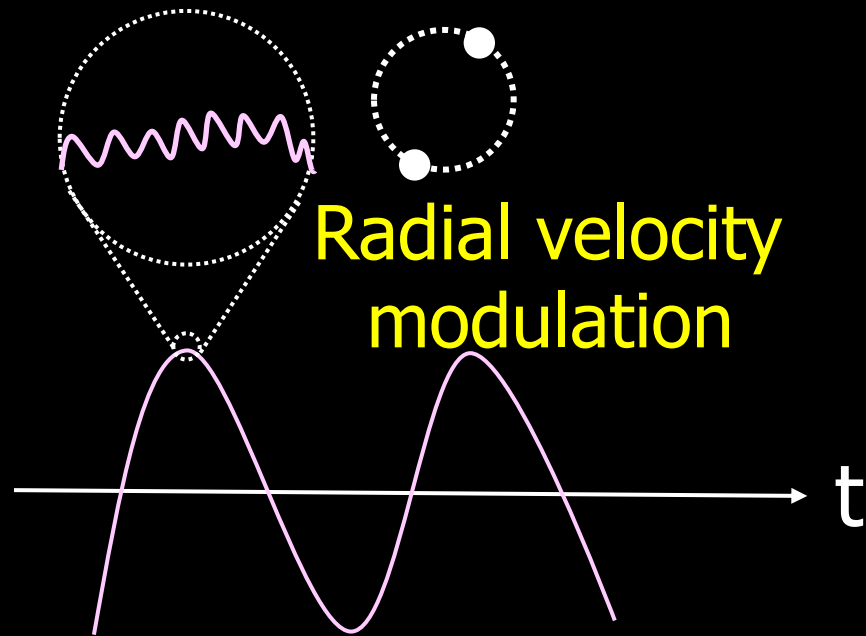
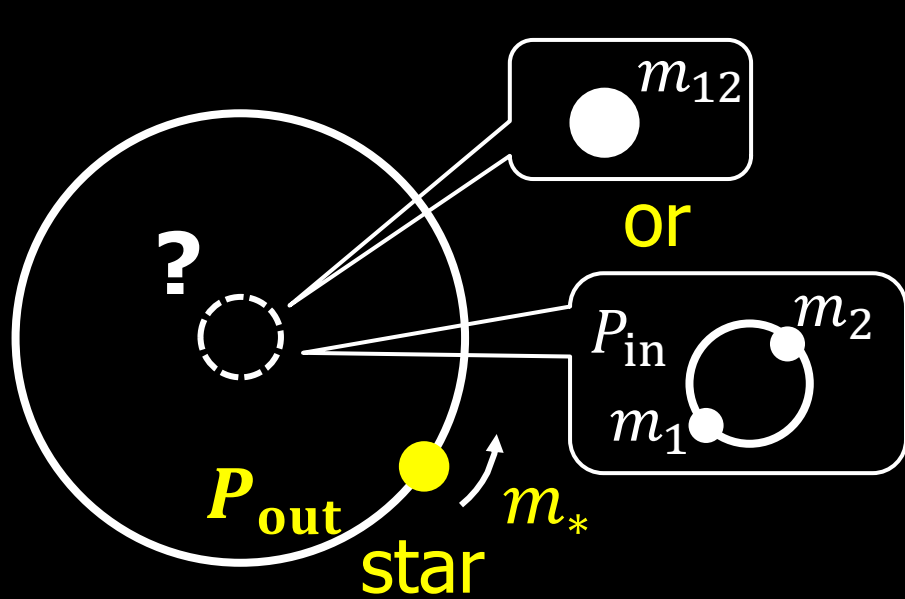


Signatures of an inner binary black hole with a tertiary orbiting star



Yasushi Suto Department of Physics and Research Center for the Early Universe
The University of Tokyo

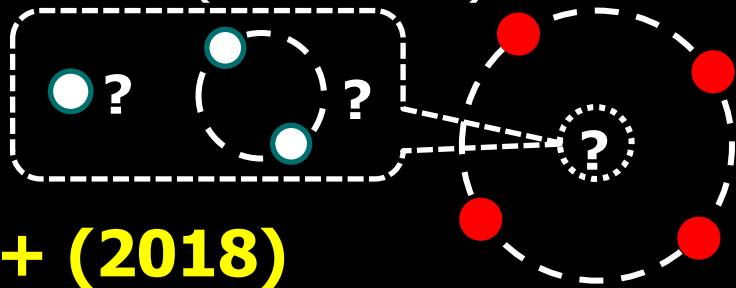
Astronomy session@ Copernicus World Congress, February 20 2023

Search for progenitors of LIGO binary BHs

star-BH binaries = star-BBH triples?

Gaia mission (2013-)

Astrometry of stars in Galaxy
~ 10^9 stars eventually
RV with 200-350m/s precision
for brightest stars (Katz 2018)



Yamaguchi+ (2018)

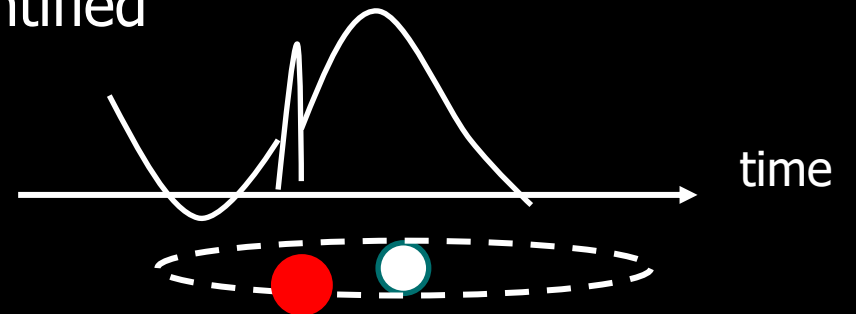
5-year mission may detect
200-1000 star-BH binaries

TESS mission (2018-)

photometry of nearby stars (~ 12mag)
transit planets

Masuda & Hotokezaka (2019)

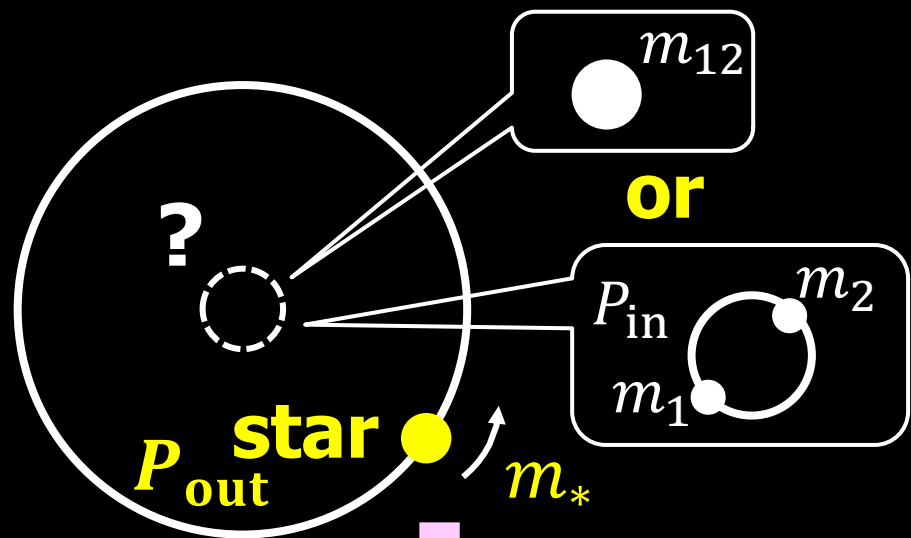
Light curve modulation
(relativistic effects, tidal deformation)
⇒ (10 – 100) star-BH binaries may be
identified



Some of them may be indeed a star-binary BH triple!

Can precise radial velocity follow-up unveil the inner BBH?

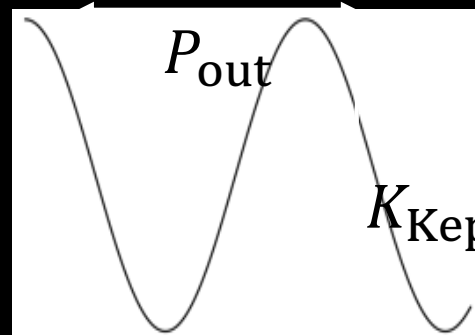
RV modulations of a tertiary star



high-precision RV follow-up

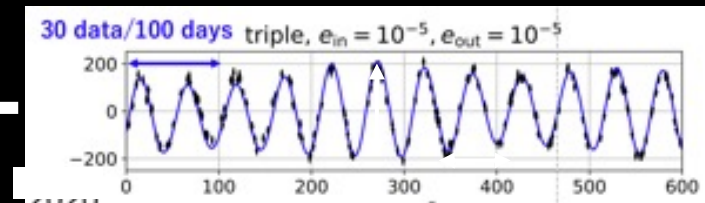
Keplerian motion RV
+ RV variations by inner binary

(i) Coplanar triple



Kepler motion + Short-term RV variations (inner-binary perturbation)

$$\text{Amp} \sim K_{Kep} \left(\frac{P_{in}}{P_{out}} \right)^{\frac{7}{3}}$$

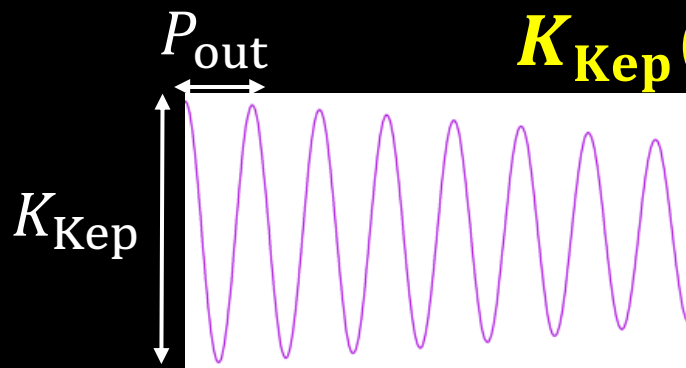


period $\sim P_{in}/2$

(ii) Non-coplanar triple

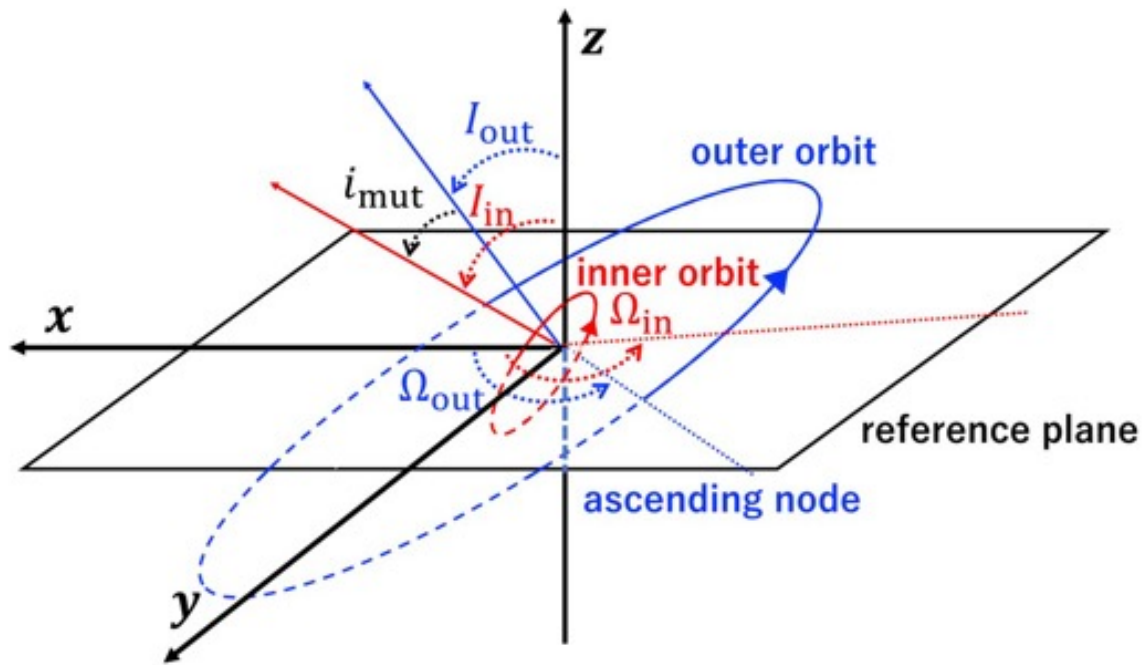
Inclination $I_{out}(t)$ modulated by precession and ZKL effect

$$K_{Kep}(t) = K_0 \sin I_{out}(t)$$



Amplitude of Kepler RV varies with a longer timescale

Examples of simulated triple systems



Hayashi & YS 2020, ApJ, 897, 29

Model	I_{out} (deg)	I_{in} (deg)	i_{mut} (deg)	m_1 (M_{\odot})	m_2 (M_{\odot})	e_{in}
P1010	90	90	0	10	10	10^{-5}
PE1010	90	90	0	10	10	0.2
R1010	90	270	180	10	10	10^{-5}
O1010	0	90	90	10	10	10^{-5}
I1010	0	45	45	10	10	10^{-5}
P0218	90	90	0	18	2	10^{-5}
PE0218	90	90	0	18	2	0.2
R0218	90	270	180	18	2	10^{-5}
O0218	0	90	90	18	2	10^{-5}
I0218	0	45	45	18	2	10^{-5}

Note. P, PE, R, O, and I indicate prograde, prograde eccentric, retrograde, orthogonal, and inclined orbits.

$P_{out} = 78.9$ days

$P_{in} = 10$ days

equal-mass binary $10M_{\odot} + 10M_{\odot}$

unequal-mass binary $2M_{\odot} + 18M_{\odot}$

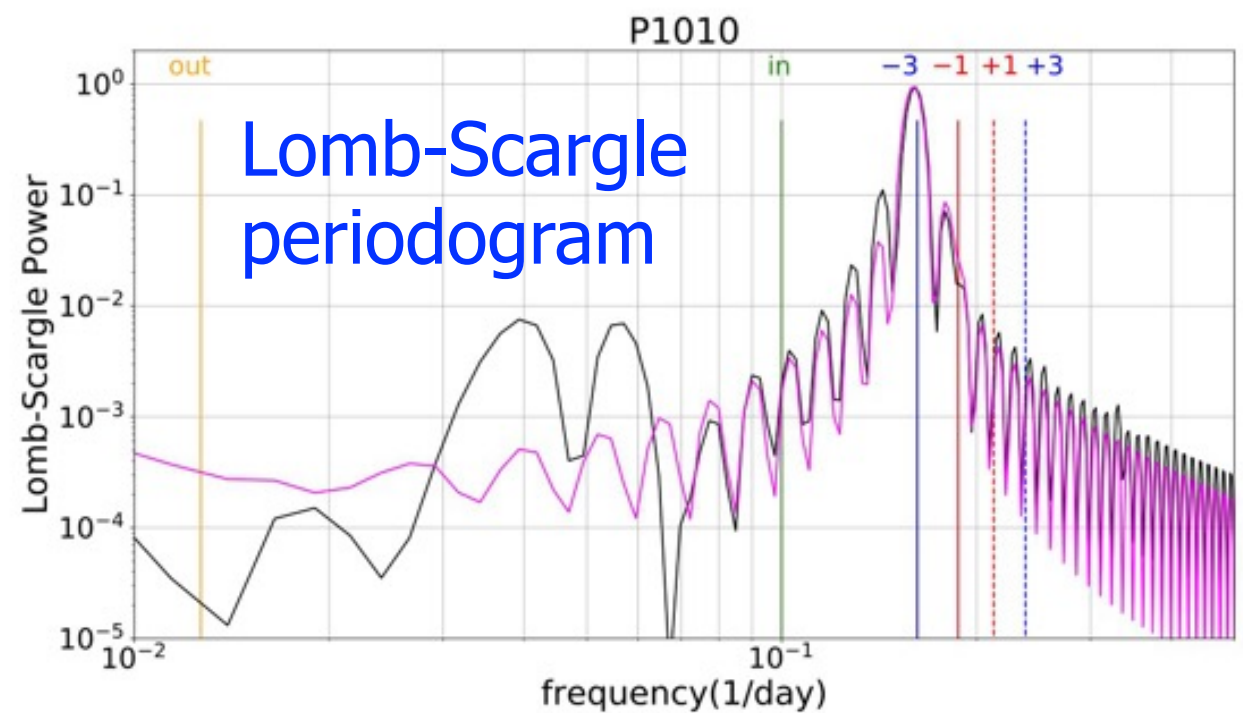
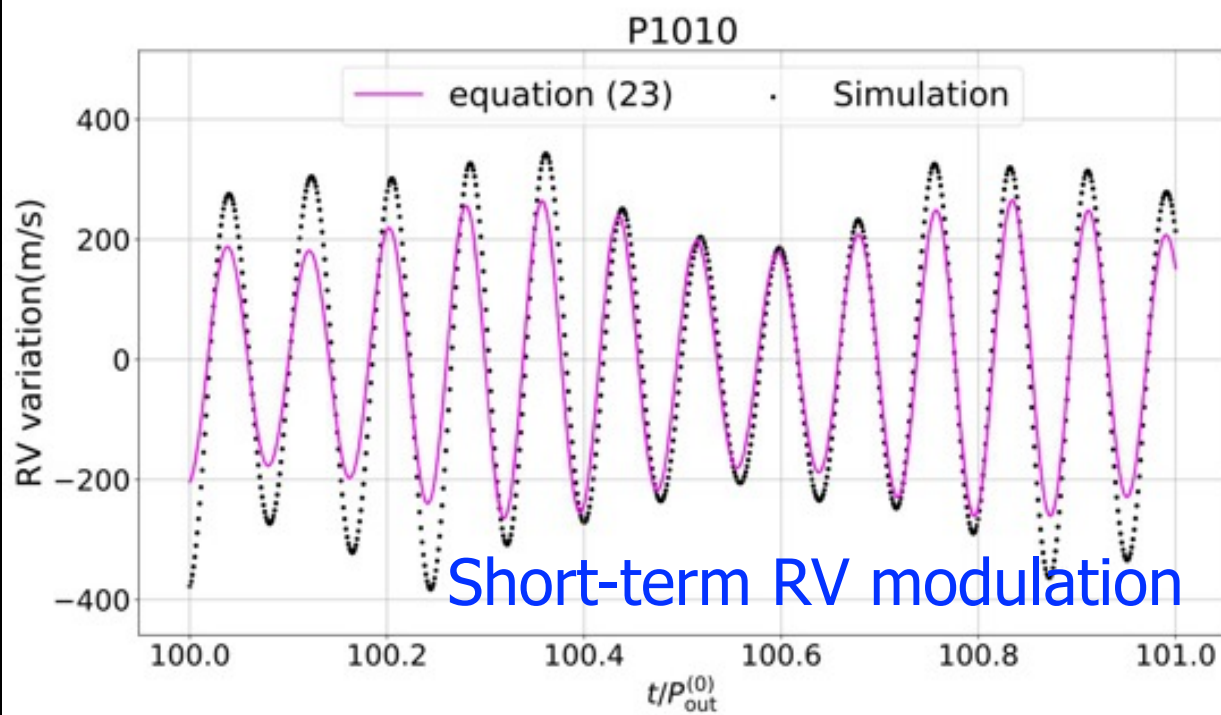
Coplanar prograde circular triples: radial velocity modulation at $\sim 2\nu_{in}$

equal-mass inner binary

Simulation against
Perturbative model
(Morais & Correia 2008, 2012)

$$\nu_{-3} \equiv 2\nu_{in} - 3\nu_{out},$$
$$\nu_{-1} \equiv 2\nu_{in} - \nu_{out}.$$

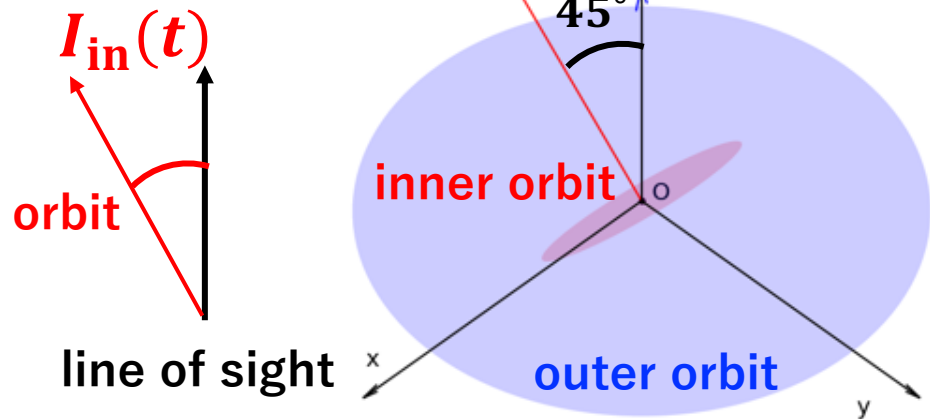
**ν_{in} : inner
orbital frequency**



Evolution of inclination for non-coplanar triples

$$i_{\text{mut}} = 45^\circ$$

$$t = 0P_{\text{out}}^{(0)}$$



$$P_{\text{out}} = 78.9 \text{ days}$$

$$P_{\text{in}} = 10 \text{ days}$$

$$m_1 = m_2 = 10M_{\odot}$$

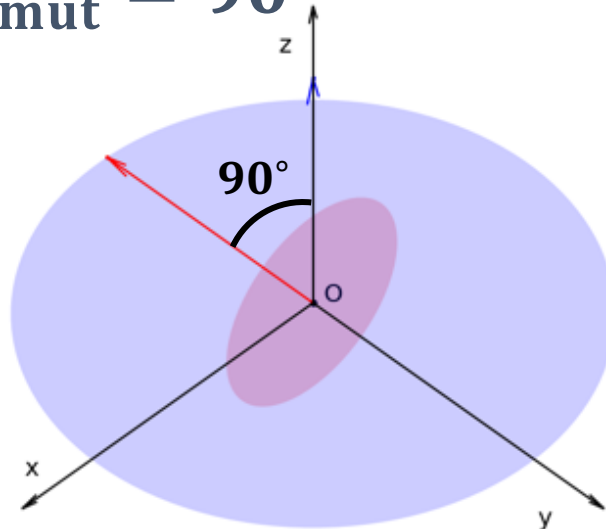
$$m_* = 3M_{\odot}$$

$$e_{\text{out}} = 0.03$$

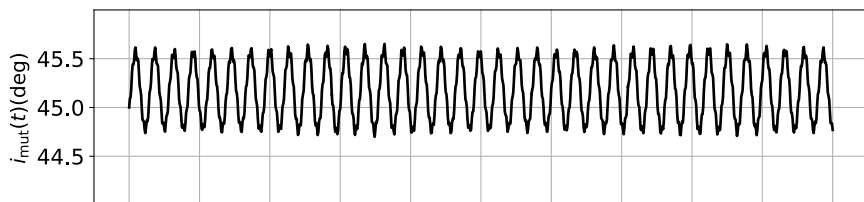
$$e_{\text{in}} = 10^{-5}$$

$$i_{\text{mut}} = 90^\circ$$

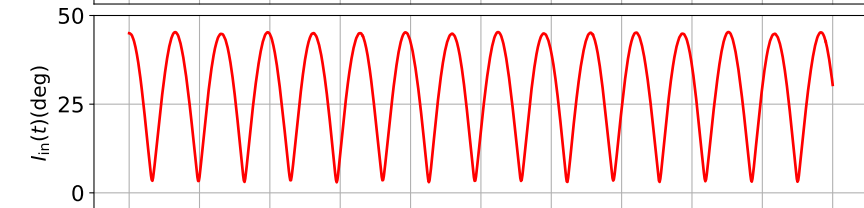
$$t = 0P_{\text{out}}^{(0)}$$



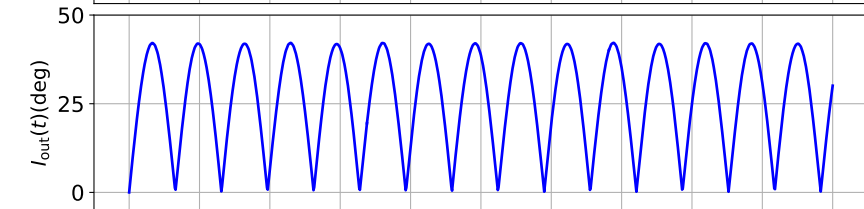
$$i_{\text{mut}}(t)$$



$$I_{\text{in}}(t)$$

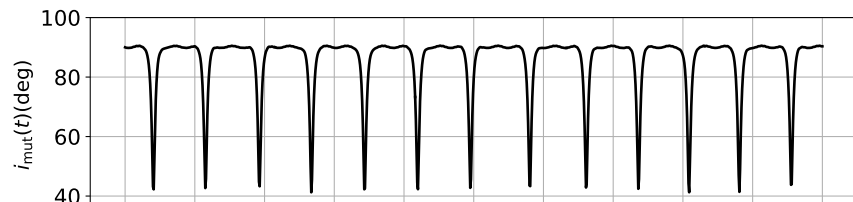


$$I_{\text{out}}(t)$$

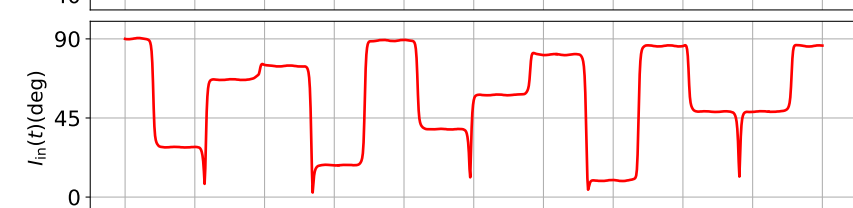


$$t/P_{\text{out}}^{(0)}$$

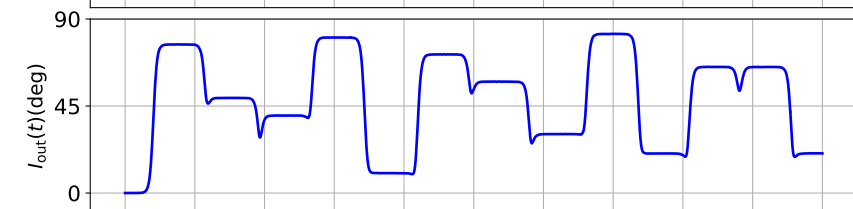
$$i_{\text{mut}}(t)$$



$$I_{\text{in}}(t)$$



$$I_{\text{out}}(t)$$



$$t/P_{\text{out}}^{(0)}$$

Evolution of inclination for non-coplanar triples

$t = 0P_{\text{out}}^{(0)}$

$t = 0P_{\text{out}}^{(0)}$

$i_{\text{mut}} = 45^\circ$

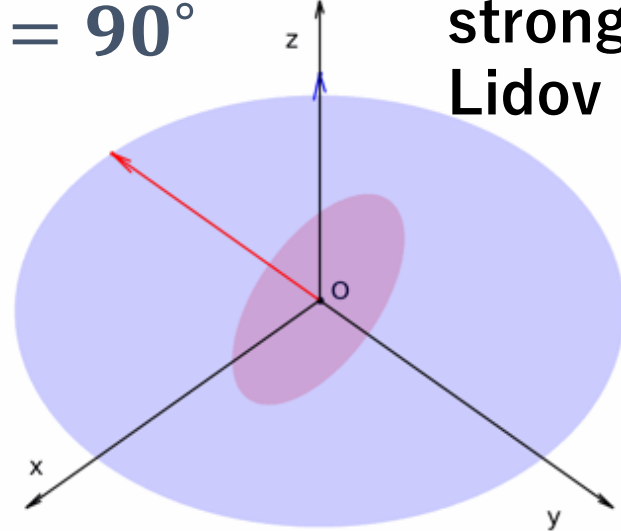
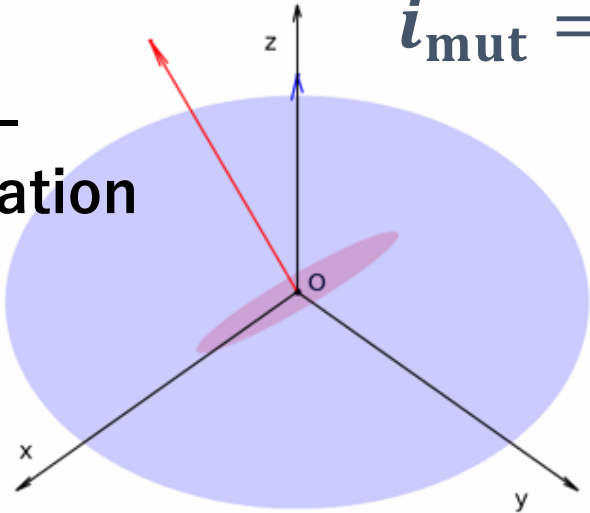
$i_{\text{mut}} = 90^\circ$

strong Kozai-Lidov oscillation

weak Kozai-Lidov oscillation

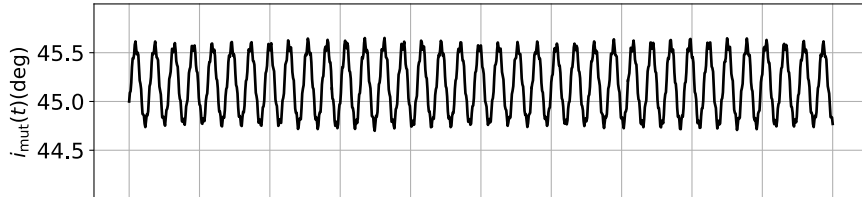
⇒ small-amplitude regular precession

⇒ large-amplitude sporadic precession

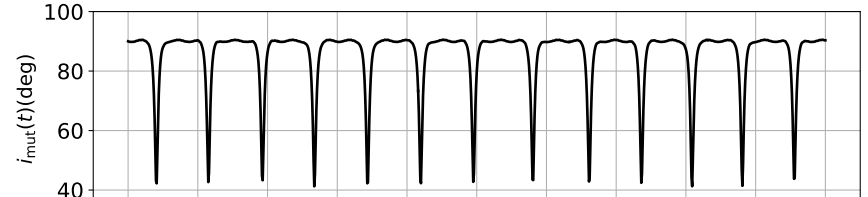


$$K_{\text{Kep}} = K_0 \sin I_{\text{out}}(t)$$

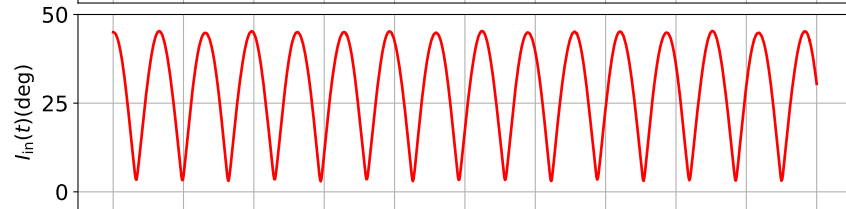
$i_{\text{mut}}(t)$



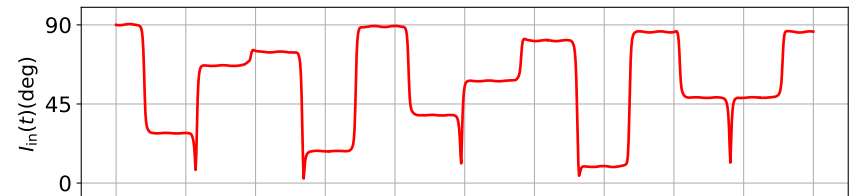
$i_{\text{mut}}(t)$



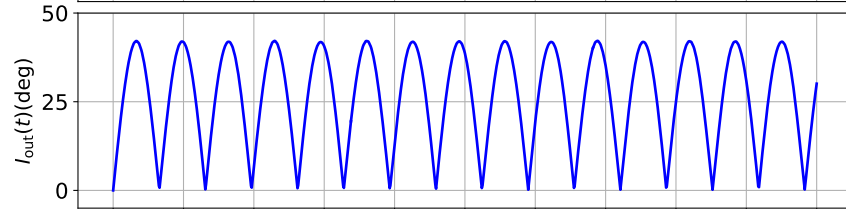
$I_{\text{in}}(t)$



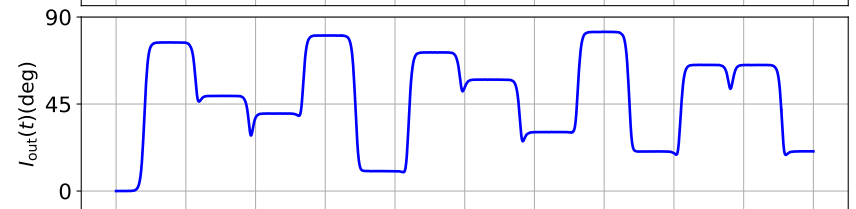
$I_{\text{in}}(t)$



$I_{\text{out}}(t)$



$I_{\text{out}}(t)$



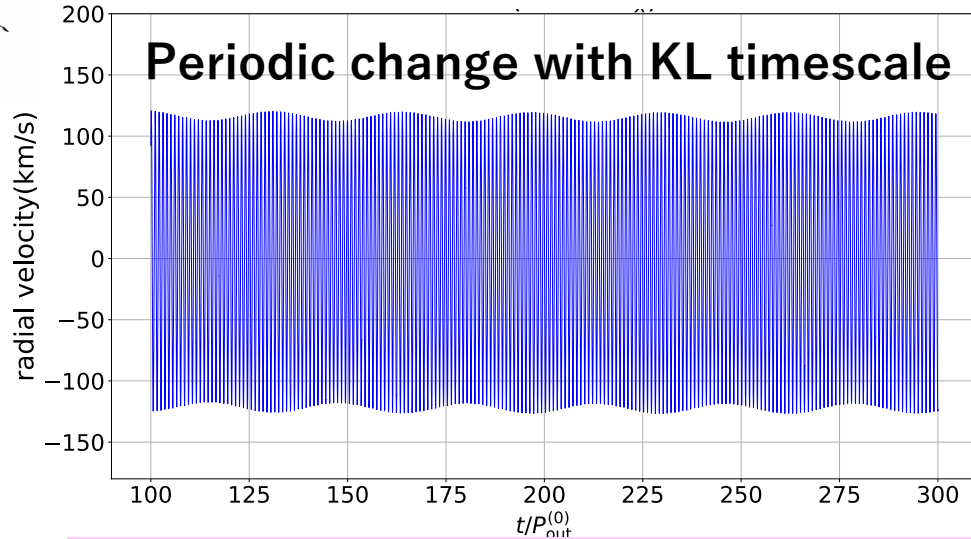
$t/P_{\text{out}}^{(0)}$

$t/P_{\text{out}}^{(0)}$

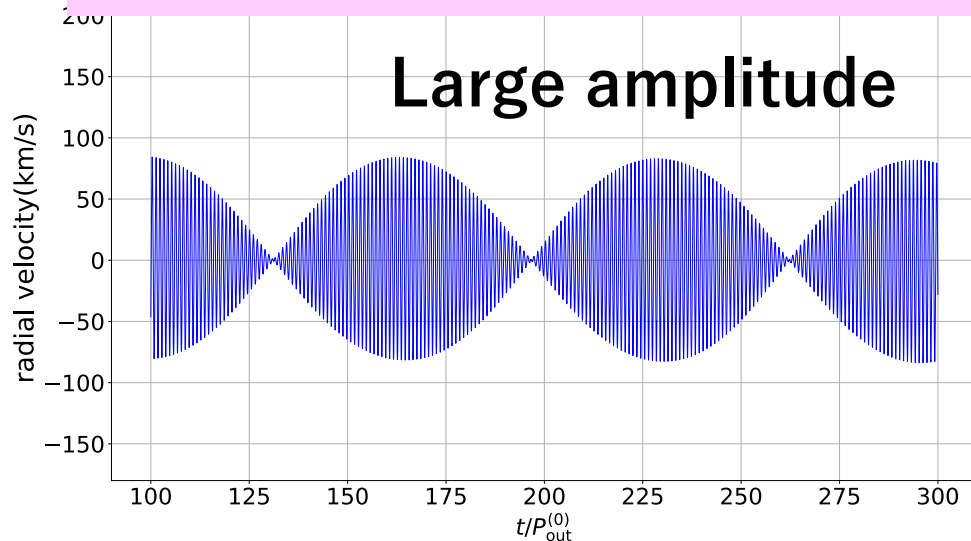
Evolution of radial velocity for non-coplanar triples

$i_{\text{mut}} = 45^\circ$ $K_{\text{Kep}} = K_0 \sin I_{\text{out}}(t)$

x-direction (near edge-on) total RV

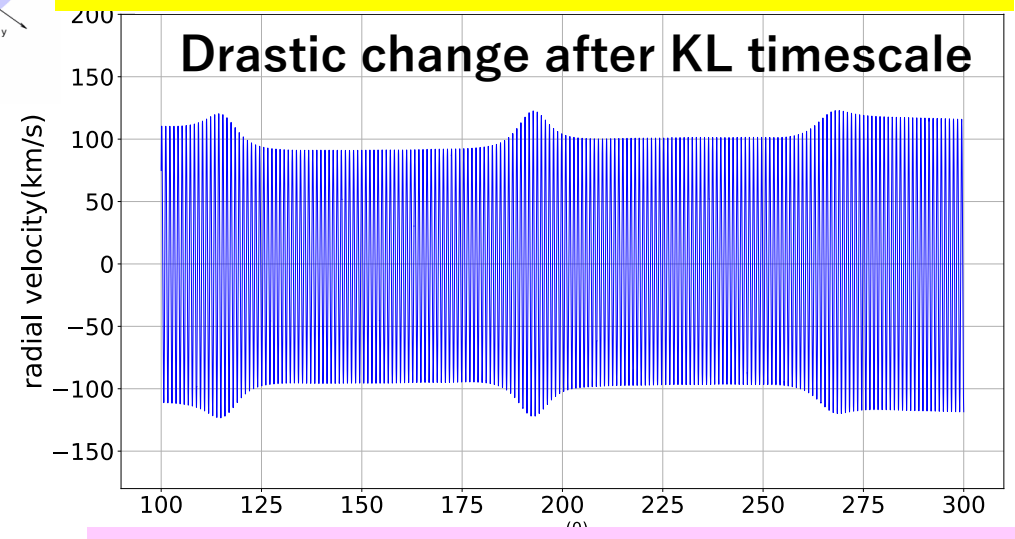


z-direction (near face-on) total RV

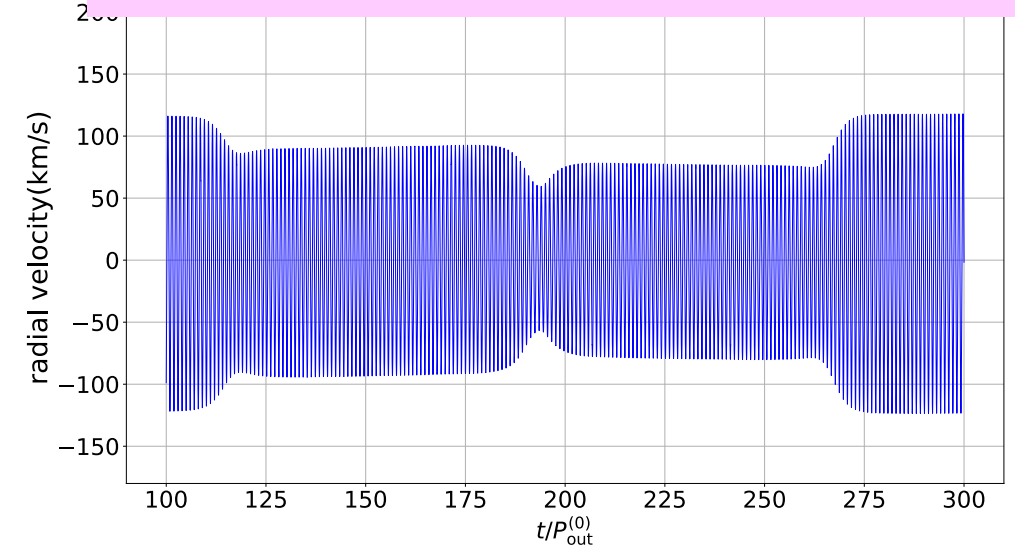


$i_{\text{mut}} = 90^\circ$

x-direction (near edge-on) total RV



z-direction (near face-on) total RV



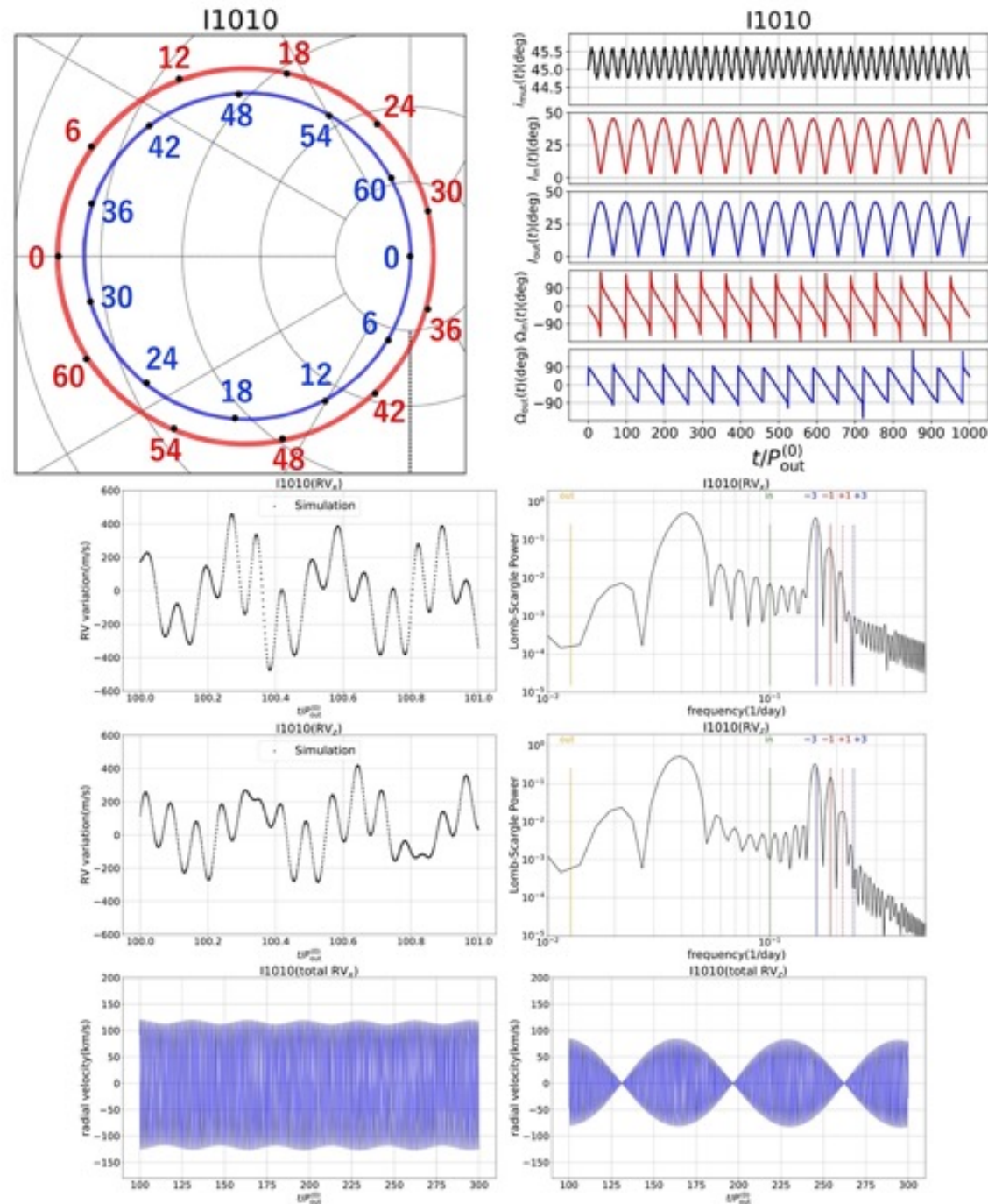
Inclined equal-mass binary

Precession timescale

$$\frac{P_\Omega}{P_{\text{out}}} \approx \frac{80.7}{\cos i_{\text{mut}}} \left(\frac{m_1 + m_2 + m_*}{23 M_\odot} \right) \left(\frac{m_*}{3 M_\odot} \right)^{-1} \\ \times \left(\frac{P_{\text{out}}}{78.9 \text{ days}} \right) \left(\frac{P_{\text{in}}}{10.0 \text{ days}} \right)^{-1}$$

Kozai-Lidov timescale

$$\frac{T_{\text{KL}}}{P_{\text{out}}} = \frac{m_1}{m_*} \left(\frac{P_{\text{out}}}{P_{\text{in}}} \right) (1 - e_{\text{out}}^2)^{3/2} \\ \approx 26 \left(\frac{m_1}{10 M_\odot} \right) \left(\frac{m_*}{3 M_\odot} \right)^{-1} \\ \times \left(\frac{P_{\text{out}}}{78.9 \text{ days}} \right) \left(\frac{P_{\text{in}}}{10 \text{ days}} \right)^{-1}$$



Dynamical signature of inner binary black holes in triple systems

- Radial velocity (RD) monitoring of future star-black hole binary candidates may reveal inner binary black holes (instead of single black holes) in those systems
 - short-term RD variations [Hayashi, Wang + YS: ApJ 890\(2020\)112](#)
 - periodic modulations of $O(1)$ percent of the Kepler orbital velocity amplitude with a half inner orbital period [Hayashi + YS: ApJ 897\(2020\)29](#)
 - long-term RD variations in inclined triples
 - the semi-amplitude of the Kepler orbital velocity modulated periodically by the precession of the inner and outer orbits over $(10-100)(P_{\text{out}}/P_{\text{in}})P_{\text{out}}$