

# Searching for an inner binary black-hole in a triple system



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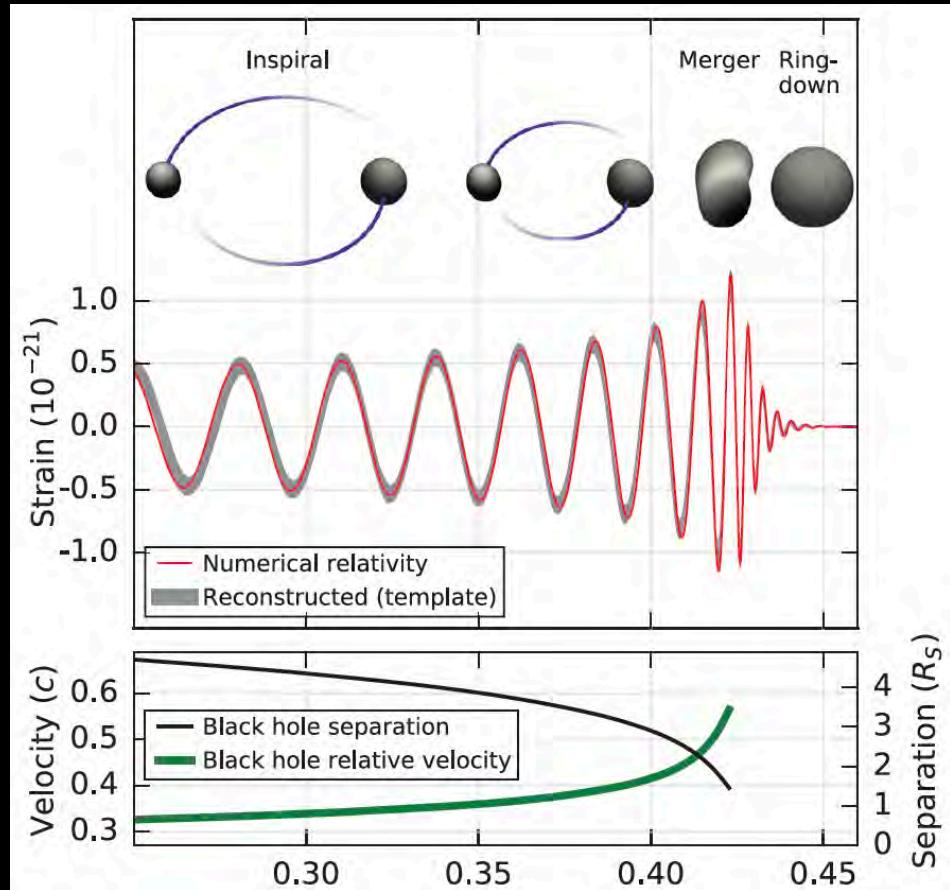
Colloquium at Physics Department, Kyoto University  
@16:00-17:30, October 29, 2020

*Alpha Centauri was a triple system,  
two suns tightly orbiting one  
another, and a third, more remote,  
circling them both.*

*What would it be like to live on a  
world with three suns in the sky?*

*— Carl Sagan, "Contact"*

# Binary black-holes in the universe

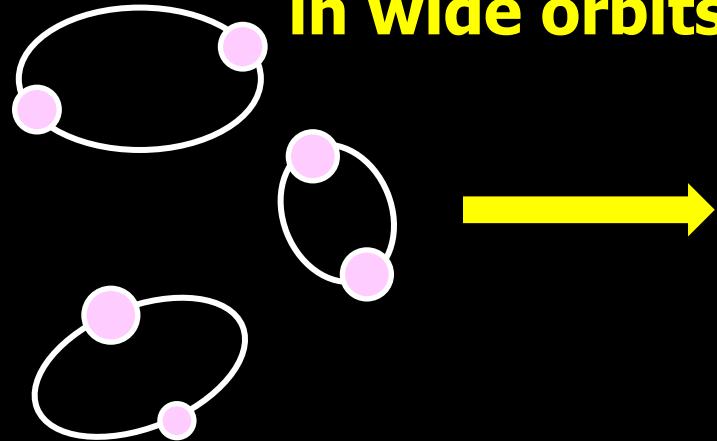


**First detection of BBHs  
via gravitational wave (GW)  
Abbot+(LIGO team) 2016**

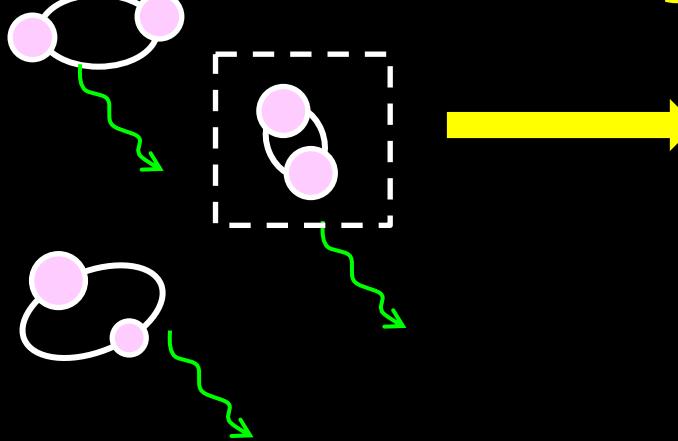
- **Origin of BBHs ?**
  - isolated binary  
(e.g., Kinugawa+ 2014)
  - dynamical capture  
(e.g., Rodriguez+ 2016)
  - primordial BHs  
(e.g., Sasaki+ 2016)
- **Where are their progenitors,  
probably with much longer  
orbital periods ?**

# Generic picture of binary BH evolution

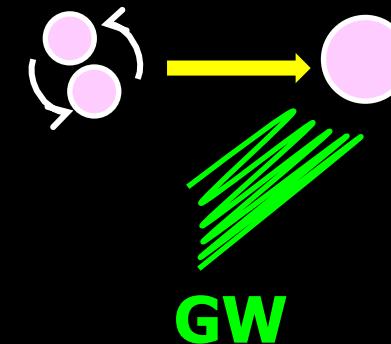
**binary black holes form  
in wide orbits**



**orbit shrinking**

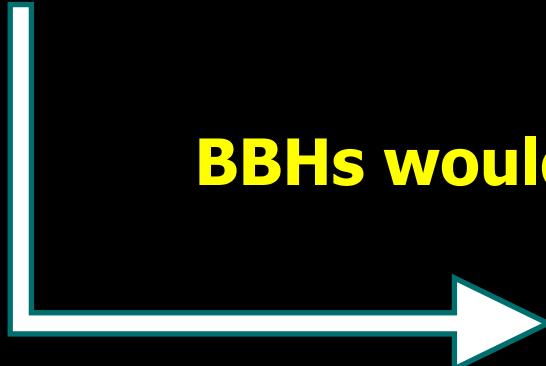


**merger**



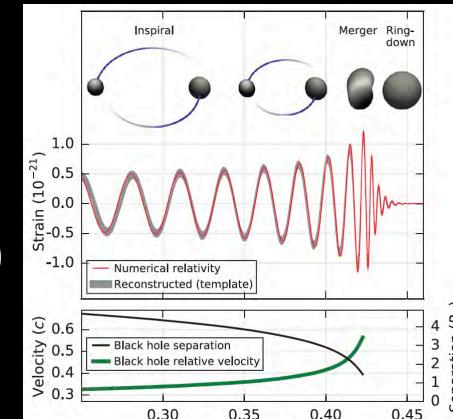
**weak GW(low-frequency)**

**BBHs would spend longer time in wide orbits before merging**



Abundant longer orbital-period BBHs may remain undetected (e.g.  $\sim 10$  day orbital period  $\sim 10^{-6}$  Hz).

**Detection strategy complementary to GW ?**

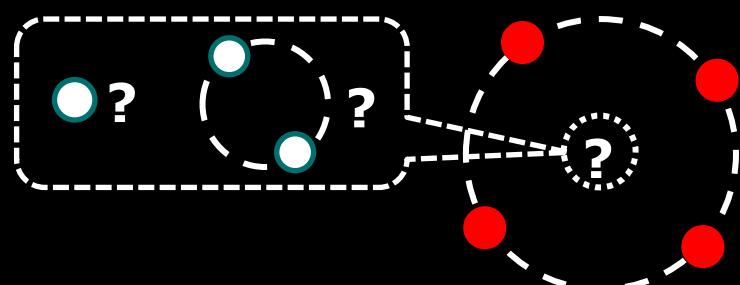


**LIGO/Virgo**

# Proposals to search for star-BH binaries

## Gaia mission (2013-)

Astrometry of stars in Galaxy  
~  $10^9$  stars eventually  
RV with 200-350m/s precision  
for brightest stars (Katz 2018)



## Yamaguchi+ (2018)

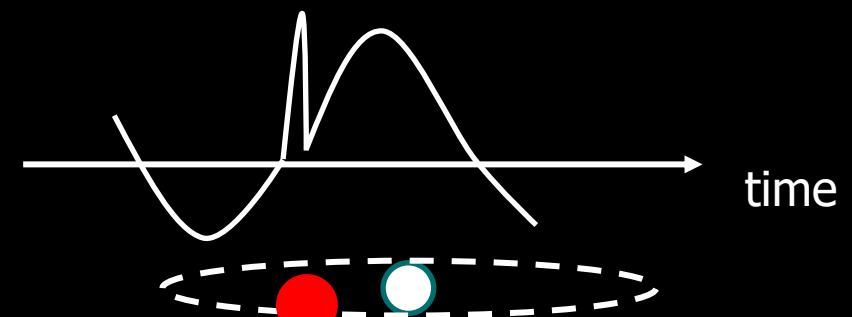
5-year mission may detect  
200-1000 star-BH binaries

## TESS mission (2018-)

photometry of nearby stars (~ 12mag)  
transit planets

## Masuda & Hotokezaka (2019)

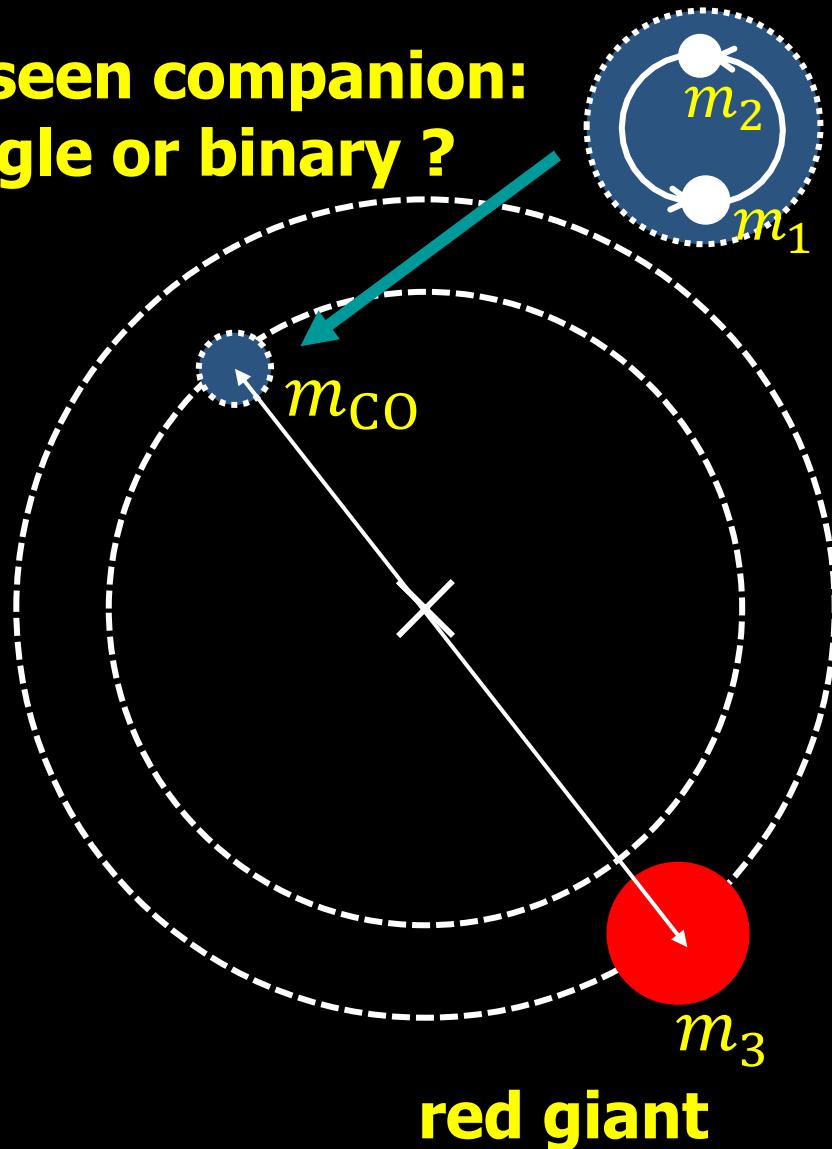
Light curve modulation  
(relativistic effects, tidal deformation)  
⇒ (10 – 100) star-BH binaries may be  
identified



**Some of them may be indeed a star-binary BH triple!  
Can precise radial velocity follow-up unveil the inner BBH?**

# A binary system 2M05215658+4359220

unseen companion:  
single or binary ?



Thompson+ (2019)

$P_{\text{out}}$	$83.205 \pm 0.064$ days
$m_{\text{co}} (= m_1 + m_2)$	$3.2^{+1.1}_{-0.4} M_{\odot}$
$m_3$	$3.0^{+0.6}_{-0.5} M_{\odot}$
$e_{\text{out}}$	$0.0048 \pm 0.0026$

highly circular !

- red giant + unseen companion binary ?
  - Detected by a low-resolution radial velocity change
  - The companion mass is  $3.2 M_{\odot}$   
⇒ a single BH or a NS binary ?

# Ups and downs of LB-1

Article

**A wide star–black-hole binary system from radial-velocity measurements**

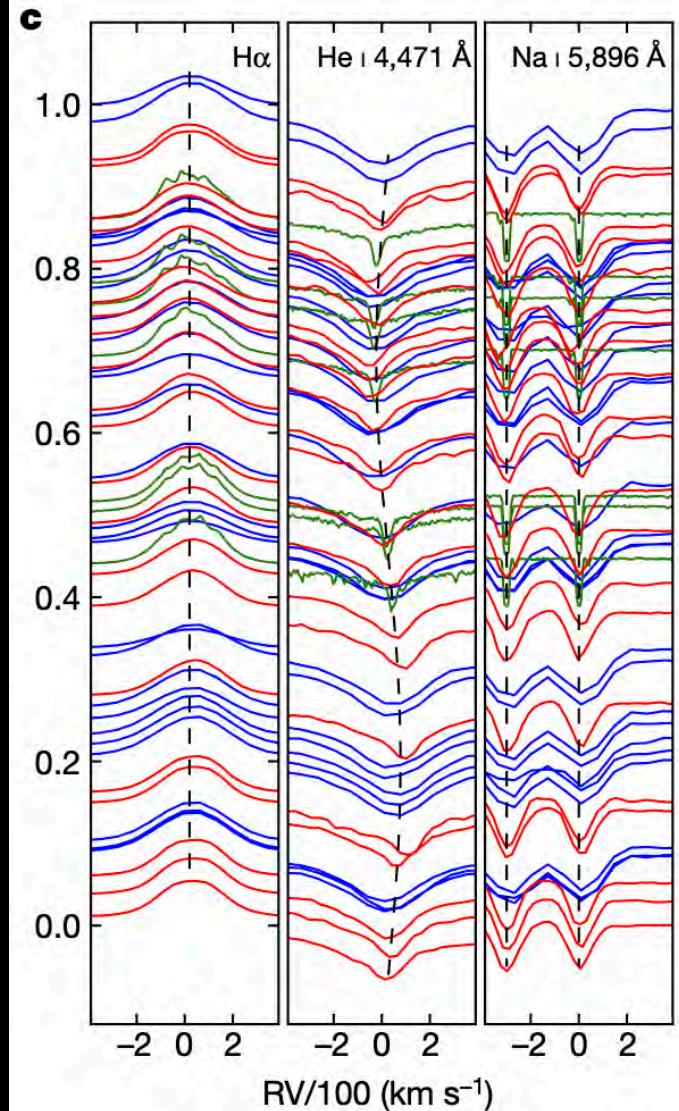
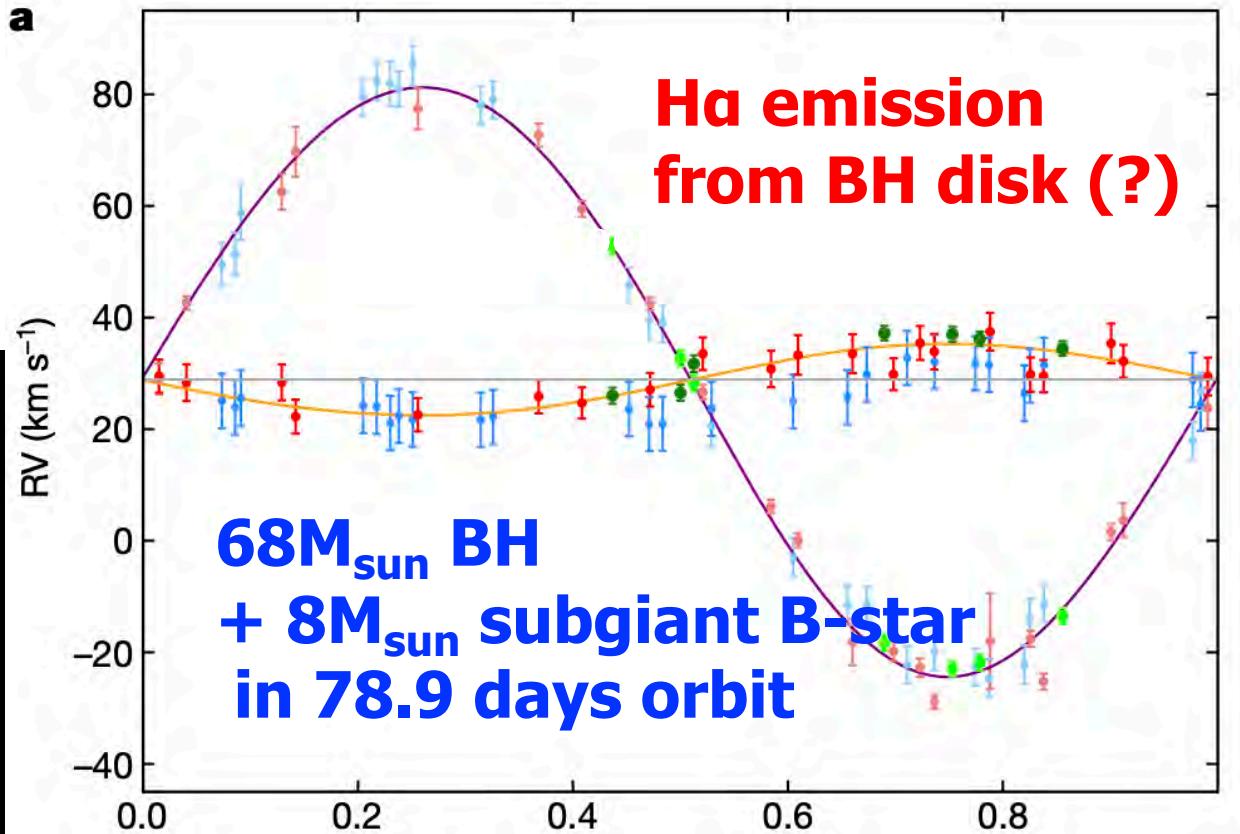
Liu et al. **Nature 575(2019)618**

<https://doi.org/10.1038/s41586-019-1766-2>

Received: 1 March 2019

Accepted: 28 August 2019

Published online: 27 November 2019



# On the signature of a 70-solar-mass black hole in LB-1

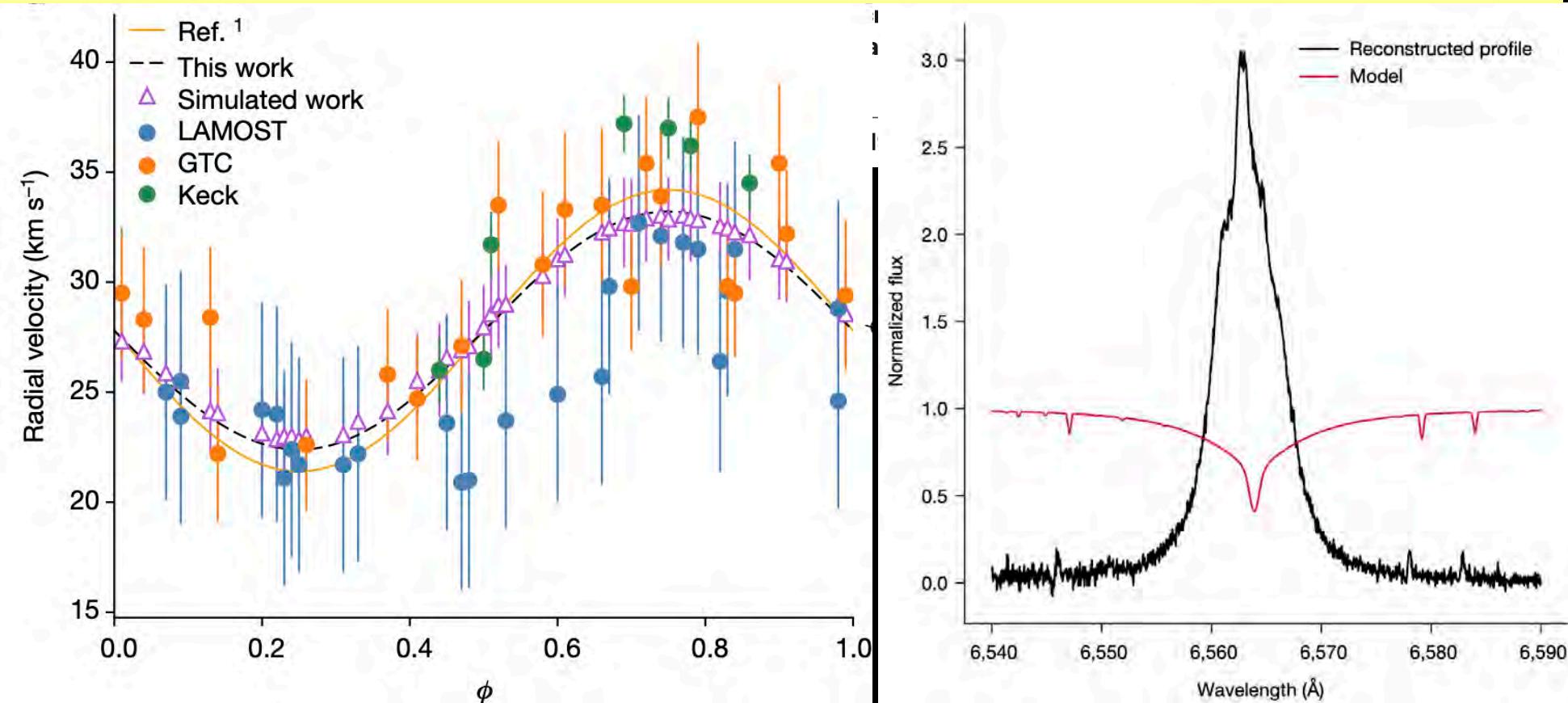
Abdul-Masih et al. Nature 580(2020) E11

Ha emission is not from BH disk, but a static Ha + B-star absorption  
The unseen companion should be much less massive ( $< 10M_{\text{sun}}$ )

Received: 6 December 2019

Accepted: 27 February 2020

Published online: 29 April 2020



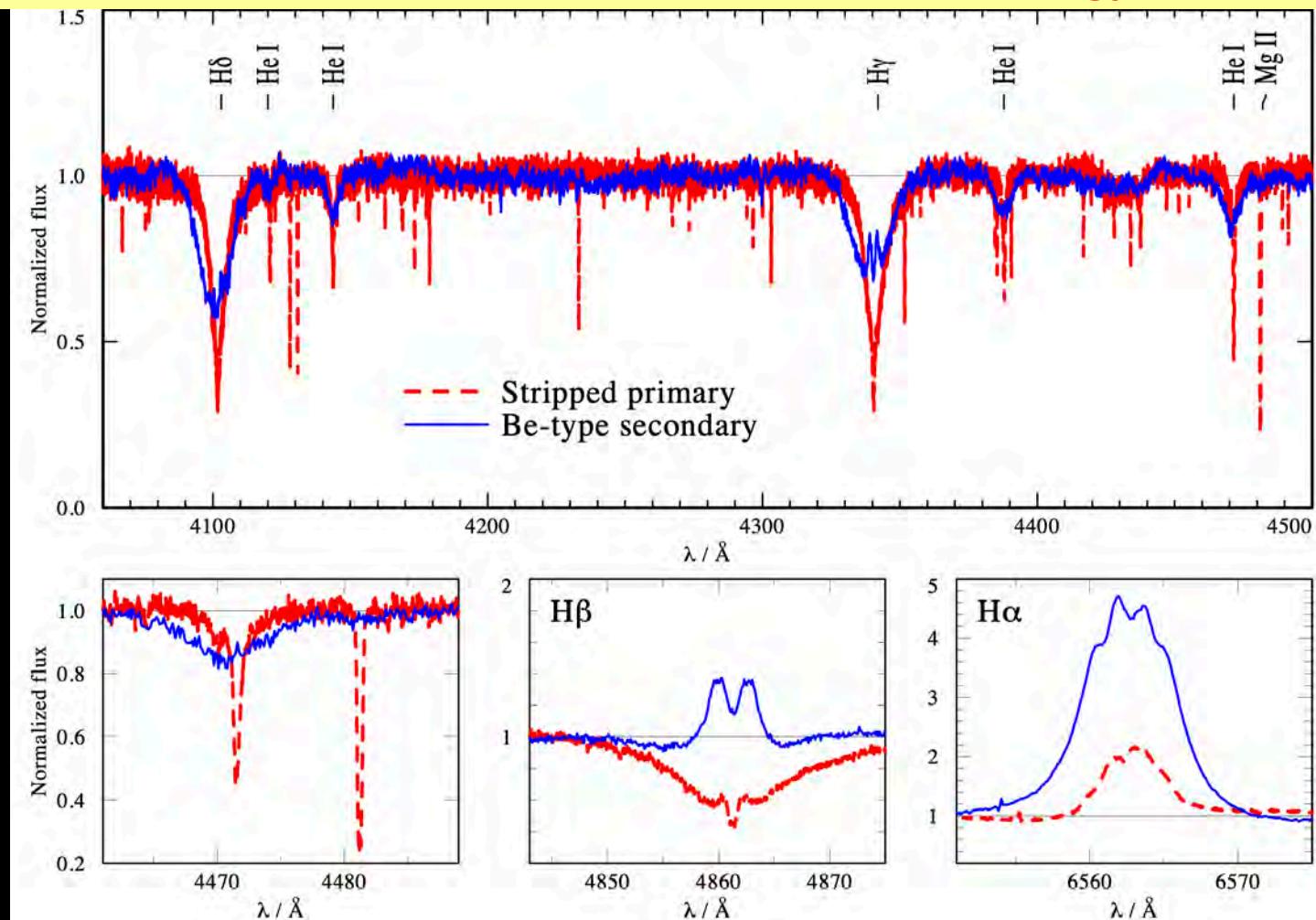
# The hidden companion in LB-1 unveiled by spectral disentangling

T. Shenar, J. Bodensteiner, M. Abdul-Masih, M. Fabry, L. Mahy, P. Marchant,

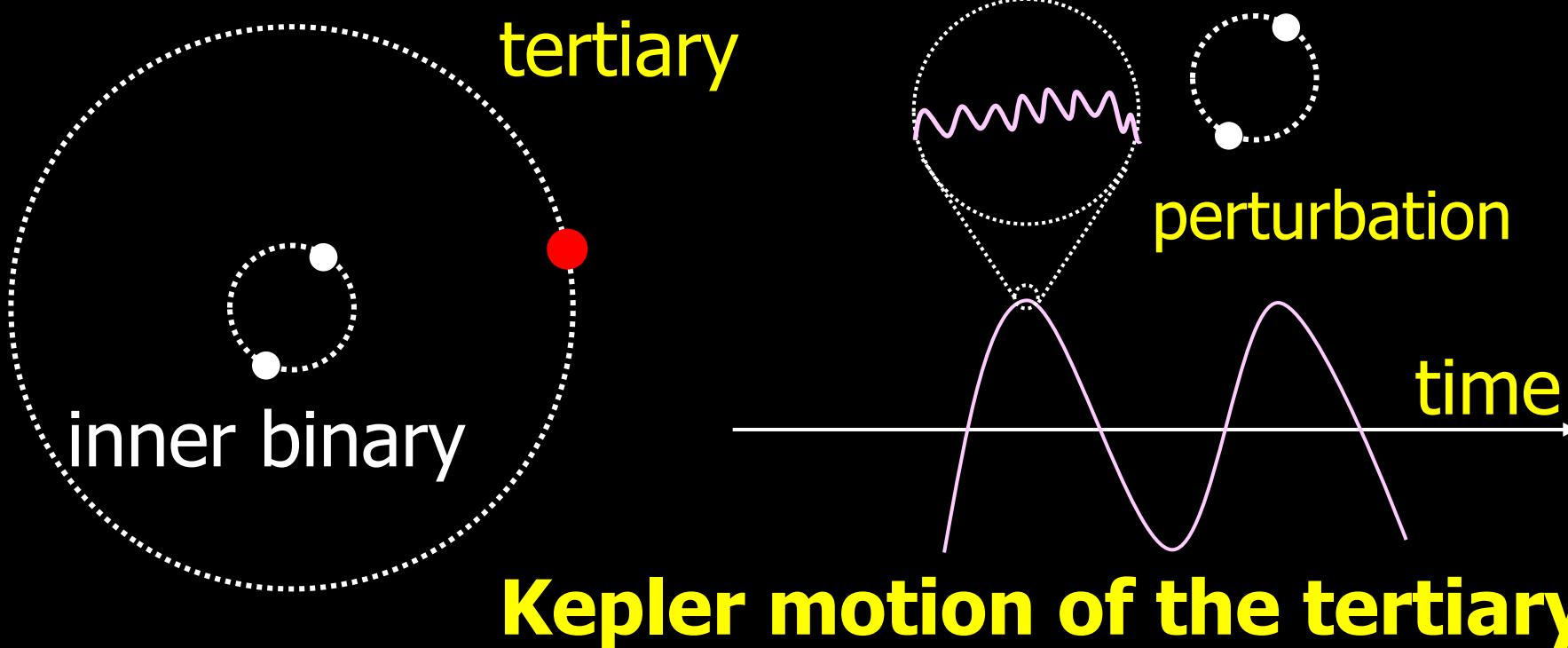
**Disentangled the spectra of LB-1 and found that LB-1 comprises a stripped He-rich star ( $1.5 \pm 0.4 M_{\text{sun}}$ ) + a Be-type secondary star ( $7 \pm 2 M_{\text{sun}}$ ) , not a BH**

T. Shenar et al.  
A&A 639(2020)L6

**LB-1 turned out to  
be not a star-BH  
system that we  
have been looking  
for, but such  
candidates will  
come in future !**



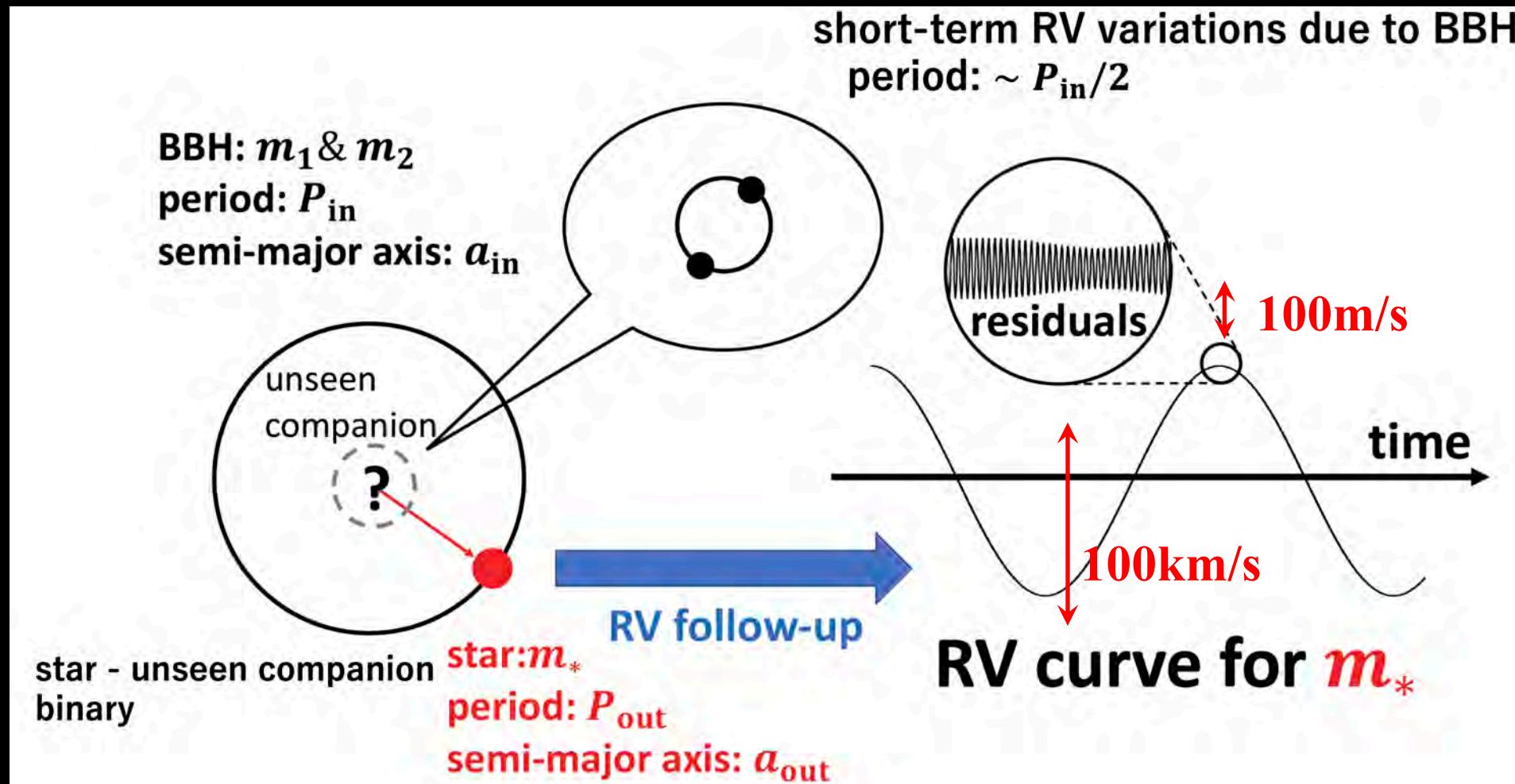
# Radial velocity modulation of a tertiary star due to an inner binary



Toshinori Hayashi  
林利憲

Hayashi, Wang + YS: ApJ 890(2020)112  
Hayashi + YS: ApJ 897(2020)29

# Triple=black hole binary + outer tertiary star

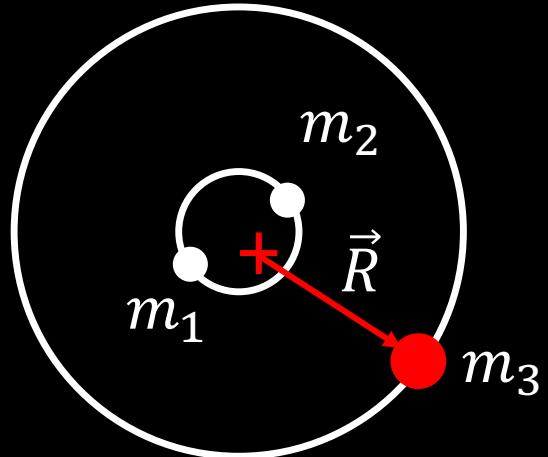


Coplanar systems:

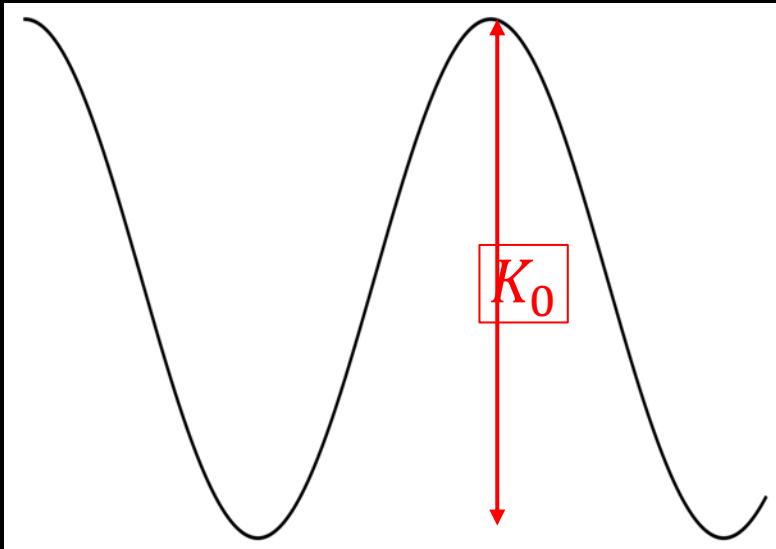
Hayashi, Wang & YS 2020, ApJ 890, 112

Non-coplanar systems: Hayashi & YS 2020, ApJ, 897, 29

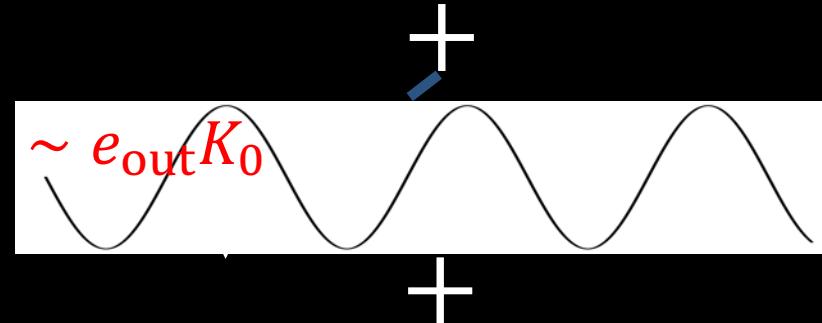
# RV modulations for coplanar triples



RV =

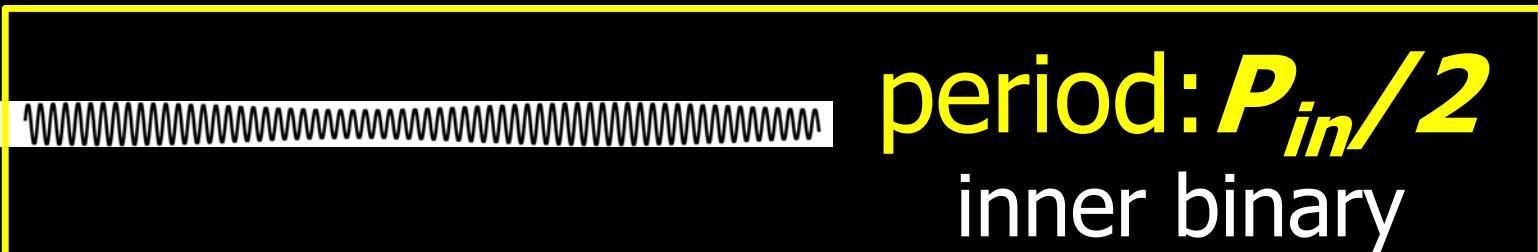


period:  **$P_{out}$**



period:  **$P_{out}/2$**   
first order in  $e_{out}$

$$\left( \sqrt{\frac{m_1}{m_2}} + \sqrt{\frac{m_2}{m_1}} \right)^{-2} \left( \frac{a_{in}}{a_{out}} \right)^{3.5} K_0$$



period:  **$P_{in}/2$**   
inner binary

# Approximate expressions for RV of the tertiary star

$$V_{\text{RV}}(t) = V_{\text{Kep}}^{(0)}(t) + \delta V_{\text{Kep}}(t) + V_{\text{bin}}(t).$$

Morais & Correia (2008)  
Hayashi & YS (2020)

$$\begin{aligned}\nu_{-3} &\equiv 2\nu_{\text{in}} - 3\nu_{\text{out}}, \\ \nu_{-1} &\equiv 2\nu_{\text{in}} - \nu_{\text{out}}.\end{aligned}$$

## (i) Unperturbed Kepler motion

$$V_{\text{Kep}}^{(0)}(t) = K_0 \sin I_{\text{out}} \cos[\nu_{\text{out}} t + f_{\text{out},0} + \omega_{\text{out}}]$$

$$K_0 \equiv \frac{m_1 + m_2}{m_1 + m_2 + m_*} a_{\text{out}} \nu_{\text{out}},$$

## (ii) Perturbation to the Kepler motion

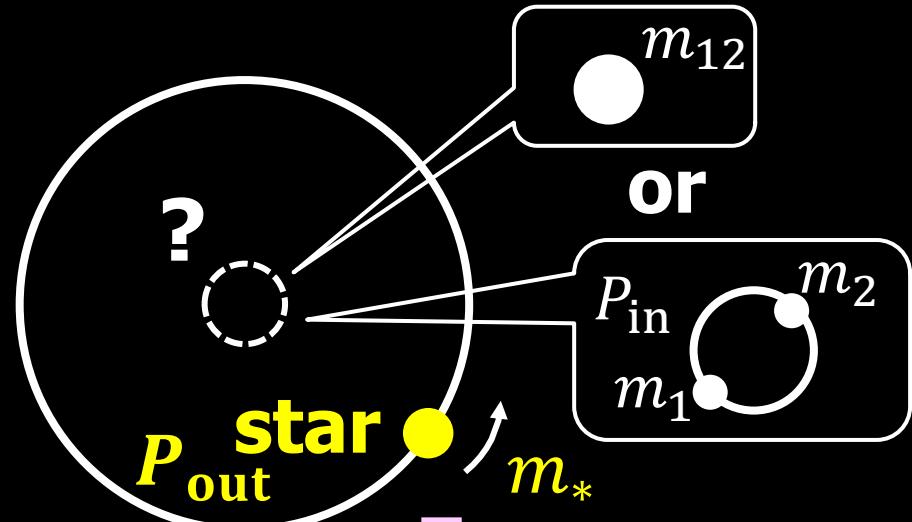
$$\delta V_{\text{Kep}}(t) = K_1 \sin I_{\text{out}} \cos[\nu_{\text{out}} t + f_{\text{out},0} + \omega_{\text{out}}]$$

$$K_1 \equiv \frac{3}{4} K_0 \left( \frac{a_{\text{in}}}{a_{\text{out}}} \right)^2 \frac{m_1 m_2}{(m_1 + m_2)^2}.$$

## (iii) Modulation by the inner binary

$$\begin{aligned}V_{\text{bin}}(t) &= -\frac{15}{16} K_{\text{bin}} \sin I_{\text{out}} \cos[(2\nu_{\text{in}} - 3\nu_{\text{out}})t \\ &\quad + 2(f_{\text{in},0} + \omega_{\text{in}}) - 3(f_{\text{out},0} + \omega_{\text{out}})] \\ &\quad + \frac{3}{16} K_{\text{bin}} \sin I_{\text{out}} \cos[(2\nu_{\text{in}} - \nu_{\text{out}})t \\ &\quad + 2(f_{\text{in},0} + \omega_{\text{in}}) - (f_{\text{out},0} + \omega_{\text{out}})], \\ K_{\text{bin}} &\equiv \frac{m_1 m_2}{(m_1 + m_2)^2} \sqrt{\frac{m_1 + m_2 + m_*}{m_1 + m_2}} \left( \frac{a_{\text{in}}}{a_{\text{out}}} \right)^{7/2} K_0,\end{aligned}$$

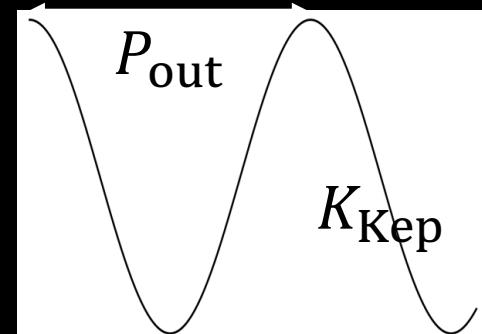
# RV modulations for non-coplanar triples



↓  
high-precision RV follow-up

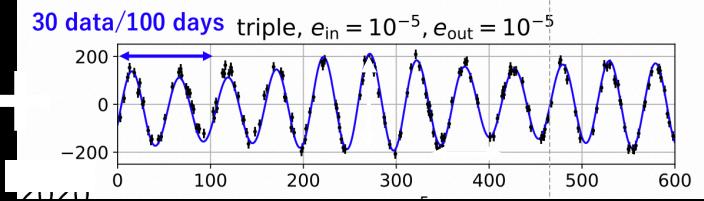
Keplerian motion RV  
+ RV variations by inner binary

## (i) Coplanar triple



Kepler motion + Short-term RV variations  
(inner-binary perturbation)

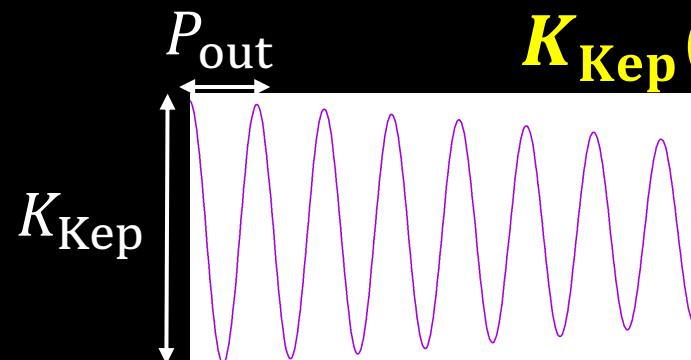
$$\text{Amp} \sim K_{\text{Kep}} \left( \frac{P_{\text{in}}}{P_{\text{out}}} \right)^{\frac{7}{3}}$$



$$\text{Period} \sim P_{\text{in}}/2$$

## (ii) Non-coplanar triple

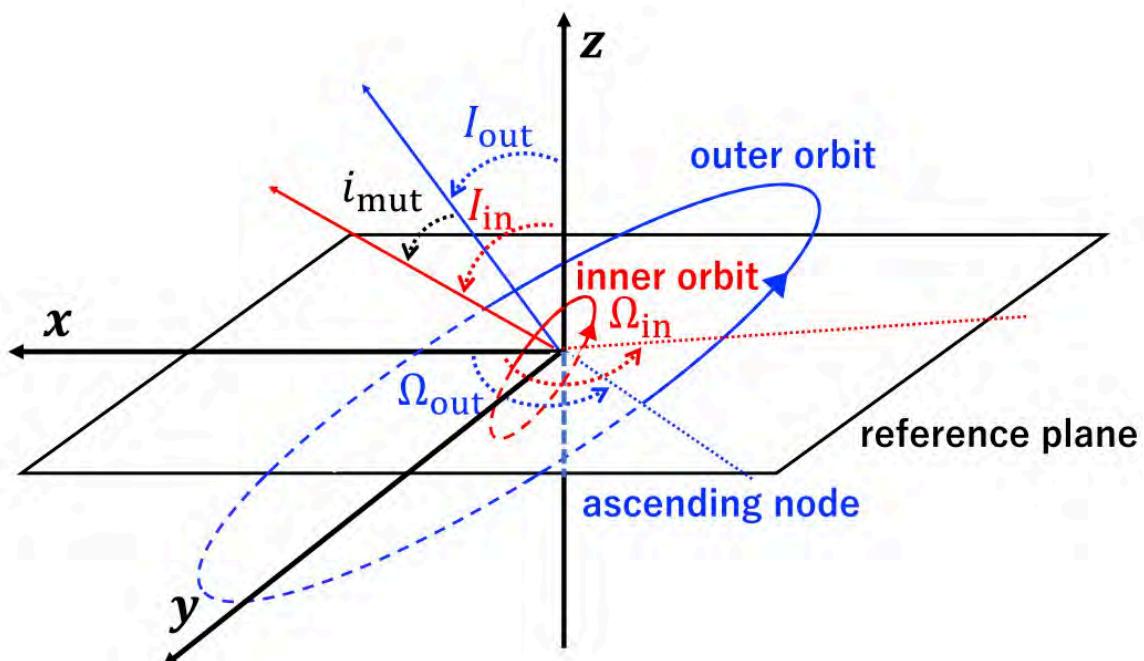
Inclination  $I_{\text{out}}(t)$  modulated in the Kozai-Lidov timescale



$$K_{\text{Kep}}(t) = K_0 \sin I_{\text{out}}(t)$$

Amplitude of Kepler RV  
varies with the timescale

# Parameters for simulated triple systems



$P_{\text{out}} = 78.9 \text{ days}$

$P_{\text{in}} = 10 \text{ days}$

equal-mass binary  $10M_{\odot} + 10M_{\odot}$

unequal-mass binary  $2M_{\odot} + 18M_{\odot}$

Hayashi & YS 2020, ApJ, 897, 29

Model	$I_{\text{out}}$ (deg)	$I_{\text{in}}$ (deg)	$i_{\text{mut}}$ (deg)	$m_1 (M_{\odot})$	$m_2 (M_{\odot})$	$e_{\text{in}}$
P1010	90	90	0	10	10	$10^{-5}$
PE1010	90	90	0	10	10	0.2
R1010	90	270	180	10	10	$10^{-5}$
O1010	0	90	90	10	10	$10^{-5}$
I1010	0	45	45	10	10	$10^{-5}$
<hr/>						
P0218	90	90	0	18	2	$10^{-5}$
PE0218	90	90	0	18	2	0.2
R0218	90	270	180	18	2	$10^{-5}$
O0218	0	90	90	18	2	$10^{-5}$
I0218	0	45	45	18	2	$10^{-5}$

Note. P, PE, R, O, and I indicate prograde, prograde eccentric, retrograde, orthogonal, and inclined orbits.

# Coplanar circular triples

Prograde  
equal-mass

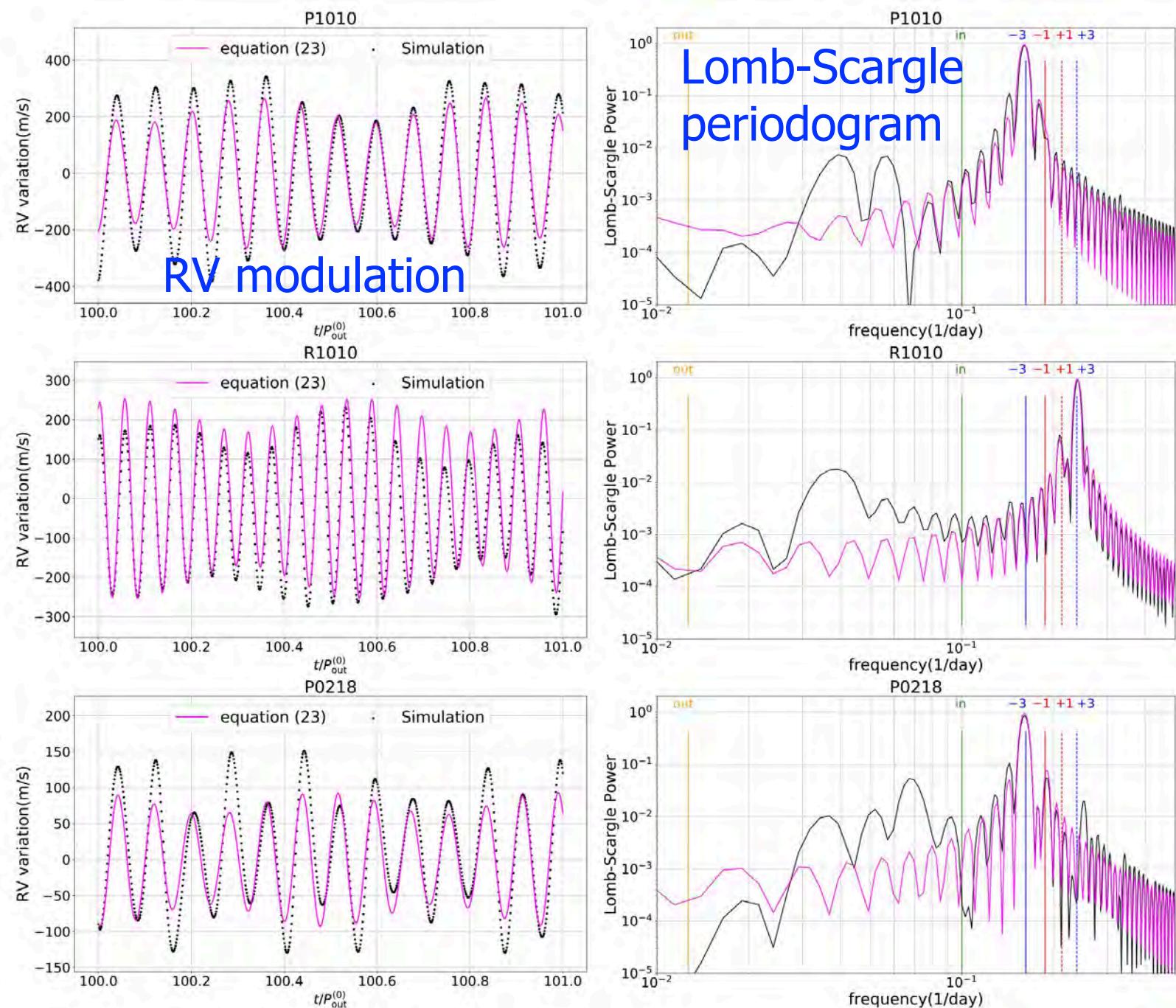
Simulation against  
Perturbative model  
(Morais & Correia 2008, 2012)

Retrograde  
equal-mass

$$\nu_{-3} \equiv 2\nu_{\text{in}} - 3\nu_{\text{out}},$$

$$\nu_{-1} \equiv 2\nu_{\text{in}} - \nu_{\text{out}}.$$

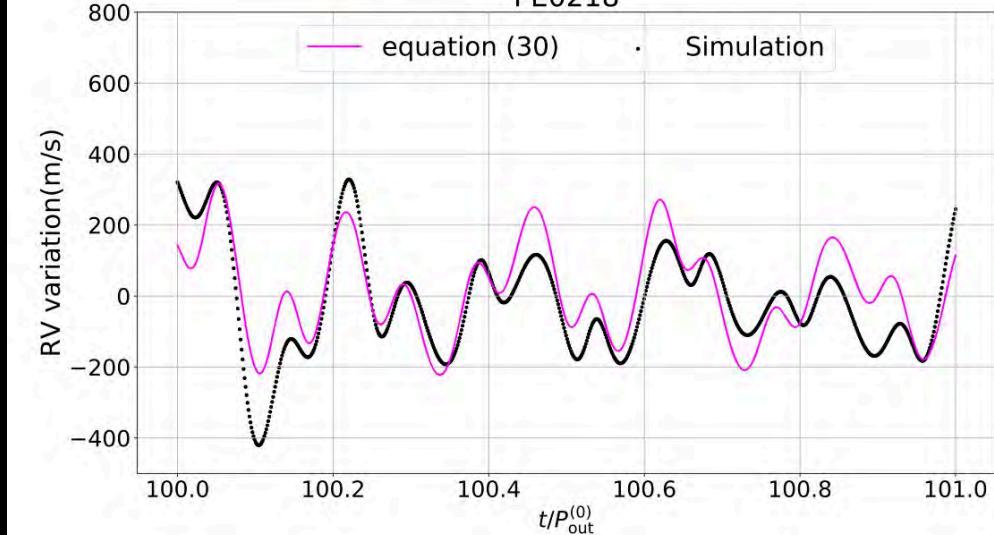
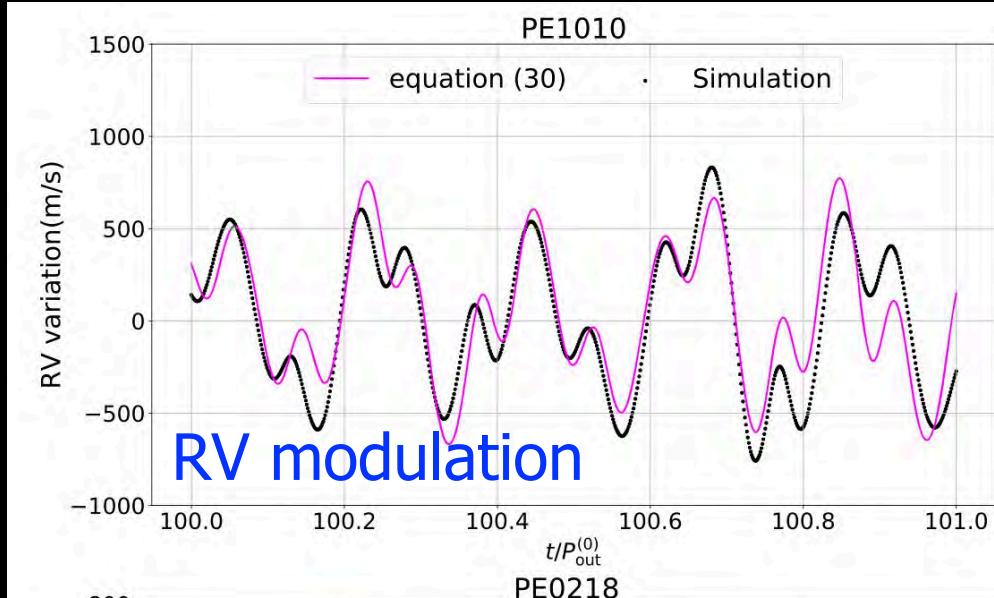
Prograde  
unequal-mass



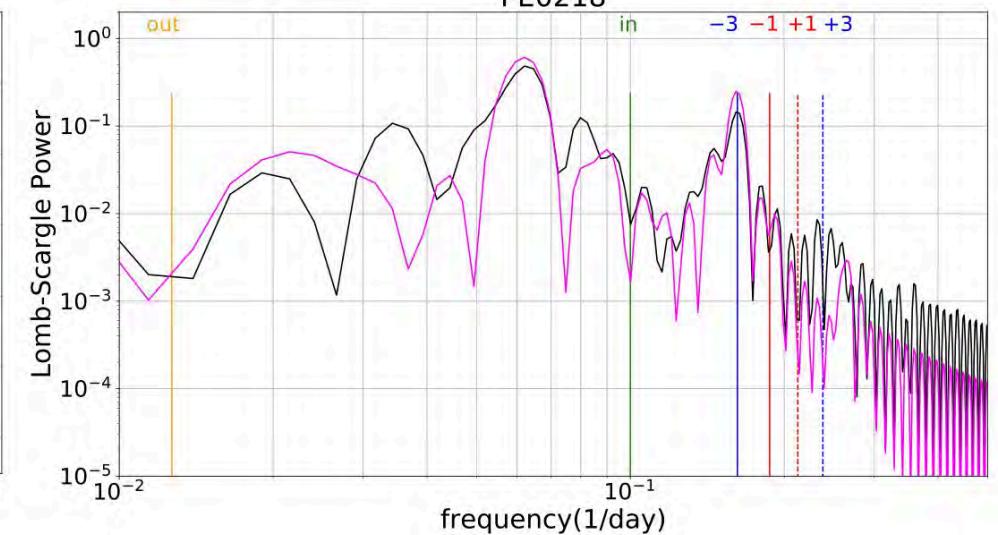
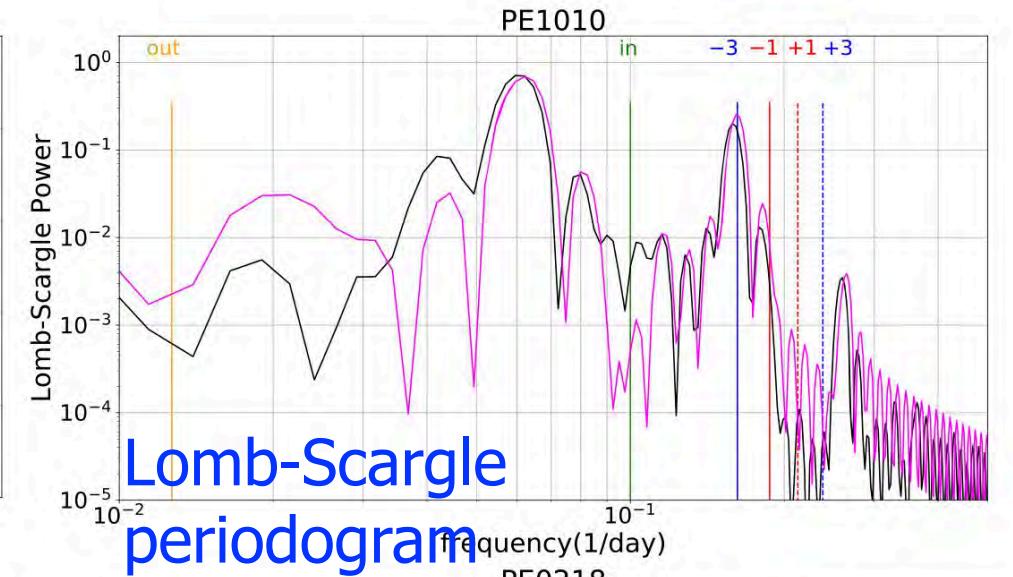
# Coplanar eccentric triples

Simulation against Perturbative model (Morais & Correia 2008, 2012)

Prograde  
equal-mass



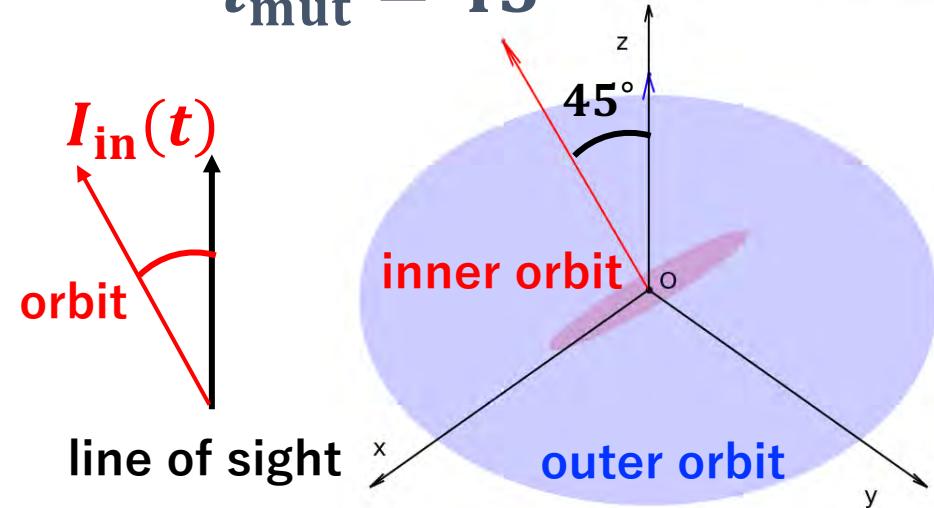
Prograde  
unequal-mass



# Evolution of inclination for non-coplanar triples

$$i_{\text{mut}} = 45^\circ$$

$$t = 0P_{\text{out}}^{(0)}$$



$$P_{\text{out}} = 78.9 \text{ days}$$

$$P_{\text{in}} = 10 \text{ days}$$

$$m_1 = m_2 = 10M_\odot$$

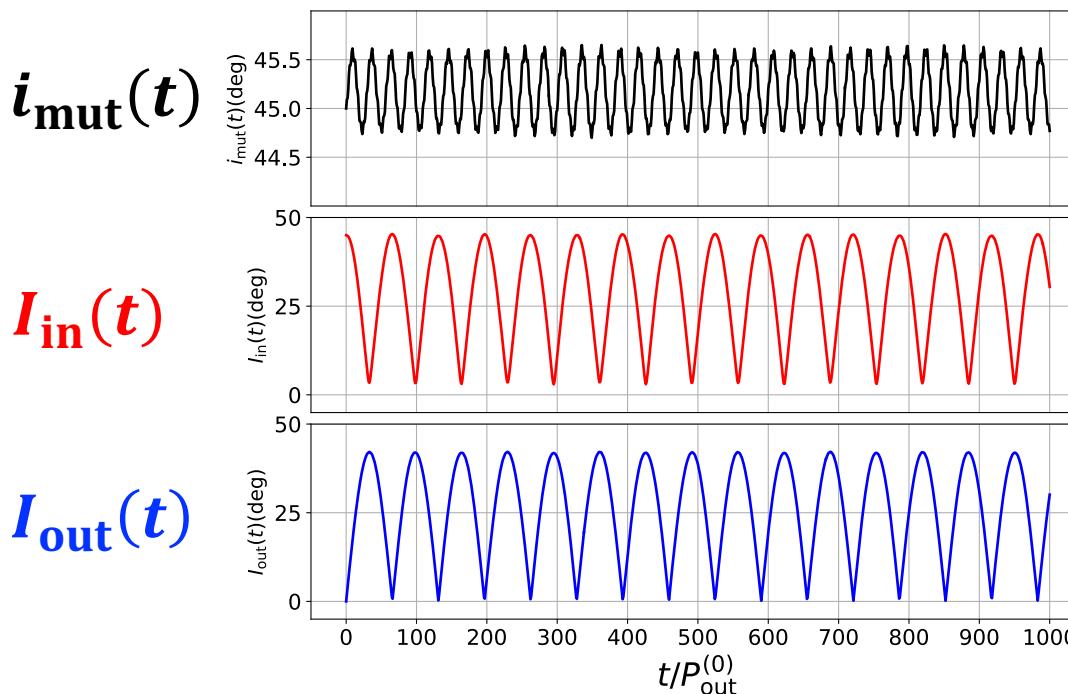
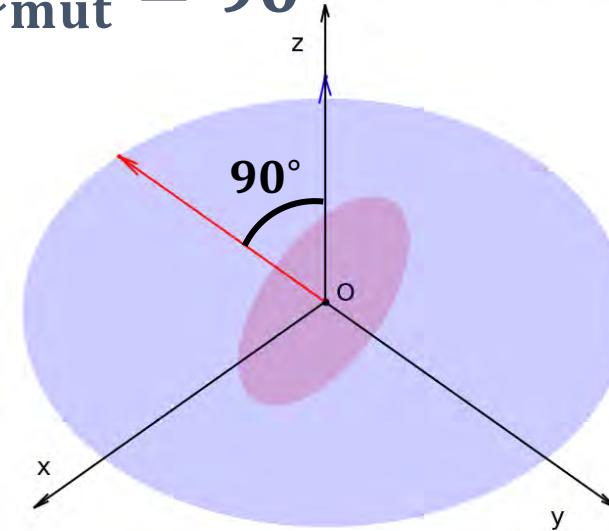
$$m_* = 3M_\odot$$

$$e_{\text{out}} = 0.03$$

$$e_{\text{in}} = 10^{-5}$$

$$i_{\text{mut}} = 90^\circ$$

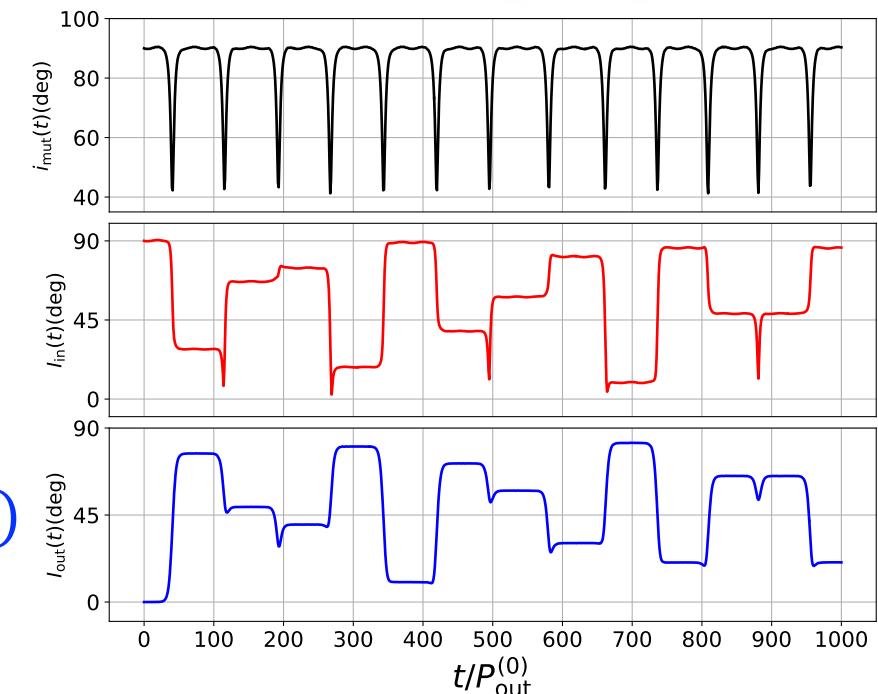
$$t = 0P_{\text{out}}^{(0)}$$



$$i_{\text{mut}}(t)$$

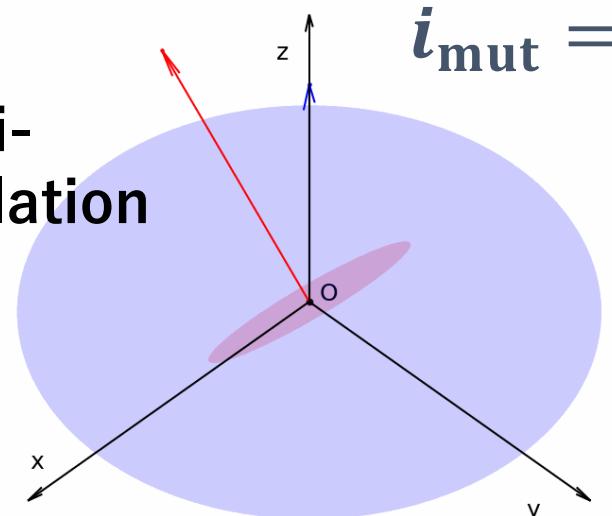
$$I_{\text{in}}(t)$$

$$I_{\text{out}}(t)$$

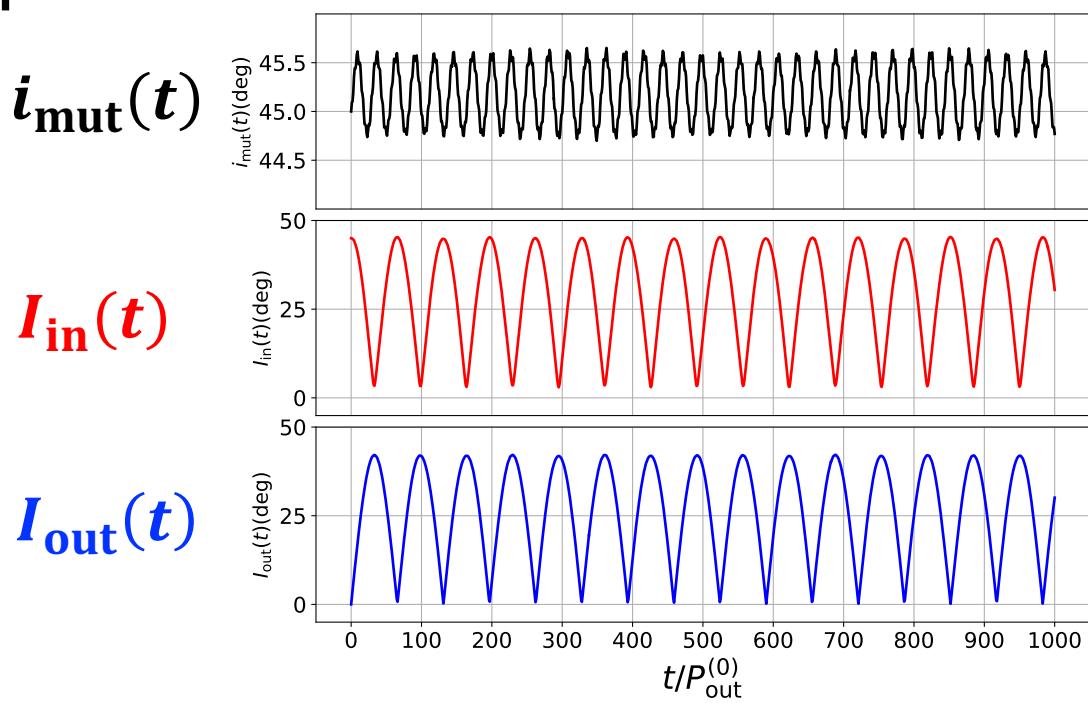


# Evolution of inclination for non-coplanar triples

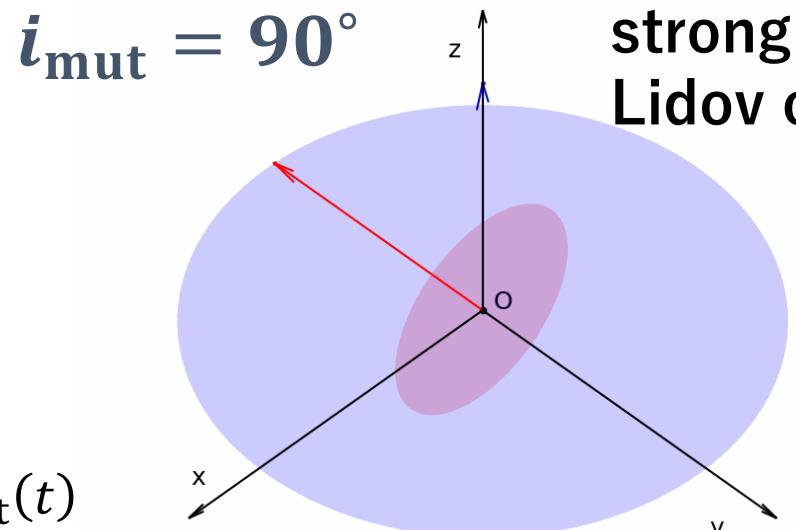
$t = 0P_{\text{out}}^{(0)}$



weak Kozai-Lidov oscillation  
⇒ small-amplitude regular precession

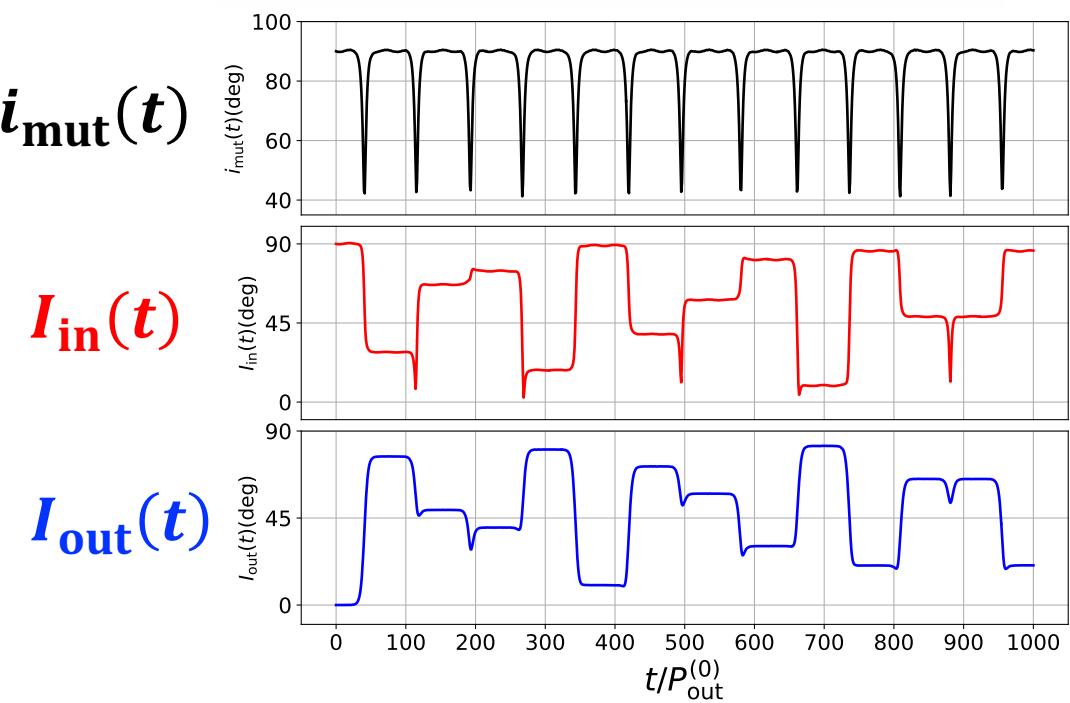


$t = 0P_{\text{out}}^{(0)}$

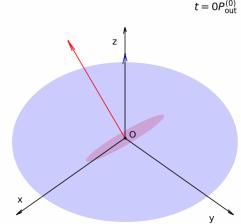


$i_{\text{mut}} = 90^\circ$   
strong Kozai-Lidov oscillation

$\Rightarrow$  large-amplitude sporadic precession

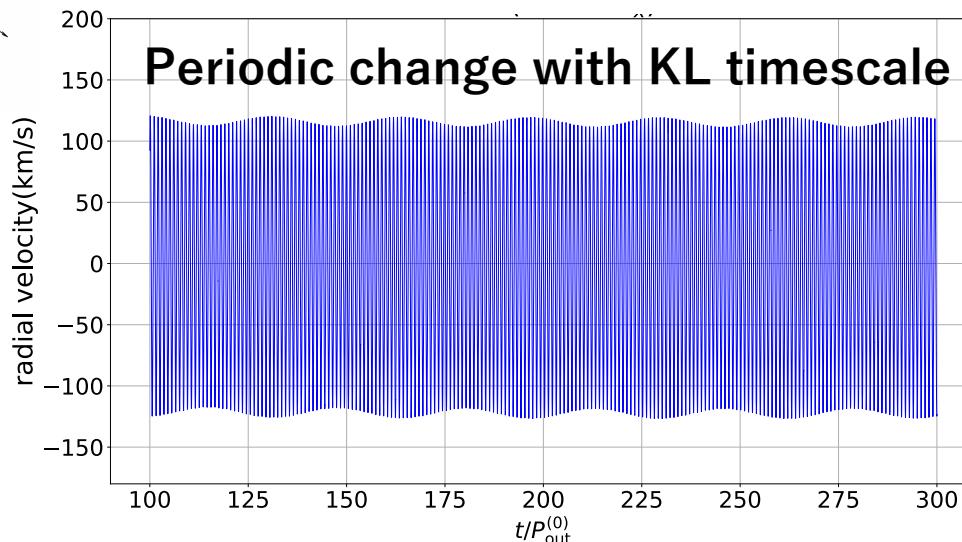


# Evolution of radial velocity for non-coplanar triples

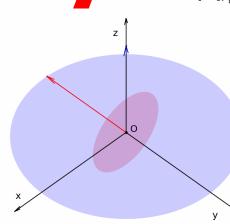
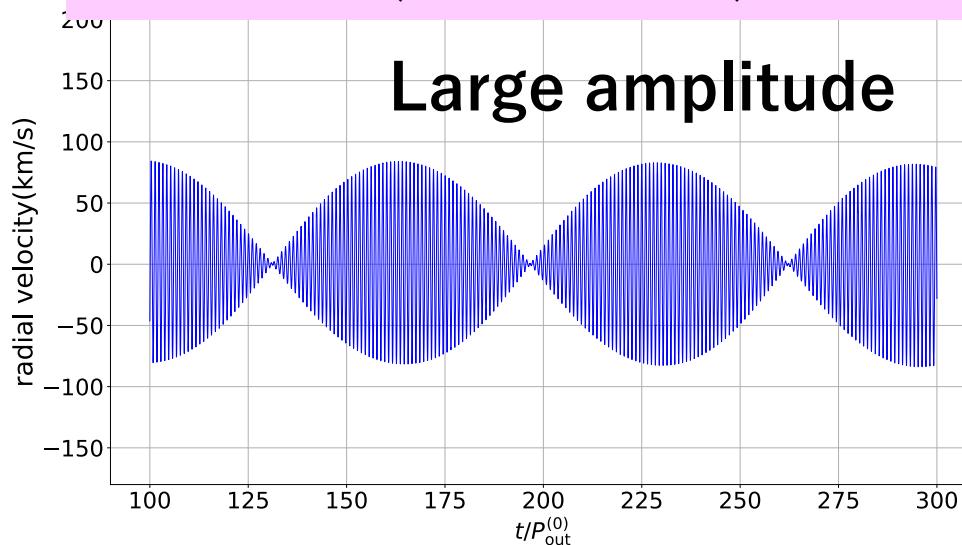


$$i_{\text{mut}} = 45^\circ \quad K_{\text{Kep}} = K_0 \sin I_{\text{out}}(t)$$

x-direction (near edge-on) total RV

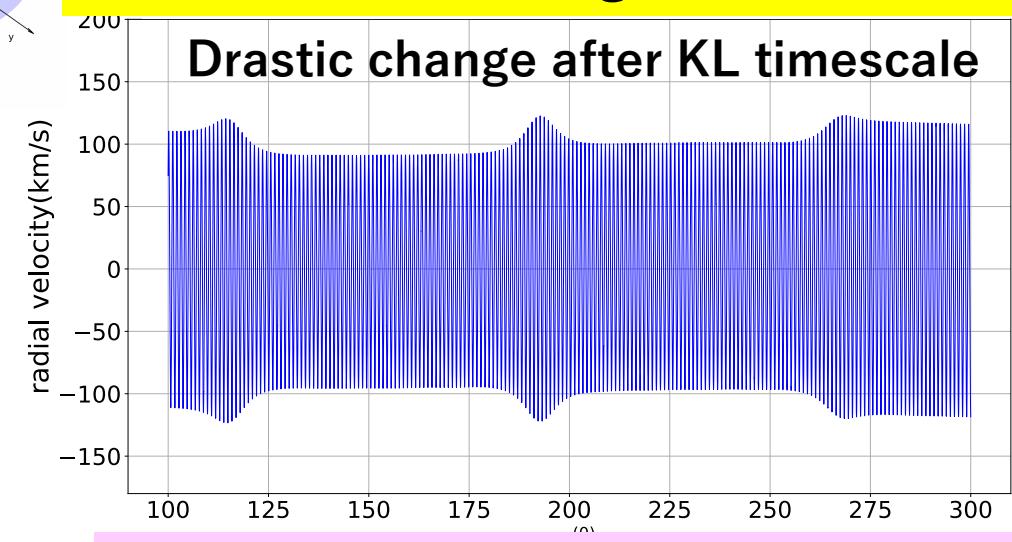


z-direction (near face-on) total RV

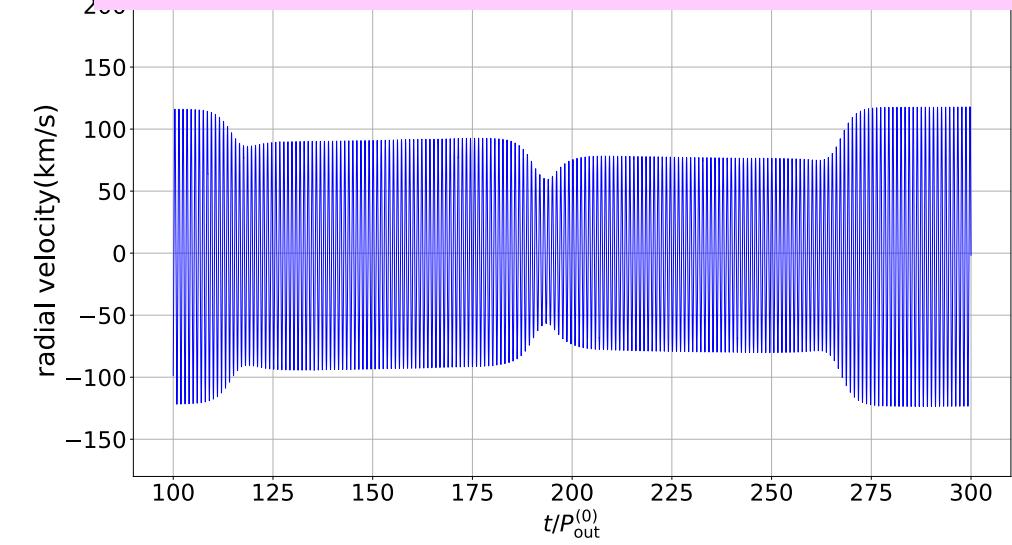


$$i_{\text{mut}} = 90^\circ$$

x-direction (near edge-on) total RV



z-direction (near face-on) total RV



# Inclined equal-mass binary

## Precession timescale

$$\frac{P_\Omega}{P_{\text{out}}} \approx \frac{80.7}{\cos i_{\text{mut}}} \left( \frac{m_1 + m_2 + m_*}{23 M_\odot} \right) \left( \frac{m_*}{3 M_\odot} \right)^{-1}$$

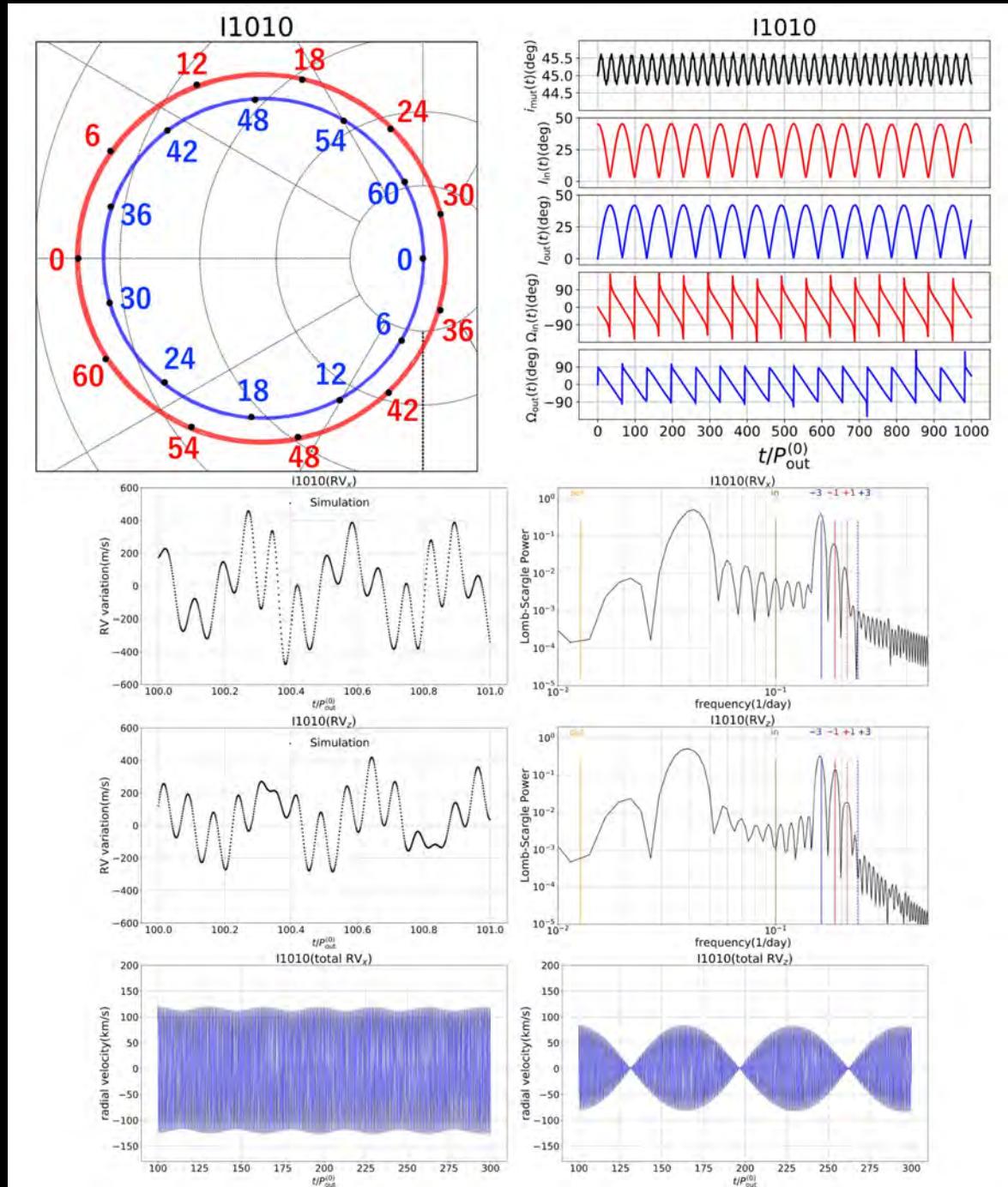
$$\times \left( \frac{P_{\text{out}}}{78.9 \text{ days}} \right) \left( \frac{P_{\text{in}}}{10.0 \text{ days}} \right)^{-1}$$

## Kozai-Lidov timescale

$$\frac{T_{\text{KL}}}{P_{\text{out}}} = \frac{m_1}{m_*} \left( \frac{P_{\text{out}}}{P_{\text{in}}} \right) (1 - e_{\text{out}}^2)^{3/2}$$

$$\approx 26 \left( \frac{m_1}{10 M_\odot} \right) \left( \frac{m_*}{3 M_\odot} \right)^{-1}$$

$$\times \left( \frac{P_{\text{out}}}{78.9 \text{ days}} \right) \left( \frac{P_{\text{in}}}{10 \text{ days}} \right)^{-1}$$



# Orthogonal equal-mass binary

## Precession timescale

$$\frac{P_\Omega}{P_{\text{out}}} \approx \frac{80.7}{\cos i_{\text{mut}}} \left( \frac{m_1 + m_2 + m_*}{23 M_\odot} \right) \left( \frac{m_*}{3 M_\odot} \right)^{-1}$$

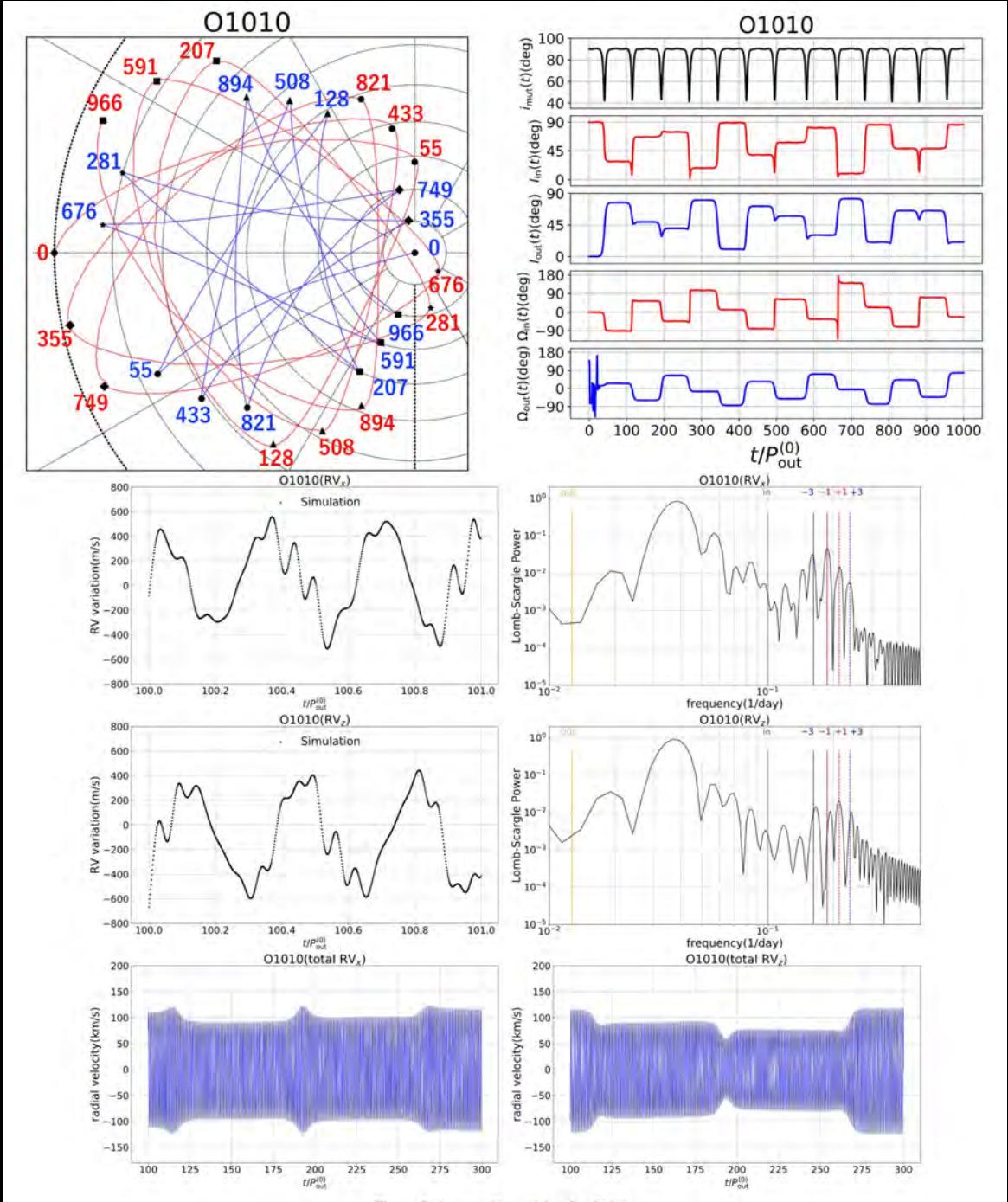
$$\times \left( \frac{P_{\text{out}}}{78.9 \text{ days}} \right) \left( \frac{P_{\text{in}}}{10.0 \text{ days}} \right)^{-1}$$

## Kozai-Lidov timescale

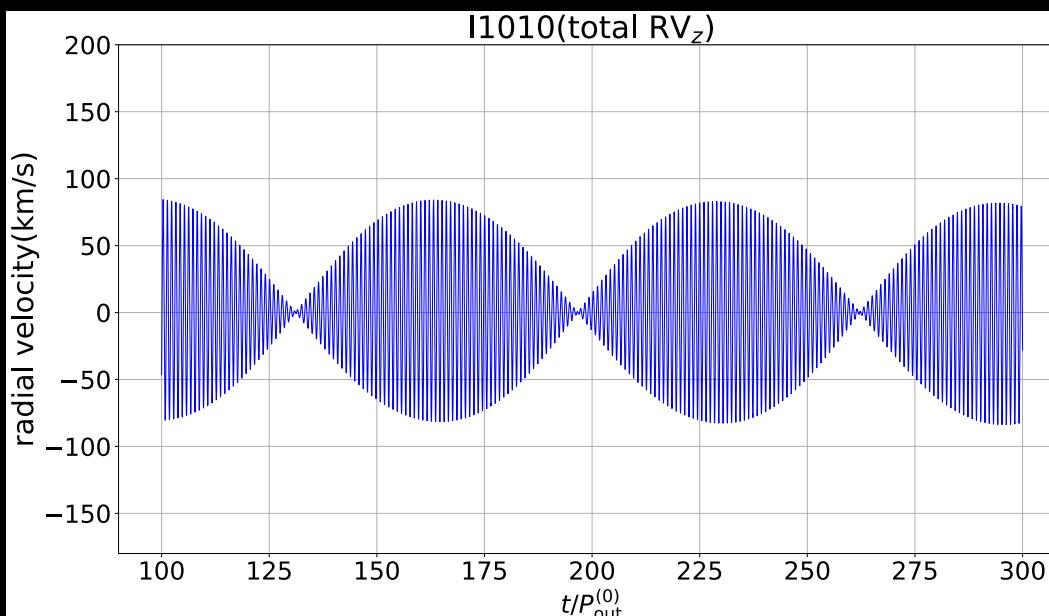
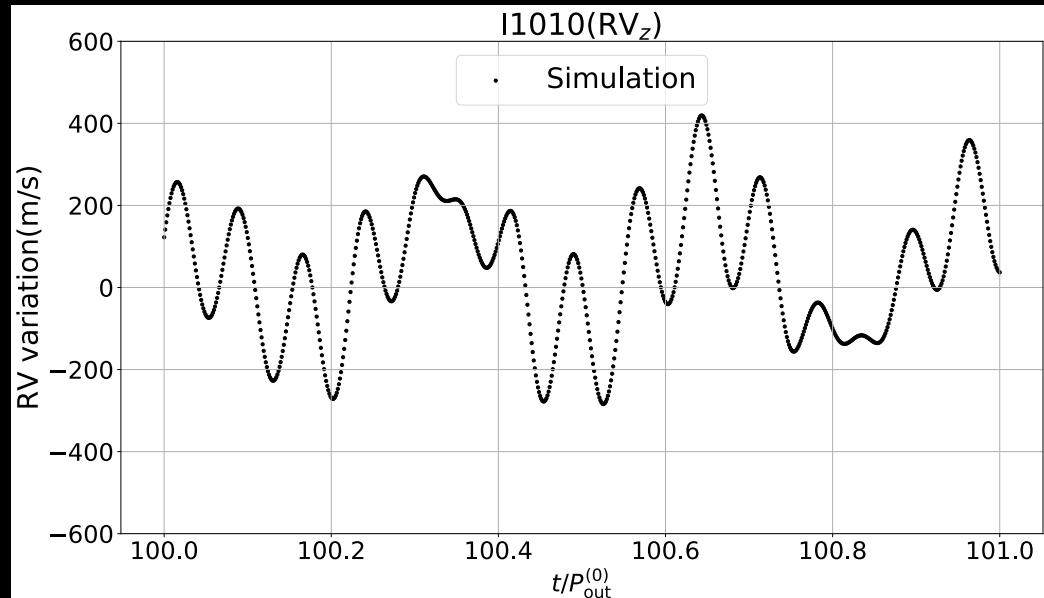
$$\frac{T_{\text{KL}}}{P_{\text{out}}} = \frac{m_1}{m_*} \left( \frac{P_{\text{out}}}{P_{\text{in}}} \right) (1 - e_{\text{out}}^2)^{3/2}$$

$$\approx 26 \left( \frac{m_1}{10 M_\odot} \right) \left( \frac{m_*}{3 M_\odot} \right)^{-1}$$

$$\times \left( \frac{P_{\text{out}}}{78.9 \text{ days}} \right) \left( \frac{P_{\text{in}}}{10 \text{ days}} \right)^{-1}$$



# Non-coplanar effect (precession+Kozai-Lidov)



**Inner BH binary**

**$10M_{\odot} + 10M_{\odot}$**

**Initial orbital inclination 45 deg.**

short-period modulation

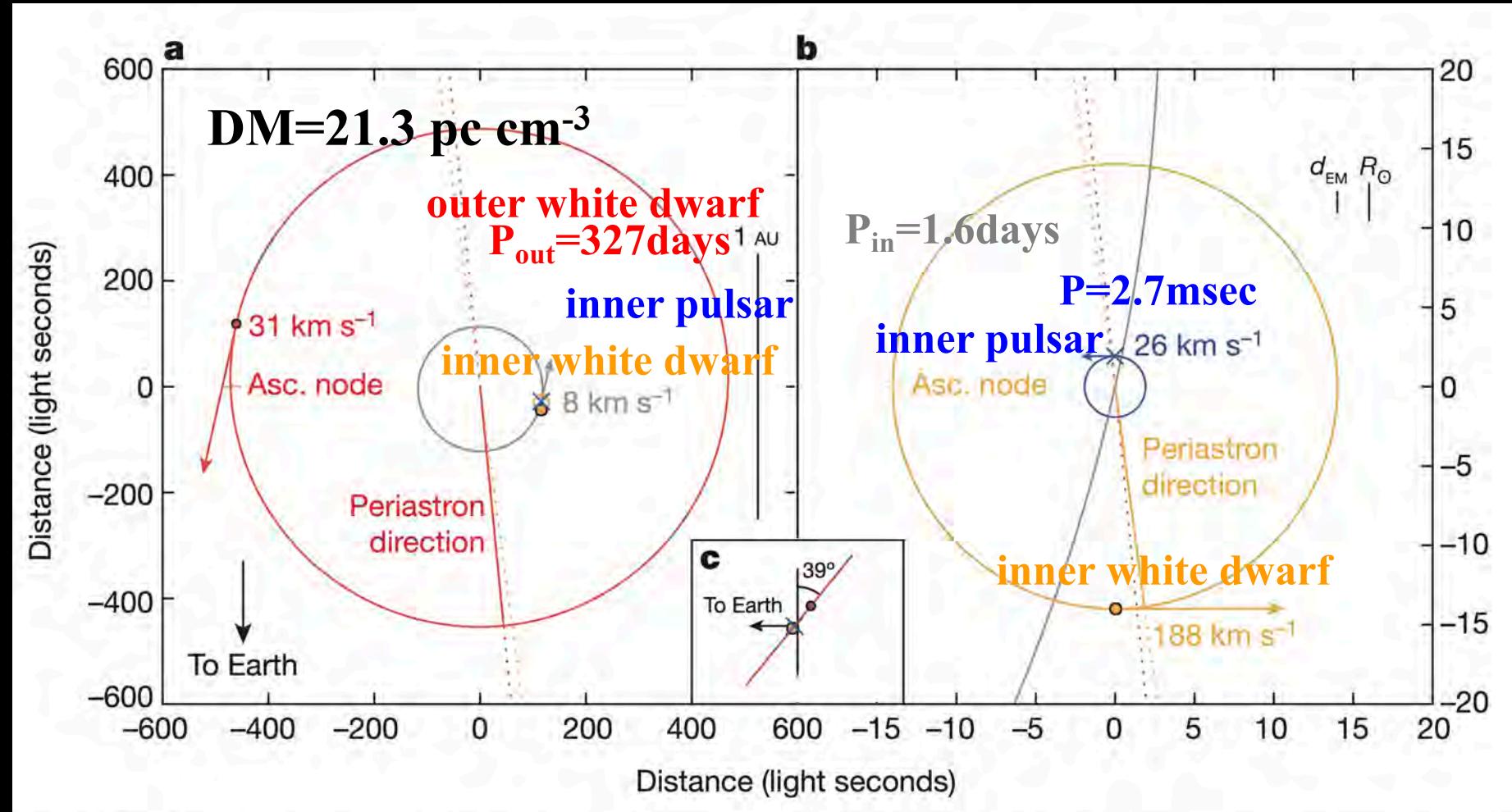
(inner binary orbital period/2)  
of  $O(100\text{m/s})$

long-period modulation

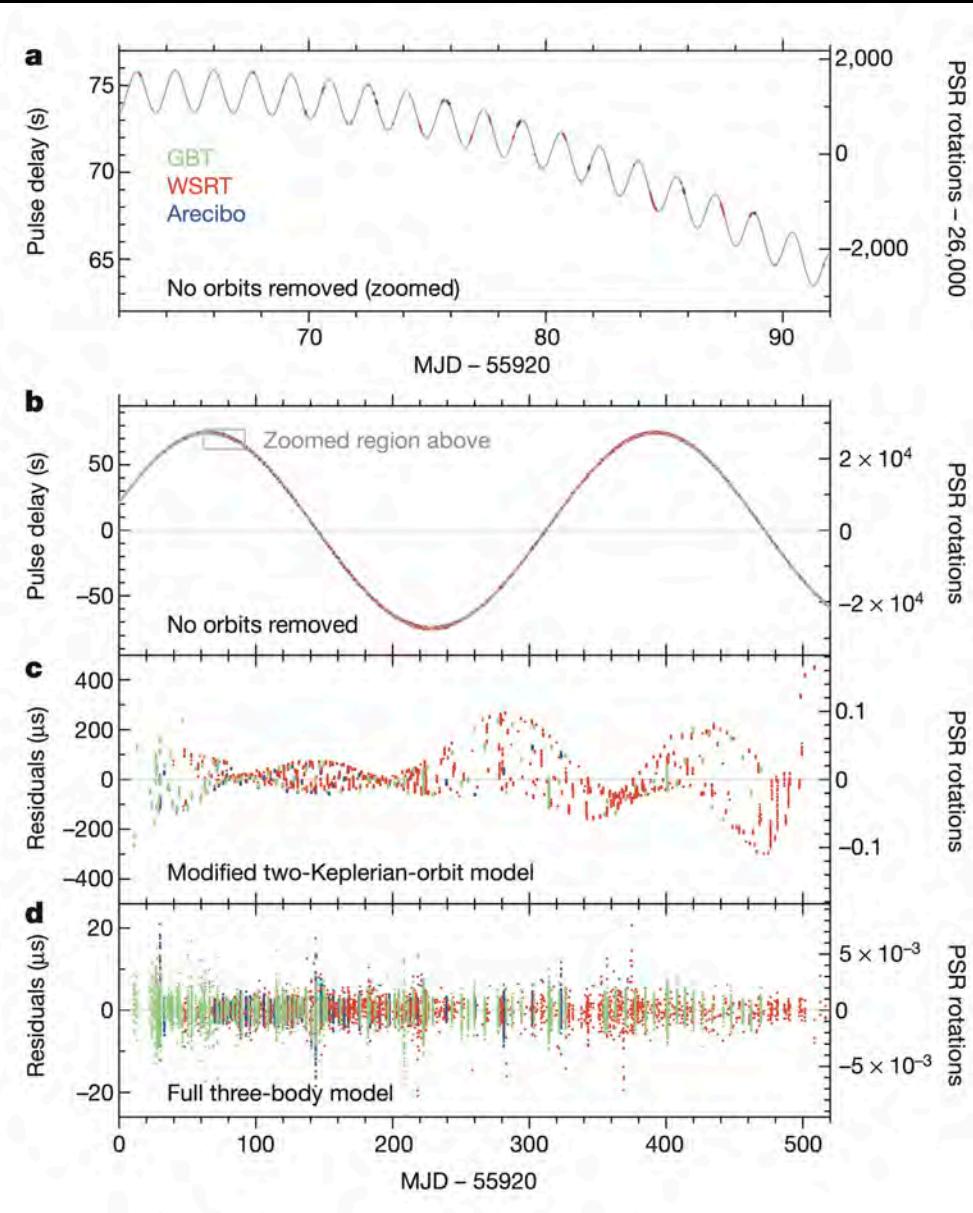
(orbital precession + Kozai-Lidov  
effect over the KL time-scale)  
of  $O(100\text{km/s})$

Hayashi & YS (2020)

# PSR J0337+1715: a hierarchical triple comprising an inner compact WD+pulsar binary



# PSR J0337+1715: triple architecture revealed by pulsar timing analysis



PSR J0337+1715	
inner orbital period (pulsar+WD)	1.629401788(5) day
outer orbital period (WD)	327.257541(7) day
pulsar spin period	2.73258863244(9) msec
mutual orbital inclination	0.0120(17) deg. <b>highly circular &amp; coplanar !</b>
Pulsar mass	$1.4378(13) M_{\odot}$
Inner WD mass	$0.19751(15) M_{\odot}$
Outer WD mass	$0.4101(3) M_{\odot}$

Ransom et al. Nature 505 (2014) 520

# Radial velocity vs. Pulsar arrival timing

- Radial velocity monitoring
  - High-resolution spectroscopy required for 10 m/s precision
  - Limited to targeted monitoring of nearby & bright stars
- Pulsar arrival timing analysis
  - Very precise measurement feasible
  - can survey almost the entire Galaxy
  - Systematic survey (Pulsar Timing Array) operating
- The fraction of triples with a tertiary star (RV) or a tertiary pulsar is largely unknown, and therefore they are complementary. It is worthwhile to explore simultaneously

# Pulsar arrival time delays

- Unperturbed Rømer delay

- due to the unperturbed Keplerian motion of a tertiary pulsar around the center of mass of the inner binary

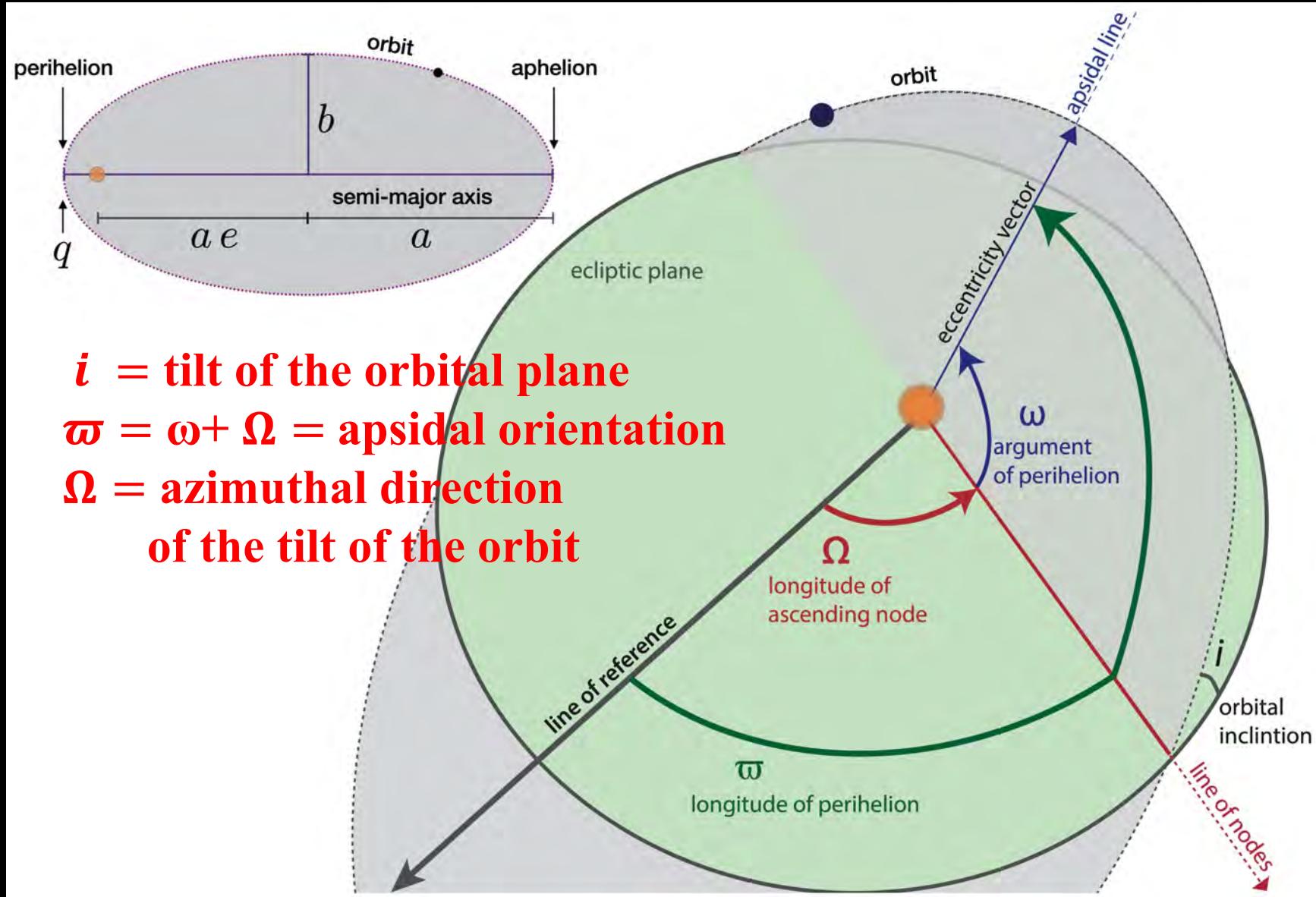
- Relativistic delays

- Einstein delay (gravitational redshift due to the eccentric orbit)
  - Shapiro delay (photon travel time change due to the space curvature)

- Perturbed Rømer delay modulation

- due to perturbed Keplerian motion of a tertiary pulsar from the inner binary motion

# Keplerian orbital elements



# Unperturbed Rømer delay

- **Rømer delay** (corresponding to the Keplerian motion around the central binary of total mass  $m_{12}$ )

$$\Delta_{\text{R,Kep}}(t) = x[\sin \omega_{\text{out}}(\cos E_{\text{out}} - e_{\text{out}}) + \sqrt{1 - e_{\text{out}}^2} \cos \omega_{\text{out}} \sin E_{\text{out}}]$$

Eccentric anomaly  $E_{\text{out}}=E_{\text{out}}(t)$  via the Kepler equation

$$2\pi t = P_{\text{out}}(E_{\text{out}} - e_{\text{out}} \sin E_{\text{out}})$$

Semi-amplitude of the Romer delay

$$x \equiv \frac{m_{12}}{m_{123}} \frac{a_{\text{out}} \sin I_{\text{out}}}{c} \approx 570 \text{ sec} \left( \frac{m_{12}}{m_{123}} \right) \left( \frac{m_{123}}{20 M_{\odot}} \right)^{1/3} \left( \frac{P_{\text{out}}}{100 \text{ days}} \right)^{2/3} \sin I_{\text{out}}$$

# Relativistic delays

## ■ Einstein delay

$$\Delta_E(t) = \gamma_E \sin E_{\text{out}}$$

Gravitational redshift due to the eccentric orbital motion of the tertiary pulsar around  $m_{12}$

Semi-amplitude of the Einstein delay

$$\begin{aligned}\gamma_E &\equiv \left(\frac{\mathcal{G}}{c^3}\right)^{2/3} \left(\frac{P_{\text{out}}}{2\pi}\right)^{1/3} e_{\text{out}} \frac{m_{12}(m_3 + 2m_{12})}{m_{123}^{4/3}} \\ &\approx 2.4 \text{ msec} \left(\frac{P_{\text{out}}}{100 \text{ days}}\right)^{1/3} \left(\frac{m_{12}}{20 M_\odot}\right) \left(\frac{m_{123}}{20 M_\odot}\right)^{-1/3} \left(1 + \frac{m_{12}}{m_{123}}\right) \left(\frac{e_{\text{out}}}{0.01}\right)\end{aligned}$$

## ■ Shapiro delay

Photon travel time change due to the curvature of the space-time

$$\begin{aligned}\Delta_S(t) &= -2r \ln [1 - e_{\text{out}} \cos E_{\text{out}} \\ &\quad - s (\sin \omega_{\text{out}} (\cos E_{\text{out}} - e_{\text{out}}) + \sqrt{1 - e_{\text{out}}^2} \cos \omega_{\text{out}} \sin E_{\text{out}})]\end{aligned}$$

range parameter  
shape parameter

$$r \equiv \frac{\mathcal{G}m_{12}}{c^3} \approx 98 \text{ } \mu\text{sec} \left(\frac{m_{12}}{20 M_\odot}\right)$$
$$s \equiv \sin I_{\text{out}}.$$

Significantly large for  $s=1$   
(edge-on) systems

# Perturbed Rømer delay modulation

Modulation due to the inner binary motion in a coplanar circular orbit

$$\Delta_{\text{R,BBH}}(t) \equiv \frac{z_{\text{BBH}}(t)}{c} = \frac{15}{16} \frac{K_{\text{BBH}} P_{\text{in}}}{4\pi c} \sin I_{\text{out}} \frac{2\nu_{\text{in}}}{2\nu_{\text{in}} - 3\nu_{\text{out}}} \sin(\nu_{-3} t + \theta_{0,-3}) \\ + \frac{3}{16} \frac{K_{\text{BBH}} P_{\text{in}}}{4\pi c} \sin I_{\text{out}} \frac{2\nu_{\text{in}}}{2\nu_{\text{in}} - \nu_{\text{out}}} \sin(\nu_{-1} t + \theta_{0,-1}).$$

$$\nu_{-3} \equiv 2\nu_{\text{in}} - 3\nu_{\text{out}},$$

$$\nu_{-1} \equiv 2\nu_{\text{in}} - \nu_{\text{out}}.$$

Semi-amplitude of the perturbed Rømer delay modulation

$$\frac{K_{\text{BBH}} P_{\text{in}}}{4\pi c} \sin I_{\text{out}} = \frac{1}{2} \frac{m_1 m_2}{m_{12}^2} \left( \frac{m_{12}}{m_{123}} \right)^{2/3} \left( \frac{P_{\text{in}}}{P_{\text{out}}} \right)^{7/3} x \\ \approx 23 \text{ msec} \left( \frac{K_{\text{BBH}}}{100 \text{ m/s}} \right) \left( \frac{P_{\text{in}}}{10 \text{ days}} \right) \sin I_{\text{out}},$$

# Examples of pulsar arrival timing curves for triples

Based on analytic expressions  
by Backer & Hellings (1986)  
and Morais & Correia 2008, 2011)

$$m_1 = m_2 = 10M_{\odot}$$

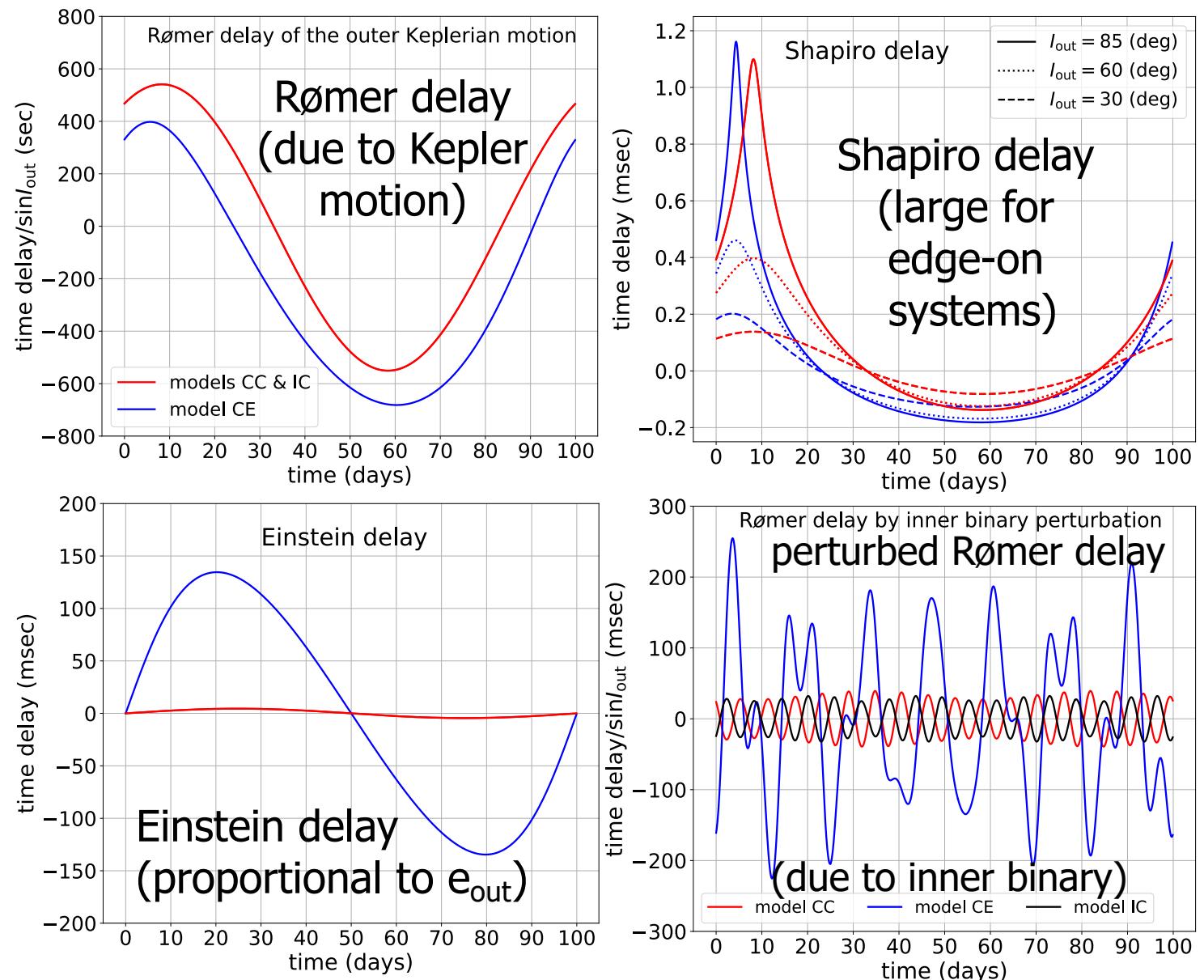
$$m_3 = 1.4M_{\odot}$$

$$P_{\text{out}} = 100 \text{ days}$$

$$P_{\text{in}} = 10 \text{ days}$$

- **Model CC (Coplanar Circular)**
  - $e_{\text{out}} = 0.01, e_{\text{in}} = 0.0, i_{\text{mut}} = 0^\circ$
- **Model CE (Coplanar Eccentric)**
  - $e_{\text{out}} = 0.3, e_{\text{in}} = 0.02, i_{\text{mut}} = 0^\circ$
- **Model IC (Inclined Circular)**
  - $e_{\text{out}} = 0.01, e_{\text{in}} = 0.0, i_{\text{mut}} = 45^\circ$

Hayashi & YS (2020, submitted)



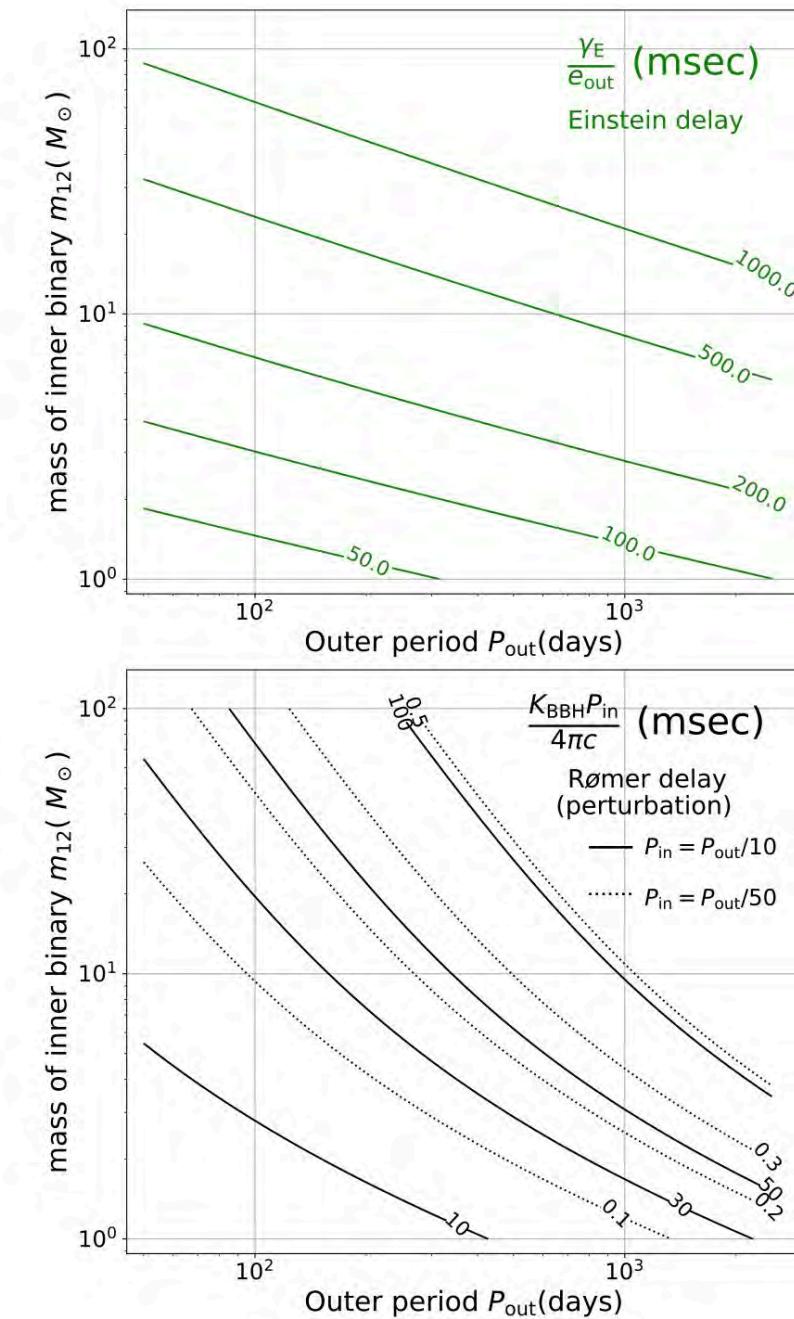
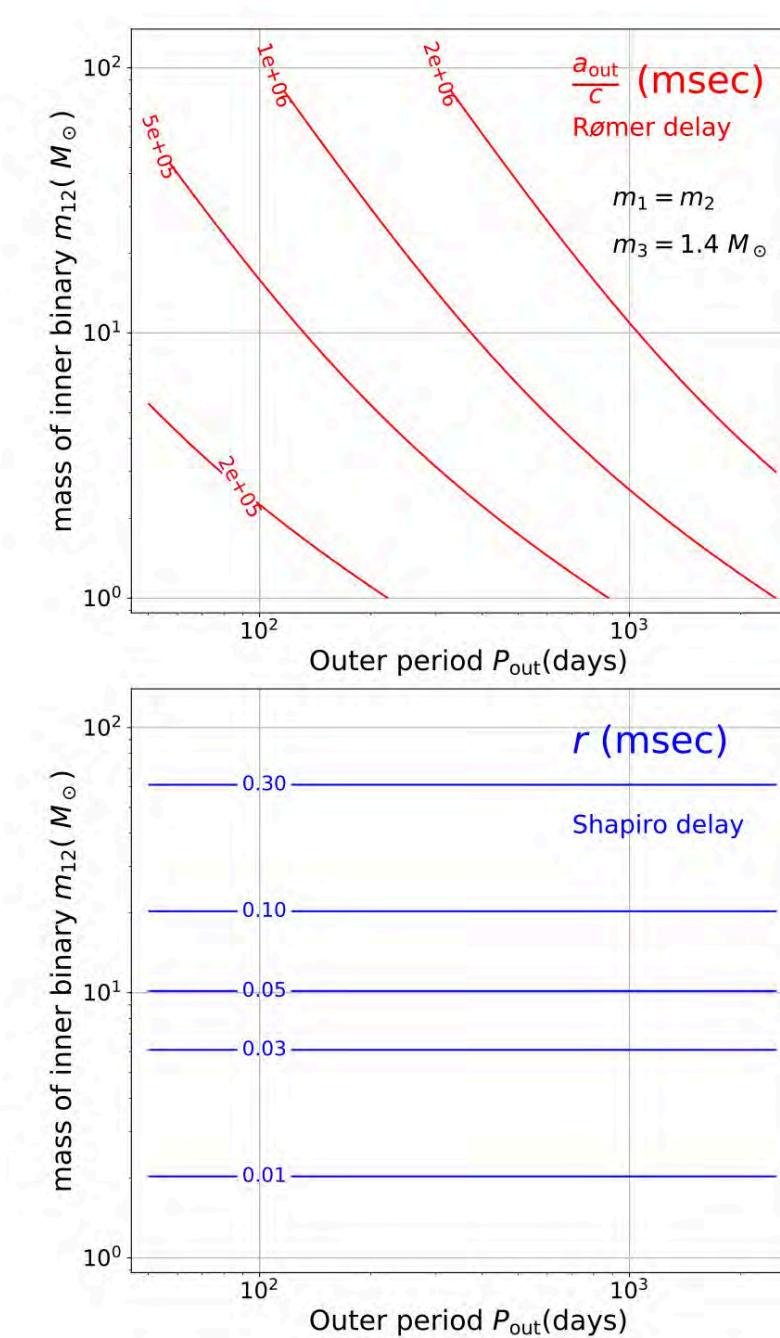
# Comparison of arrival time delays

$$m_{12} = m_1 + m_2$$

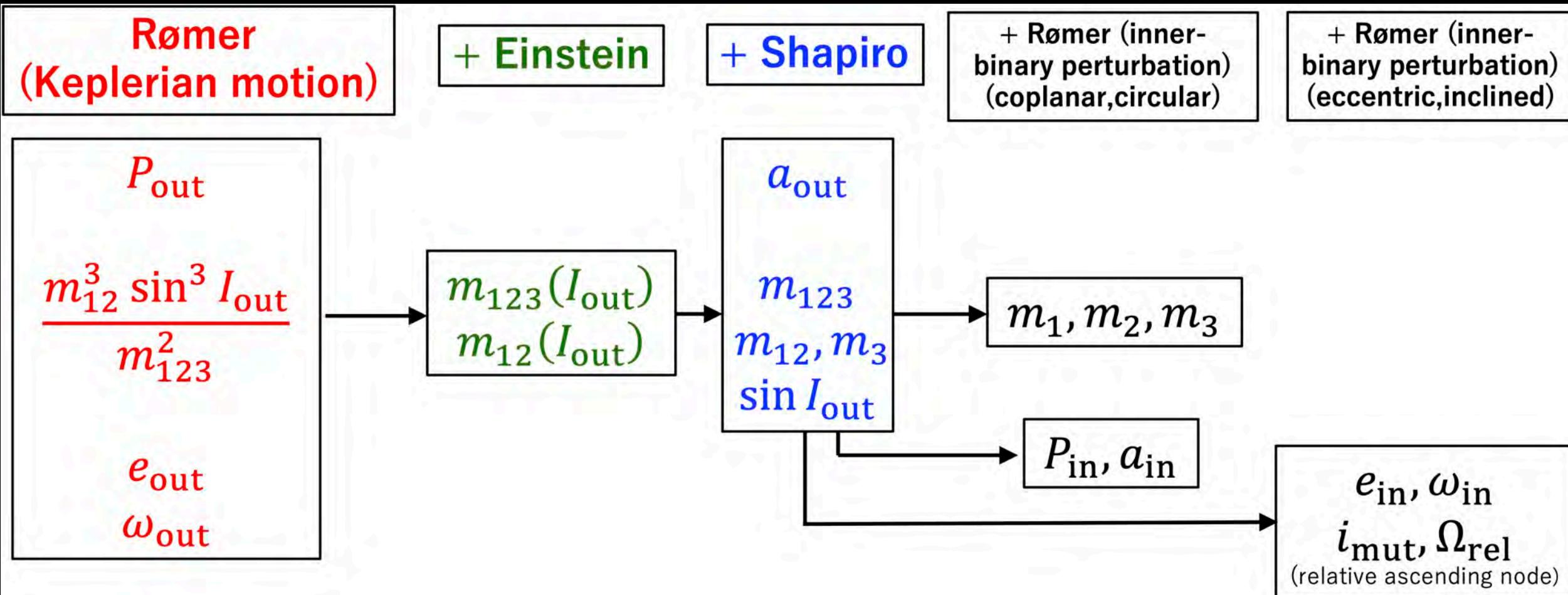
$$m_1 = m_2$$

$$m_3 = 1.4 M_{\odot}$$

- Those time-delay measurements break the degeneracy of the system parameters



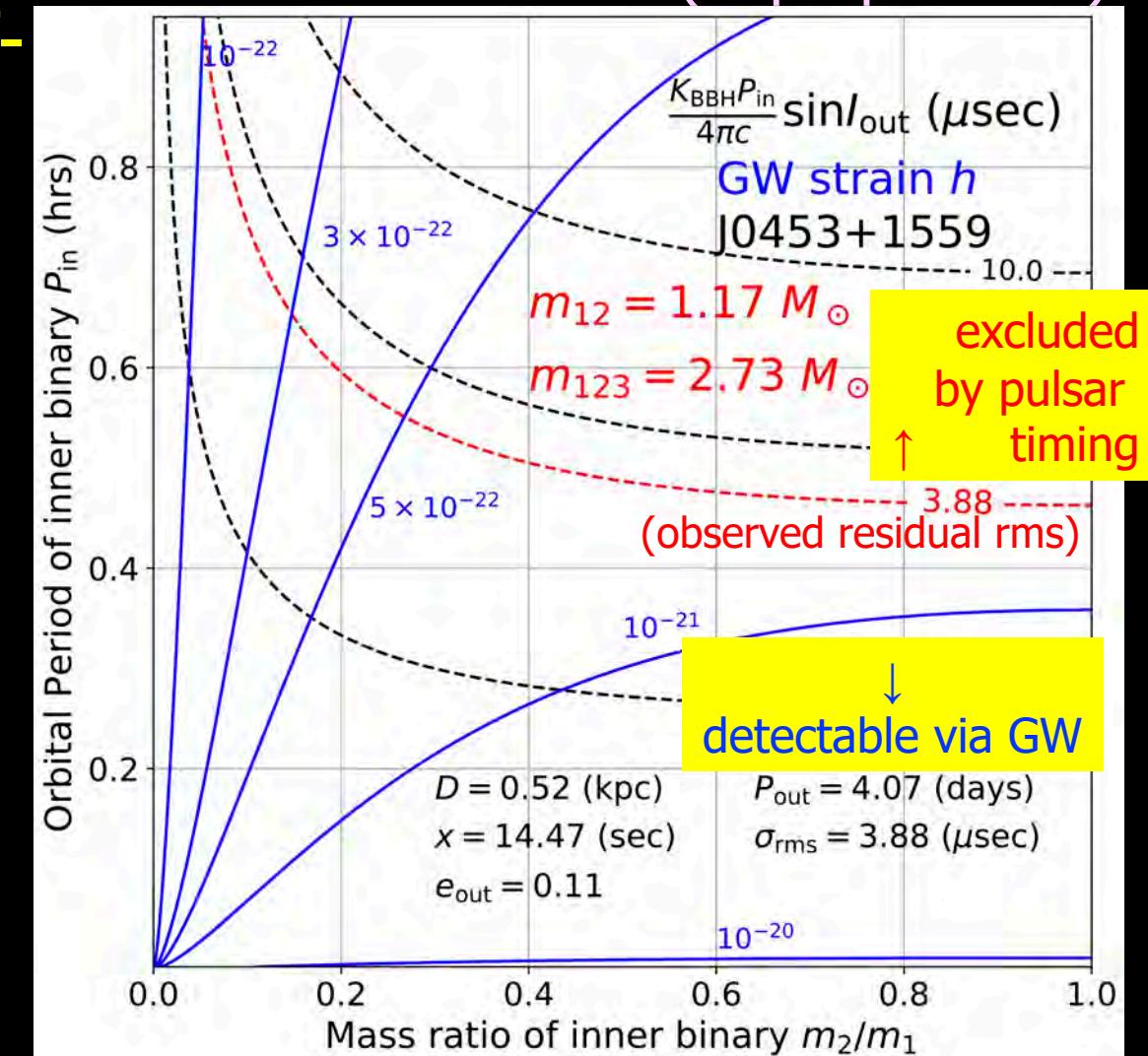
# Unveiling the triple system parameters from the pulsar arrival timing analysis



# Proof-of-concept using known NS binaries

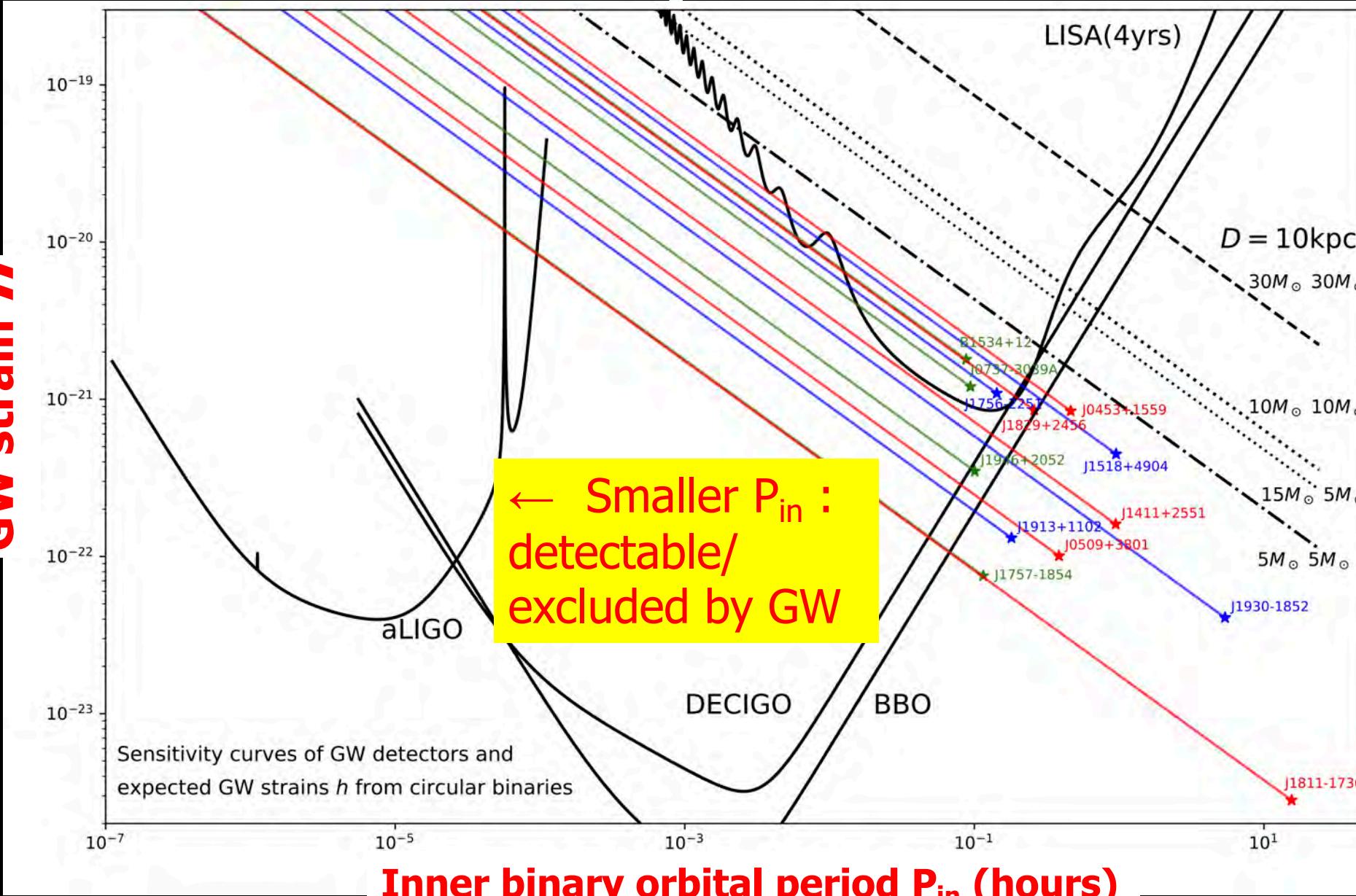
- No candidate for a pulsar-BH binary yet
- Consider known NS binaries as a proof-of-concept of our methodology
  - Given  $P_{\text{out}}$ , a large value of  $P_{\text{in}}$  is excluded by the **dynamical stability** of a possible inner binary in a triple system
  - A small value of  $P_{\text{in}}$  does not generate a detectable **Rømer delay modulation** (the inner binary is indistinguishable from a single object)
  - Such inner binaries, however, emit **gravitational wave** that is detectable with future instruments including LISA and DECIGO

Kumamoto, Hayashi, Takahashi  
& YS (in preparation)



# Constraints and predictions for NS binaries

GW strain  $h$



Circular and equal-mass inner binaries assumed

⇒ Larger  $P_{in}$  :  
detectable/  
excluded  
by pulsar timing

# Conclusions

*Everything not forbidden by the laws of nature  
is mandatory* – Carl Sagan "Contact"

- **Methodologies to search for wide-separation binary BHs** (likely but hidden progenitors of binary BHs detected by LIGO)
  - **Radial velocity of tertiary stars:** nearby star-BH system if detected from Gaia and/or TESS surveys
  - **Arrival timing of tertiary pulsars:** (even more distant) pulsar—BH systems if detected from future pulsar surveys

