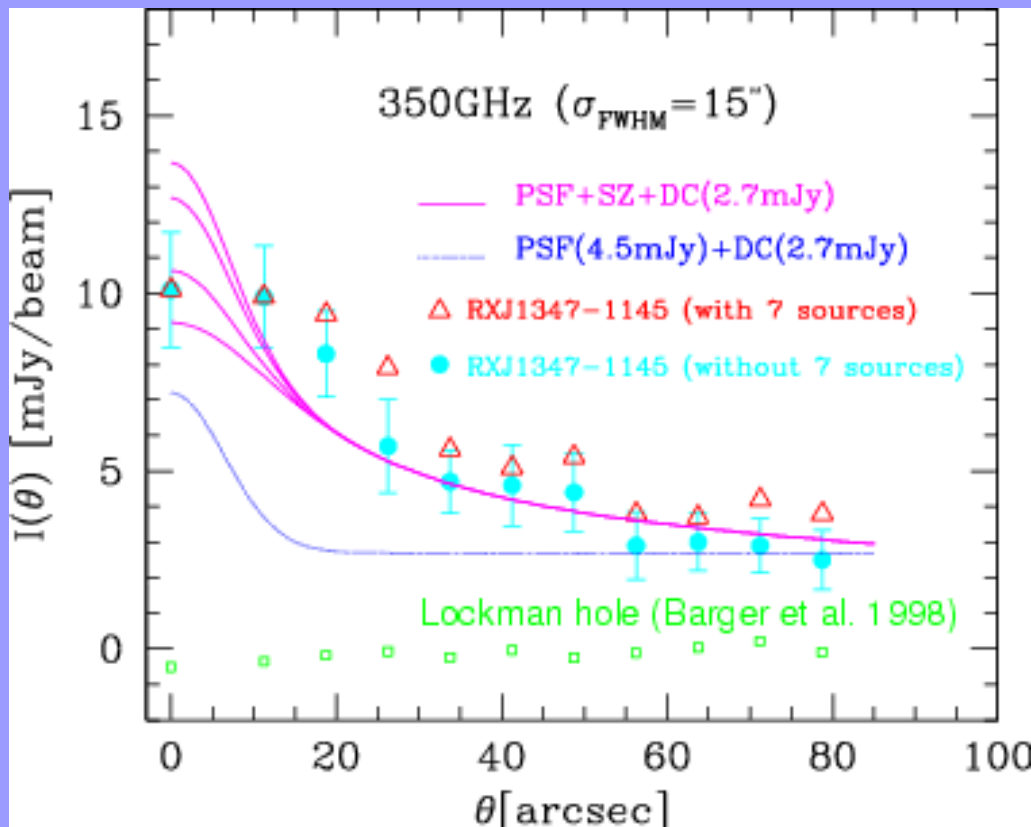
$$n_{e0} h_{50}^{-1/2} = 0.094 \text{ cm}^{-3}$$

$$\beta = 0.57 \quad \text{Schindler et al. (1997)}$$

$$T = 15.9_{-2.7}^{+6.5} \text{ keV} \quad \text{Ettori et al. (2001)}$$

Radial profile via submm SZ effect

- first detection of the radial profile of a cluster in the submm SZ effect at 350GHz (temperature increment)



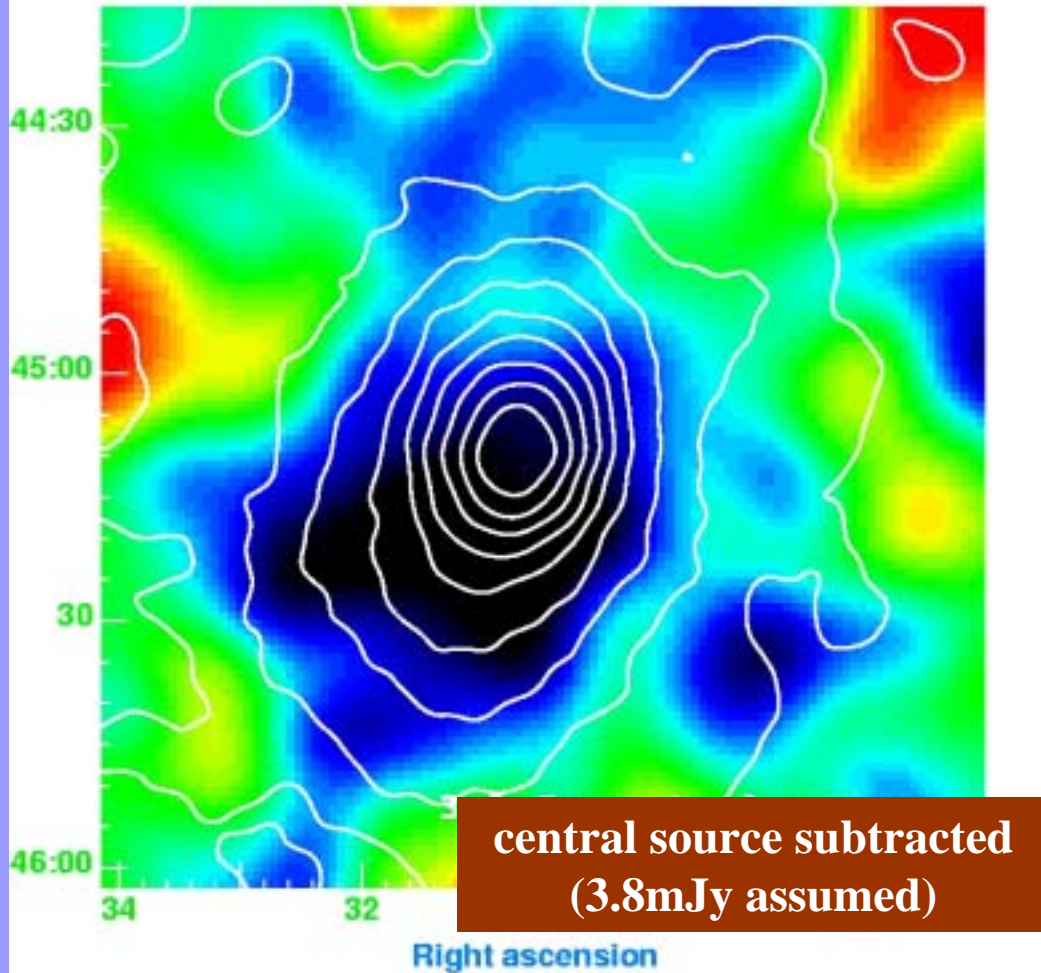
350GHz with SCUBA
at J.C.Maxwell telescope
on May 30, 31, 1998

central point source
with $\sim 3.5\text{mJy}$
+
extended SZ profile

Komatsu et al.
ApJ 516(1998)L1

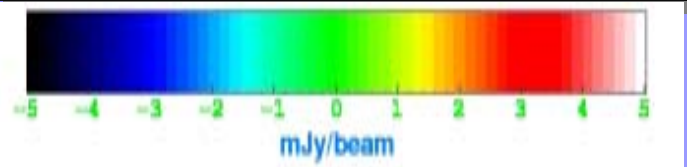
SZ map of RXJ1347-1145 at 150 GHz

(d) RX J1347-1145 / NOBA vs ROSAT



150GHz with NOBA
(Nobeyama Bolometer
Array) at Nobeyama
45m telescope
in March, April, 1999
and February 2000
FWHM=13''

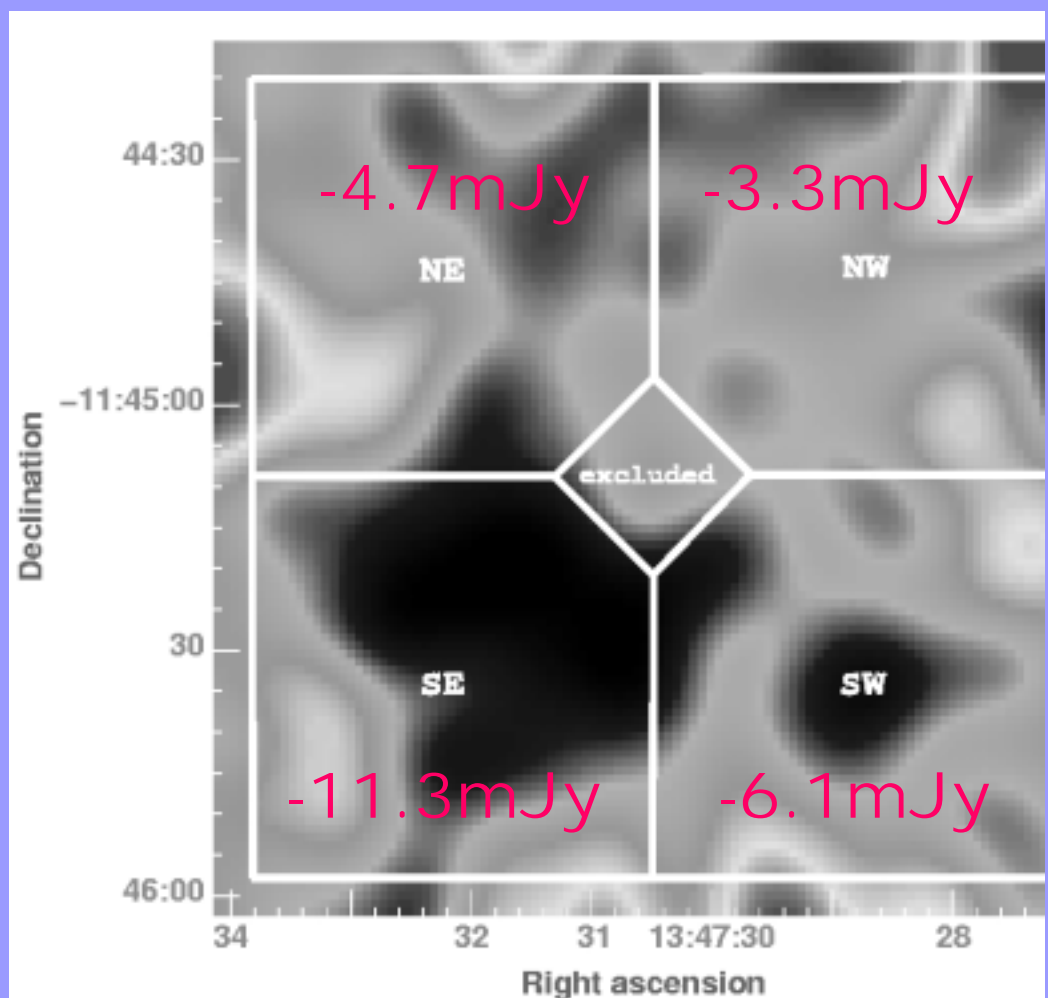
- Globally similar morphology to the X-ray image
- Substructure in the South-East direction



Substructure in the 150GHz SZ image

$$\sigma = 2.0 \text{ mJy}$$

RXJ1347@ 150GHz
Komatsu et al. (2001)



- divided in 4 regions

- mean observed flux: $-6.4 \pm 1.0 \text{ mJy}$

- predicted flux: -5.1 mJy (9.3 keV), -8.8 mJy (16.2 keV)

- large asymmetry/substructure

Confirmed by Chandra and BIMA observations

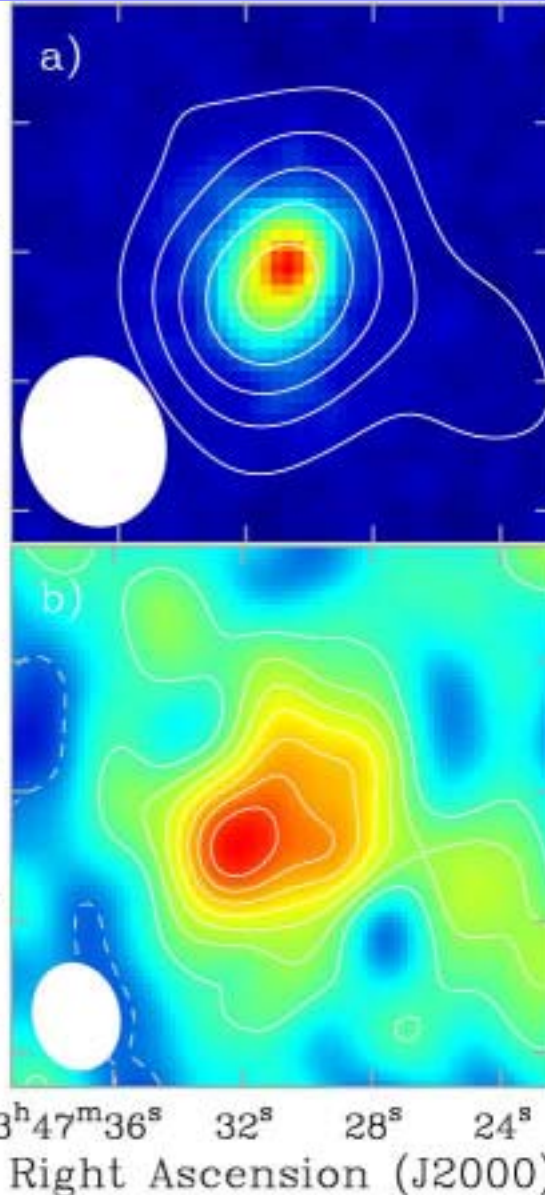
RXJ1347-1145

BIMA@30GHz
63" x 80" beam
(10.3mJy point source removed)

Carlstrom et al.
(2001)

BIMA@30GHz
40" x 50" beam
(10.3mJy point source removed)

- clusters look different in different bands and/or different z .
- spatial resolution is quite important.



Conclusions

- We have developed an accurate model for clustering of *dark matter halos* on the light-cone.
 - gravitational nonlinear evolution
 - redshift-space distortion
 - mass-, time-, and scale-dependent bias of halos
 - selection function
- The model can be applied to predicting the clustering of X-ray/SZ-selected clusters, *provided a good physical model for halo-cluster connection beyond the unrealistic one-to-one correspondence in the last century.*
- *The goal of the next generation cluster surveys is not precision cosmology (independent check/confirmation of the values of cosmological parameters is just boring), but is to understand `what are the clusters of galaxies`.*